

Section - A

(1) $|adj A| = |A|^2 \Rightarrow 144 = |A|^2 \Rightarrow |A| = \pm 12 \therefore$ option (c)

(2) $\begin{vmatrix} 2 \sin x & 3 \\ 1 & 2 \sin x \end{vmatrix} = 0 \Rightarrow 4 \sin^2 x - 3 = 0 \Rightarrow \sin x = \pm \frac{\sqrt{3}}{2} \Rightarrow x = \frac{\pi}{3}, \frac{2\pi}{3}$
 \therefore option (d)

(3) $\det(AABC) = 0 \Rightarrow \begin{vmatrix} 3 & -2 & 1 \\ k & 2 & 1 \\ 8 & 8 & 1 \end{vmatrix} = 0 \Rightarrow k = 5 \therefore$ option (b)

(4) here, $x+2 = -(2x-3) \Rightarrow x = \frac{1}{3} \therefore$ option (a)

(5) $y = \tan^{-1}(\sec x + \tan x) = \tan^{-1}\left(\frac{1+\sin x}{\cos x}\right) = \tan^{-1}\left(\frac{1+\cos\left(\frac{\pi}{2}-x\right)}{\sin\left(\frac{\pi}{2}-x\right)}\right)$
 $= \tan^{-1}\left(\frac{2\cos^2\left(\frac{\pi}{4}-\frac{x}{2}\right)}{2\sin\left(\frac{\pi}{4}-\frac{x}{2}\right)\cos\left(\frac{\pi}{4}-\frac{x}{2}\right)}\right)$
 $= \tan^{-1}\left(\cot\left(\frac{\pi}{4}-\frac{x}{2}\right)\right)$
 $= \tan^{-1}\left(\tan\left(\frac{\pi}{2}-\frac{\pi}{4}+\frac{x}{2}\right)\right)$
 $= \frac{\pi}{4} + \frac{x}{2} \therefore \frac{dy}{dx} = \frac{1}{2}$
 \therefore option (a)

(6) $k = \lim_{x \rightarrow 0} \frac{1 - \cos 4x}{8x^2} = \lim_{x \rightarrow 0} \frac{2 \sin^2 2x}{8x^2}$
 $= \lim_{2x \rightarrow 0} \left(\frac{\sin 2x}{2x}\right)^2 = 1^2 = 1 \therefore$ option (a)

(7) $I = \int \frac{x+3}{(x+4)^2} \cdot e^x dx = \int \frac{x+4-1}{(x+4)^2} \cdot e^x dx = \int \left[\frac{1}{x+4} - \frac{1}{(x+4)^2}\right] \cdot e^x dx$
 $= \frac{e^x}{x+4} + C \therefore$ option (a)

(8) $I = \int \frac{dx}{e^x + e^{-x}} = \int \frac{e^x}{e^{2x} + 1} dx$ put $e^x = t \therefore I = \int \frac{dt}{1+t^2} = \tan^{-1} t + C$
 $= \tan^{-1} e^x + C \therefore$ option (a)

(9) $A_{22} = \begin{vmatrix} 10 & 2 \\ 9 & 2 \end{vmatrix} = 2$; $A_{23} = -\begin{vmatrix} 10 & 19 \\ 9 & 24 \end{vmatrix} = -69$
 $\therefore A_{22} + A_{23} = 2 + (-69) = -67 \therefore$ option (c)

(10) $\frac{dy}{dx} + \frac{1}{x \log x} \cdot y = \frac{2}{x} \therefore$ I.F. $= e^{\int \frac{1}{x \log x} dx} = e^{\log(\log x)} = \log x$
 \therefore option (c)

(11) clearly $2+3=5$ \therefore option (d)

(12) $\vec{AB} = 2\hat{i} + (4-x)\hat{j} + 4\hat{k}$; $\vec{BC} = (y-3)\hat{i} - 6\hat{j} - 12\hat{k}$

here, $\frac{2}{y-3} = \frac{4-x}{-6} = \frac{4}{-12} \Rightarrow x=2, y=-3 \therefore$ option (a)

(13) $\vec{a} \cdot \vec{b} = -1 \Rightarrow |\vec{a}| \cdot |\vec{b}| \cdot \cos\theta = -1 \Rightarrow \cos\theta = -\frac{1}{2} \Rightarrow \theta = \cos^{-1}(-\frac{1}{2}) = \frac{2\pi}{3}$
 \therefore option (c)

(14) $A = \frac{1}{2} |\vec{d}_1 \times \vec{d}_2| = \frac{1}{2} \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 1 & -2 \\ 1 & -3 & 4 \end{vmatrix} = \frac{1}{2} |-2\hat{i} - 14\hat{j} - 10\hat{k}|$
 $= \frac{1}{2} \sqrt{(-2)^2 + (-14)^2 + (-10)^2} = \frac{\sqrt{300}}{2} = 5\sqrt{3}$
 \therefore option (b)

(15) $\cos^2 \frac{\pi}{3} + \cos^2 \frac{\pi}{4} + \cos^2 \gamma = 1 \Rightarrow \frac{1}{4} + \frac{1}{2} + \cos^2 \gamma = 1 \Rightarrow \cos \gamma = \frac{1}{2} \Rightarrow \gamma = \frac{\pi}{3}$
 \Rightarrow option (b)

(16) $P(W, G, G) = \frac{4}{16} \times \frac{7}{15} \times \frac{6}{14} = \frac{1}{20} \therefore$ option (a)

(17) $Z = 11x + 7y$
 $Z_{(10,3)} = 21$; $Z_{(9,5)} = 35$; $Z_{(3,2)} = 47 \therefore$ option (a)

(18) option (d)

(19) option (a)

(20) option (d)

Section-B

(21) $\vec{d}_1 = \vec{a} + \vec{b} = 3\hat{i} + 6\hat{j} - 2\hat{k} \therefore |\vec{d}_1| = \sqrt{49} = 7$
 $\vec{d}_2 = \vec{b} - \vec{a} = \hat{i} + 2\hat{j} - 8\hat{k} \therefore |\vec{d}_2| = \sqrt{69}$
 \therefore unit vectors along \vec{d}_1 & \vec{d}_2 are $\frac{1}{7}(3\hat{i} + 6\hat{j} - 2\hat{k})$ & $\frac{1}{\sqrt{69}}(\hat{i} + 2\hat{j} - 8\hat{k})$
OR

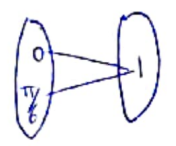
here, $|\vec{a}| = |\vec{b}| = 1$
also, $(\vec{a} + 3\vec{b}) \cdot (7\vec{a} - 5\vec{b}) = 0$
 $\Rightarrow 7|\vec{a}|^2 + 16(\vec{a} \cdot \vec{b}) - 15|\vec{b}|^2 = 0$
 $\Rightarrow 16 \cdot |\vec{a}| \cdot |\vec{b}| \cdot \cos\theta = 15 - 7 \Rightarrow \cos\theta = \frac{8}{16} = \frac{1}{2}$
 $\Rightarrow \theta = \frac{\pi}{3}$

(22) $\vec{AB} = \vec{OB} - \vec{OA} = (2\hat{i} - \hat{j} + 3\hat{k}) - (\hat{i} - \hat{j} + \hat{k}) = \hat{i} + 2\hat{k}$
 $\vec{CD} = \vec{OD} - \vec{OC} = (3\hat{i} - 2\hat{j} + \hat{k}) - (2\hat{i} - 3\hat{k}) = \hat{i} - 2\hat{j} + 4\hat{k}$
 Req. Projection = $\frac{\vec{AB} \cdot \vec{CD}}{|\vec{CD}|} = \frac{(1)(1) + 2(4)}{\sqrt{1+4+16}} = \frac{9}{\sqrt{21}}$ Ans

(23) Let $y = \sin\left(2 \tan^{-1} \sqrt{\frac{1-x}{1+x}}\right)$
 Put $x = \cos 2\theta \Rightarrow \theta = \frac{1}{2} \cos^{-1} x$
 $\therefore y = \sin\left(2 \tan^{-1} \sqrt{\frac{1-\cos 2\theta}{1+\cos 2\theta}}\right) = \sin\left(2 \tan^{-1}(\tan \theta)\right) = \sin(2\theta)$
 $= \sin(\cos^{-1} x)$
 $= \sin(\sin^{-1} \sqrt{1-x^2})$
 $= \sqrt{1-x^2}$ Ans

OR

$f: \mathbb{R} \rightarrow \mathbb{R}; f(x) = \sin^2 x + \cos^2 x$



\therefore not one-one ; Not onto as $R_f = \{1\} \neq \text{Co-domain}$
 $\Rightarrow f$ is not bijective

(24) $y = [\log(x + \sqrt{x^2+1})]^2$
 $\Rightarrow \frac{dy}{dx} = 2 \cdot \log(x + \sqrt{x^2+1}) \cdot x \left[1 + \frac{2x}{2\sqrt{x^2+1}}\right] \times \frac{1}{x + \sqrt{x^2+1}}$
 $= 2 \log(x + \sqrt{x^2+1}) \cdot \left(\frac{\sqrt{x^2+1} + x}{\sqrt{x^2+1}} \times \frac{1}{x + \sqrt{x^2+1}}\right)$
 $\Rightarrow \sqrt{1+x^2} \cdot \frac{dy}{dx} = 2 \log(x + \sqrt{x^2+1})$

diff. again,

$\sqrt{1+x^2} \cdot \frac{d^2y}{dx^2} + \frac{dy}{dx} \cdot \frac{1}{2\sqrt{1+x^2}} \cdot (2x) = 2x \cdot \frac{1}{x + \sqrt{x^2+1}} \times \left(1 + \frac{2x}{2\sqrt{x^2+1}}\right)$

$\Rightarrow (1+x^2) \cdot \frac{d^2y}{dx^2} + x \frac{dy}{dx} = 2$. Hence proved

(25) $\frac{dV}{dt} = 12 \text{ cm}^3/\text{s}; h = \frac{1}{6} r \Rightarrow r = 6h$



Now, $V = \frac{1}{3} \pi r^2 h = \frac{1}{3} \pi (6h)^2 \times h \Rightarrow V = 12\pi h^3$

$\Rightarrow \frac{dV}{dt} = 36\pi h^2 \frac{dh}{dt} \Rightarrow 12 = 36\pi h^2 \frac{dh}{dt}$

$\Rightarrow \left. \frac{dh}{dt} \right|_{h=4\text{cm}} = \frac{12}{36\pi(4)^2} = \frac{1}{48\pi} \text{ cm/s}$ Ans

Section-C

(26) $I = \int_0^{\pi} \frac{x \tan x}{\sec x + \tan x} dx$ — (1)

$= \int_0^{\pi} \frac{(\pi-x) \cdot \tan(\pi-x)}{\sec(\pi-x) + \tan(\pi-x)} dx$

$I = \int_0^{\pi} \frac{x + (\pi-x) \tan x}{x + (\sec x + \tan x)} dx$ — (2)

adding (1) + (2)

$2I = \pi \int_0^{\pi} \frac{\tan x}{\sec x + \tan x} \times \frac{\sec x - \tan x}{\sec x - \tan x} dx$

$\Rightarrow I = \frac{\pi}{2} \int_0^{\pi} \frac{\sec x \tan x - \tan^2 x}{1} dx$

$= \frac{\pi}{2} \int_0^{\pi} (\sec x \tan x - \sec^2 x + 1) dx$

$= \frac{\pi}{2} [\sec x - \tan x + x]_0^{\pi} = \frac{\pi}{2} (\pi - 2)$ Ans

OR

$I = \int_1^4 |x-1| + |x-2| + |x-3| dx$

$= \int_1^2 (-x+4) dx + \int_2^3 x dx + \int_3^4 (3x-6) dx$

$= \left[-\frac{x^2}{2} + 4x \right]_1^2 + \left[\frac{x^2}{2} \right]_2^3 + \left[\frac{3x^2}{2} - 6x \right]_3^4 = \frac{19}{2}$ Ans

(27) $I = \int \frac{3x+1}{(x-2)^2(x+2)} dx$

Let $\frac{3x+1}{(x-2)^2(x+2)} = \frac{A}{x+2} + \frac{B}{x-2} + \frac{C}{(x-2)^2}$

$\Rightarrow 3x+1 = A(x-2)^2 + B(x-2)(x+2) + C(x+2)$

$\Rightarrow 3x+1 = A(x^2-4x+4) + B(x^2-4) + C(x+2)$

Equating, $A+B=0$, $-8A+2C=6$; $8A+2C=1$

Solving, $A = -\frac{5}{16}$, $B = \frac{5}{16}$, $C = \frac{7}{4}$

$I = -\frac{5}{16} \int \frac{dx}{x+2} + \frac{5}{16} \int \frac{dx}{x-2} + \frac{7}{4} \int \frac{dx}{(x-2)^2}$

$= \frac{5}{16} \log \left| \frac{x-2}{x+2} \right| - \frac{7}{4(x-2)} + C$

28

$$I = \int \cos(\log x) \cdot dx$$

$$\text{Put } \log x = t \Rightarrow x = e^t \Rightarrow dx = e^t dt$$

$$I = \int \cos t \cdot e^t dt$$

$$= \cos t \cdot e^t - \int (-\sin t) \cdot e^t dt$$

$$= \cos t \cdot e^t + \int \sin t \cdot e^t dt$$

$$= \cos t \cdot e^t + \sin t \cdot e^t - \int \cos t \cdot e^t dt$$

$$= e^t (\cos t + \sin t) - I$$

$$\Rightarrow 2I = e^t (\cos t + \sin t) \Rightarrow I = \frac{1}{2} e^t (\cos t + \sin t) + C$$

$$= \frac{1}{2} x \cdot [\cos(\log x) + \sin(\log x)] + C \text{ Ans}$$

29

$$(\tan^{-1} y - x) \cdot dy = (1+y^2) \cdot dx$$

$$\Rightarrow \frac{dx}{dy} + \frac{1}{1+y^2} \cdot x = \frac{\tan^{-1} y}{1+y^2}$$

$$\text{I.F.} = e^{\int \frac{1}{1+y^2} dy} = e^{\tan^{-1} y}$$

$$\text{Solution is: } y \cdot e^{\tan^{-1} y} = \int \frac{\tan^{-1} y}{1+y^2} \cdot e^{\tan^{-1} y} dy$$

$$\text{for } I, \tan^{-1} y = t \therefore I = \int t \cdot e^t dt = (t-1) \cdot e^t + C$$

$$\Rightarrow y = \tan t \qquad \qquad \qquad = (\tan^{-1} y - 1) \cdot e^{\tan^{-1} y} + C$$

$$\therefore \text{soln is } y \cdot e^{\tan^{-1} y} = (\tan^{-1} y - 1) \cdot e^{\tan^{-1} y} + C$$

OR

clearly given DE is homogeneous.

$$\frac{dy}{dx} - \frac{y}{x} + \sin\left(\frac{y}{x}\right) = 0$$

$$\text{Put } \frac{y}{x} = v \text{ i.e. } y = vx \Rightarrow \frac{dy}{dx} = v + x \frac{dv}{dx}$$

$$\text{Given DE becomes, } v + x \frac{dv}{dx} = v - \sin v$$

$$\Rightarrow \int \operatorname{cosec} v \, dv = -\int \frac{dx}{x}$$

$$\Rightarrow \log \left| \operatorname{cosec} \frac{y}{x} - \cot \frac{y}{x} \right| = -\log x + \log C$$

$$\Rightarrow \operatorname{cosec} \frac{y}{x} - \cot \frac{y}{x} = \frac{C}{x}$$

$$\text{when } x=2, y=\pi \Rightarrow C=2$$

$$\therefore \text{Req. solution is } \operatorname{cosec} \frac{y}{x} - \cot \frac{y}{x} = \frac{2}{x} \text{ Ans}$$

(30) $P(A) = \frac{1}{2}$, $P(B) = \frac{1}{2}$; $P(\bar{A}) = \frac{1}{2}$, $P(\bar{B}) = \frac{1}{2}$

Prob. of winning by A = $P(A) + P(\bar{A}\bar{B}A) + P(\bar{A}\bar{B}\bar{A}\bar{B}A) + \dots \infty$
 $= \frac{1}{2} + (\frac{1}{2})^2 \cdot \frac{1}{2} + (\frac{1}{2})^4 \cdot \frac{1}{2} + \dots$
 $= \frac{\frac{1}{2}}{1 - \frac{1}{4}} = \frac{2}{3}$ ($\because a + ar + ar^2 + \dots \infty = \frac{a}{1-r}$)

$P(B) = 1 - \frac{2}{3} = \frac{1}{3}$

OR

Total people = 50

E: People believe in non-violence ; F: People believe in violence

$P(E) = \frac{20}{50}$, $P(\bar{E}) = \frac{30}{50}$

X: No. of non-violent person ; $x = 0, 1, 2$

$P(x=0) = \frac{30}{50} \times \frac{29}{49}$

$P(x=1) = 2 \times \frac{30}{50} \times \frac{20}{49}$

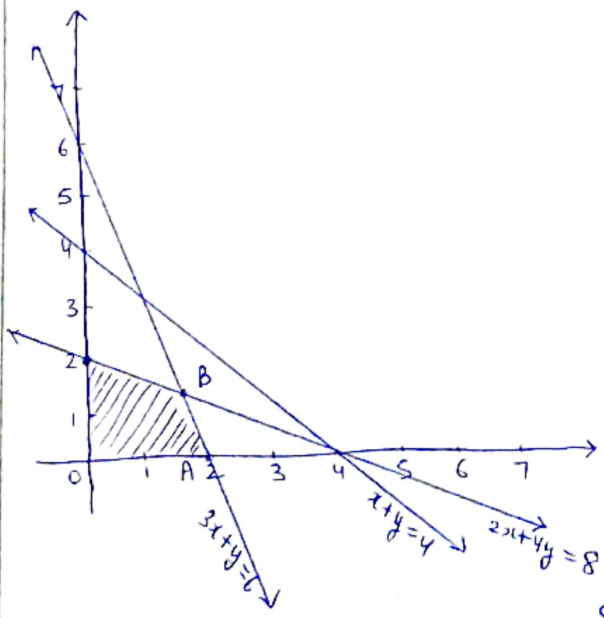
$P(x=2) = \frac{20}{50} \times \frac{19}{49}$

P.D. table

X	0	1	2
P(X)	$\frac{30}{50} \times \frac{29}{49}$	$2 \times \frac{30}{50} \times \frac{20}{49}$	$\frac{20}{50} \times \frac{19}{49}$

$E(X) = \frac{196}{245}$

(31)



Point	$Z = 2x + 5y$
(0, 0)	0
(2, 0)	4
(0, 2)	10 \rightarrow max
$(\frac{8}{5}, \frac{6}{5})$	$\frac{46}{5}$

$\therefore Z$ is max. at (0, 2).

Max. value = 10

Section - D

(32) $|A| = 1200 \neq 0 \Rightarrow A^{-1}$ exists

$A^{-1} = \frac{1}{|A|} \cdot \text{adj}A = \frac{1}{1200} \begin{pmatrix} 75 & 150 & 75 \\ 110 & -100 & 30 \\ 72 & 0 & -24 \end{pmatrix}$

$AX = B \Rightarrow X = A^{-1} \cdot B = \frac{1}{1200} \begin{pmatrix} 75 & 150 & 75 \\ 110 & -100 & 30 \\ 72 & 0 & -24 \end{pmatrix} \begin{pmatrix} 2 \\ 5 \\ -4 \end{pmatrix} = \begin{pmatrix} \frac{1}{2} \\ -\frac{1}{3} \\ \frac{1}{5} \end{pmatrix} = \begin{pmatrix} x \\ y \\ z \end{pmatrix}$

$\therefore x = 2, y = -3, z = 5$ Ans

OR

$$AB = 4I \Rightarrow B^{-1} = \frac{1}{4} \cdot A$$

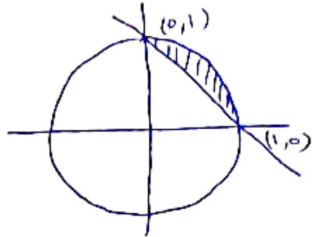
Given system $BX = C \Rightarrow X = B^{-1}C = \frac{1}{4} A \cdot C$

$$= \frac{1}{4} \begin{bmatrix} -5 & 1 & 3 \\ 7 & -1 & -5 \\ 1 & -1 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 7 \\ 2 \end{bmatrix}$$

$$= \frac{1}{4} \begin{bmatrix} 8 \\ 4 \\ -4 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ -1 \end{bmatrix}$$

$\therefore x=2, y=1, z=-1$ Ans.

(33) $A = \int (x,y) : x^2 + y^2 \leq 1 \leq x+y$
 Consider, $x^2 + y^2 = 1$ and $x+y=1$



$$A = \int_0^1 (y \text{ of circle}) dx - \int_0^1 (y \text{ of line}) dx$$

$$= \int_0^1 \sqrt{1-x^2} dx - \int_0^1 (1-x) dx$$

$$= \left[\frac{x}{2} \sqrt{1-x^2} + \frac{1}{2} \sin^{-1} x - x + \frac{x^2}{2} \right]_0^1 = \left(\frac{\pi}{4} - \frac{1}{2} \right) \text{ sq. units.}$$

(34) $f(x) = 5x^2 + 6x - 9$

for one-one Let $x_1, x_2 \in R_+$
 let $f(x_1) = f(x_2)$

$$\Rightarrow 5x_1^2 + 6x_1 - 9 = 5x_2^2 + 6x_2 - 9$$

$$\Rightarrow (x_1 - x_2)(5x_1 + 5x_2 + 6) = 0$$

$$\Rightarrow x_1 = x_2 \Rightarrow f \text{ is one-one}$$

for onto: $y = 5x^2 + 6x - 9$

$$\Rightarrow 5x^2 + 6x - 9 - y = 0 \Rightarrow x = \frac{-6 \pm \sqrt{36 + 4 \times 5(9+y)}}{10} > 0$$

$$\Rightarrow -6 \pm \sqrt{216 + 20y} > 0$$

$$\Rightarrow 216 + 20y > 36 \Rightarrow y \in (-9, \infty) = \text{Co-domain}$$

$\therefore f$ is onto

$\Rightarrow f$ is bijective fn.

OR

$R = \{(a,b) : a,b \in A ; |a-b| \text{ is div. by } 4\}$

for reflexive: $|a-a|$ i.e. 0, is div. by 4 $\Rightarrow (a,a) \in R \Rightarrow R$ is reflexive.

for symmetric: Let $(a,b) \in R \Rightarrow |a-b|$ is div. by 4
 $\Rightarrow |b-a|$ is div. by 4 $\Rightarrow (b,a) \in R \Rightarrow R$ is symm.

for transitive: Let $(a,b), (b,c) \in R$

$$\Rightarrow |a-b| \text{ is div. by } 4 \text{ and } |b-c| \text{ is div. by } 4$$

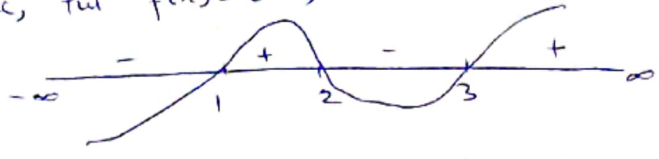
$$\Rightarrow a-b = \pm 4\lambda \text{ and } b-c = \pm 4\mu$$

$$\Rightarrow a-c = \pm 4(\lambda + \mu) = \pm 4\lambda' \Rightarrow |a-c| \text{ is div. by } 4 \Rightarrow (a,c) \in R \Rightarrow R \text{ is transitive}$$

$\therefore R$ is equivalence Relation.

Now; $[1] = \{1, 5, 9\}$ and $[2] = \{2, 10\}$

(35) $f(x) = x^4 - 8x^3 + 22x^2 - 24x + 21$
 $f'(x) = 4x^3 - 24x^2 + 44x - 24 = 4(x^3 - 6x^2 + 11x - 6) = 4(x-1)(x-2)(x-3)$
 for inc/dec, put $f'(x) = 0 \Rightarrow x = 1, 2, 3$



- (a) f is inc when $x \in [1, 2] \cup [3, \infty)$
- (b) f is dec. when $x \in (-\infty, 1] \cup [2, 3]$

Section-E

(36) E_1 : farmer is selected from village A
 E_2 : " " " " " B
 E_3 : " " " " " C
 A: farmer selected believes in technology

$P(E_1) = P(E_2) = P(E_3) = \frac{1}{3}$
 $P(A|E_1) = \frac{60}{100}$, $P(A|E_2) = \frac{70}{100}$, $P(A|E_3) = \frac{80}{100}$

(i) $P(A|E_1) = \frac{60}{100}$

(ii) $P(A) = P(E_1) \cdot P(A|E_1) + P(E_2) \cdot P(A|E_2) + P(E_3) \cdot P(A|E_3)$
 $= \frac{1}{3} \times \frac{60}{100} + \frac{1}{3} \times \frac{70}{100} + \frac{1}{3} \times \frac{80}{100} = \frac{210}{300} = \frac{7}{10}$

(iii) $P(E_2|A) = \frac{P(E_2) \cdot P(A|E_2)}{P(A)}$
 $= \frac{\frac{1}{3} \times \frac{70}{100}}{\frac{210}{300}} = \frac{1}{3}$

(37) (i) $2y + x + \pi(\frac{x}{2}) = 10 \Rightarrow y = \frac{1}{4}(20 - \pi x - 2x)$

(ii) $A = xy + \frac{1}{2}\pi(\frac{x}{2})^2 = \frac{1}{4}x(20 - \pi x - 2x) + \frac{1}{8}\pi x^2$

$\Rightarrow \frac{dA}{dx} = \frac{20 - 2\pi x - 4x}{4} + \frac{1}{4}\pi x = 0 \Rightarrow x = \frac{20}{4 + \pi}$; $\frac{d^2A}{dx^2} < 0$ here.

OR

(ii) $A = \frac{x}{4}(20 - \pi x - 2x) + \frac{\pi x^2}{8} = \frac{50}{\pi + 4}$ Sq. units

(38) $\vec{a}_2 - \vec{a}_1 = 3\hat{i} + 3\hat{j}$; $\vec{b}_1 \times \vec{b}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & -1 \\ 2 & 1 & 1 \end{vmatrix} = 3\hat{i} - 3\hat{j} - 3\hat{k}$ $\therefore |\vec{b}_1 \times \vec{b}_2| = 3\sqrt{3}$

$\therefore SD = \frac{3(3) + 3(-3) + 0}{3\sqrt{3}} = 0$

(i) line 1: $\frac{x}{1} = \frac{y}{2} = \frac{z}{-1} = \lambda \Rightarrow$ Any point $(\lambda, 2\lambda, -\lambda)$

line 2: $\frac{x-3}{2} = \frac{y-3}{1} = \frac{z}{1} = \mu \Rightarrow$ Any point $(2\mu+3, \mu+3, \mu)$

Pt. of collision, $\lambda \neq 2\mu+3$; $2\lambda = \mu+3$; $-\lambda = \mu \Rightarrow \lambda = 1, \mu = -1$

Req. Point is $(1, 2, -1)$