

## (General Instructions)

- Please check that this question paper contains <u>6</u> printed pages.
- Please check that this question paper contains \_\_38\_\_\_ questions.
- Please write down the serial number of the question before attempting it.
- Reading time of 15 minutes is given to read the question paper alone. No writing during this time.
- This Question paper contains five sections A, B, C, D and E. Each section is compulsory. However, there are internal choices in some questions.
- Section A has 18 MCQ's and 02 Assertion-Reason based questions of 1 mark each.
- Section B has 5 Very Short Answer (VSA)-type questions of 2 marks each.
- Section C has 6 Short Answer (SA)-type questions of 3 marks each.
- Section D has 4 Long Answer (LA)-type questions of 5 marks each.
- Section E has 3 source based/case based/passage based/integrated units of assessment of 4 marks each with sub-parts.

# COMMON EXAMINATION Class-12 (MATHEMATICS – 041)

Roll No.: Date: DD/MM/YYYY

### set - 2

Maximum Marks:80 Time allowed: 3 hours

Section –A (Each question carries 1 mark) (Multiple Choice Questions)

- 1. If  $\begin{bmatrix} 2x + y & 4x \\ 5x 7 & 4x \end{bmatrix} = \begin{bmatrix} 7 & 7y 13 \\ y & x + 6 \end{bmatrix}$ , then the value of x + y is: (a) 7 (b) 4 (c) 5 (d) 2  $\begin{vmatrix} 1 & 2 & 4 \end{vmatrix}$
- 2. The sum of cofactors of 7 and 10 in the determinant  $\begin{vmatrix} 1 & 2 & 4 \\ 5 & 7 & 8 \\ 9 & 10 & 12 \end{vmatrix}$  is:
  - (a) -27 (b) -12 (c) -18 (d) 0
- 3. If  $A = \begin{bmatrix} 1 & k & 3 \\ 3 & k & -2 \\ 2 & 3 & -4 \end{bmatrix}$  is singular matrix, then k = ?

(a) 
$$16/3$$
 (b)  $34/5$  (c)  $33/2$  (d)  $33/3$ 

4. If A is a square matrix of order 3 and |A| = 15, then |adj A| = ?

5. If |A| = 3 and  $A^{-1} = \begin{bmatrix} 3 & -1 \\ -5/3 & 2/3 \end{bmatrix}$ , then adj A = ?(a)  $\begin{bmatrix} 9 & 3 \\ -5 & -2 \end{bmatrix}$  (b)  $\begin{bmatrix} 9 & -3 \\ -5 & 2 \end{bmatrix}$  (c)  $\begin{bmatrix} -9 & -3 \\ 5 & 2 \end{bmatrix}$  (d)  $\begin{bmatrix} 9 & -3 \\ 5 & -2 \end{bmatrix}$ 

6. If 
$$\sqrt{x} + \sqrt{y} = \sqrt{a}$$
, then  $\frac{dy}{dx}$  is:  
(a)  $-\sqrt{\frac{x}{y}}$  (b)  $-\frac{1}{2}\sqrt{\frac{x}{y}}$  (c)  $-\sqrt{\frac{y}{x}}$  (d)  $-2\sqrt{\frac{x}{y}}$ 



7. The function  $f(x) = \begin{cases} 1+x \text{, when } x \leq 2\\ 5-x \text{, when } x > 2 \end{cases}$  is :

(a) continuous as well as differentiable at x = 2
(b) continuous but not differentiable at x = 2
(c) differentiable but not continuous at x = 2
(d) neither continuous nor differentiable at x = 2

- 8. The minimum value of  $(x^2 + \frac{250}{x})$  is: (a) 5 (b) 25 (c) 50 (d) 75
- 9. If m and n are the order and degree of the differential equation  $3x \left(\frac{dy}{dx}\right)^3 - \frac{d^2y}{dx^2} - 8y = \sin y$  respectively then, write the value of m + n.
  - (a) 1 (b) 2 (c) 3 (d) 4

10. The general solution of the differential equation  $x \frac{dy}{dx} = y + x \tan(\frac{y}{x})$  is:

(a) C x = 
$$\sin\left(\frac{y}{x}\right)$$
 (b)  $\sin\left(\frac{y}{x}\right) = C$  (c)  $\sin\left(\frac{y}{x}\right) = Cy$  (d)  $\sin\left(\frac{x}{y}\right) = C$ 

- 11. The projection of the vector  $2\hat{i} + 3\hat{j} + 2\hat{k}$  on the vector  $\hat{i} + 2\hat{j} + \hat{k}$  is:
  - (a)  $10/\sqrt{6}$  (b) 10/3 (c)  $5/\sqrt{6}$  (d)  $10/\sqrt{3}$
- 12. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are the unit vectors and  $\vec{a} + \vec{b} + \vec{c} = \vec{0}$ . Evaluate the quantity  $\mu = \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{a} \cdot \vec{c} = ?$ 
  - (a)  $\frac{1}{2}$  (b)  $\frac{1}{2}$  (c)  $\frac{3}{2}$  (d)  $-\frac{3}{2}$
- 13. Two adjacent sides of a parallelogram are represented by the vectors  $\vec{a} = 3\hat{i} + \hat{j} + 4\hat{k}$  and  $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ , then the area of parallelogram is :
  - (a)  $\sqrt{42}$  sq. units(b) 6 sq. units(c)  $\sqrt{35}$  sq. units(d)  $\sqrt{52}$  sq. units

14. The cartesian equation of the line joining the points (3, -2, -5) and (3, -2, 6) is :

(a)  $\frac{x+3}{0} = \frac{y-2}{0} = \frac{z+5}{11}$ (b)  $\frac{x-3}{0} = \frac{y+2}{0} = \frac{z+5}{11}$ (c)  $\frac{x+3}{0} = \frac{y+2}{0} = \frac{z-5}{11}$ (d)  $\frac{x-3}{0} = \frac{y+2}{0} = \frac{z+5}{-11}$ 

15. If  $(\hat{\iota} + 3\hat{\jmath} + 8\hat{k}) X (3\hat{\iota} - k\hat{\jmath} + m\hat{k}) = \vec{0}$ , then k and m are :

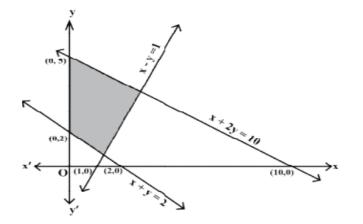
(a) 
$$m=24$$
,  $k=-9$  (b)  $m=-24$ ,  $k=-9$  (c)  $m=-9$ ,  $k=18$  (d) $m=27$ ,  $n=-9$ 

**16.** The optimal value of the objective function is attained at the points:

- (a) on X- axis (b) corner points of the feasible region
- (c) on Y axis (d) in the first quadrant



17. The feasible region corresponding to the linear constraints of a linear programming problem is given below:



Which of the following is not a constraint to the given Linear Programming Problem?(a)  $x + y \ge 2$ (b)  $x + 2y \le 10$ (c)  $x - y \ge 1$ (d)  $x - y \le 1$ 

18. If A and B are two independent events with P(A) = 3/5 and P(B) = 4/9, then find  $P(\overline{A} \cap \overline{B})$ (a) 1/9 (b) 2/9 (c) 1/3 (d) 4/9

#### ASSERTION-REASON BASED QUESTIONS

In the following questions, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct answer out of the following choices.

19.Assertion (A):  $\sin^{-1}(\sin(2\pi/3)) = 2\pi/3$ .

Reasoning(R):  $\sin^{-1}(\sin \theta) = \theta$ , if  $\theta \in [-\pi/2, \pi/2]$ 

- (a) Both (A) and (R) are true and (R) is the correct explanation of (A).
- (b) Both (A) and (R) are true but (R) is not the correct explanation of (A).
- (c) (A) is true but (R) is false.
- (d) (A) is false but (R) is true.
- 20. Assertion(A): If  $\int_0^1 (3x^2 + 2x + k) dx = 0$ , then the value if k is 2

Reasoning(R):  $\int_a^b x^n dx = \left[\frac{x^{n+1}}{n+1}\right] + c$ 

- (a) Both (A) and (R) are true and (R) is the correct explanation of (A).
- (b) Both (A) and (R) are true but (R) is not the correct explanation of (A).
- (c) (A) is true but (R) is false.
- (d) (A) is false but (R) is true.

#### Section –B

(This section comprises of very short answer type questions (VSA) of 2 marks each)

21. Let set A = { 1, 2, 3, 4} and relation R = {(1,1), (2,2), (3,3),(4,4), (1,2), (1,3), (3,2)}. Show that R is reflexive and transitive.



22. The volume of cube is increasing at the rate of 7 cm<sup>3</sup>/sec. How fast is its surface area increasing at the instant when the length of an edge of the cube is 12 cm?

OR

Water is leaking from a conical funnel at the rate of  $5 \text{ cm}^3/\text{sec.}$  If the radius of the base of the funnel is 5 cm and its altitude is 10 cm. Find the rate at which the water level is dropping when it is 2.5 cm from the top.

- 23. Find the maximum profit that a company can make, if the profit function is given by  $P(x) = 41 + 24x 18x^2$ .
- 24. Evaluate:  $\int_{0}^{\frac{\pi}{2}} \sqrt{1 + \cos 2x} \, \mathrm{dx}.$

OR

Evaluate :  $\int_1^{\sqrt{2}} \frac{dx}{x\sqrt{x^2-1}}$ .

25. Using integration, find the area of the region bounded by the line 2y + x = 8, the x-axis and the lines x = 2 and x = 4.

#### Section – C

(This section comprises of short answer type questions (SA) of 3 marks each)

26. If 
$$y = (x)^{\cos x} + (\cos x)^{\sin x}$$
, find  $\frac{dy}{dx}$ .

27. Evaluate:  $\int \left[\frac{1}{\log x} - \frac{1}{(\log x)^2}\right] dx$ 

- 28. Evaluate:  $\int \frac{\cos x}{\sin^2 x + 4\sin x + 5} \, \mathrm{d}x.$
- 29. Find the particular solution of the differential equation  $\frac{dy}{dx} 3y \cot x = \sin 2x$ , given that y = 2 when  $x = \frac{\pi}{2}$ . OR

Find the general equation of the differential equation  $(x - 1) \frac{dy}{dx} = 2 x^3 y$ .

**30.** Solve the linear programming problem graphically:

Maximise Z = 60 x + 40 y

Subject to constraints:  $5x + 6y \le 45$ ;  $3x + 2y \le 18$ ;  $x \ge 0$ ,  $y \ge 0$ .

31. Three critics review a book. For the three critics, the odds in favour of the book are (5:2), (4:3) and (3:4) respectively. Find the probability that the majority is in favour of the books.

OR

There are 5 bags, each containing 5 white balls and 3 black balls. Also,

there are 6 bags, each containing 2 white balls and 4 black balls. A white ball is drawn at random. Find the probability that this white ball is from a bag of first group.



### Section –D

[This section comprises of long answer type questions (LA) of 5 marks each]

32. Show that the relation R on N x N, defined by (a,b) R (c, d) ⇔ a + d= b + c is an equivalence relation ( where N is the set of natural numbers). OR

Show that the function f: N  $\rightarrow$  N, defined by f(n) =  $\begin{cases} \frac{n+1}{2} & \text{, if } n \text{ is odd} \\ \frac{n}{2} & \text{, if } n \text{ is even} \end{cases}$  is not one-one

but onto.

- 33. Given A =  $\begin{bmatrix} 1 & -1 & 1 \\ 1 & -2 & -2 \\ 2 & 1 & 3 \end{bmatrix}$  and B =  $\begin{bmatrix} -4 & 4 & 4 \\ -7 & 1 & 3 \\ 5 & -3 & -1 \end{bmatrix}$ , find AB and use this result in solving the following system of equations: x - y + z = 4; x - 2y - 2z = 9; 2x = y = 3z = 1.
- 34. Using integration, find the area of the region bounded by the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , where a > b.
- **35.** Show that the lines  $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$  and  $\frac{x-4}{5} = \frac{y-1}{2} = z$  intersect each other. Also find the point of intersection.

OR

Find the shortest distance between the following pair of lines:  

$$\frac{x-5}{4} = \frac{y-7}{-5} = \frac{z+3}{-5}$$
 and  $\frac{x-8}{7} = \frac{y-7}{1} = \frac{z-5}{3}$ .

### Section –E

[This section comprises of 3 case- study/passage-based questions of 4 marks each with sub parts. The first two case study questions have three sub parts (i), (ii), (iii) of marks 1,1,2 respectively].

**36.** Read the following passage and Answer the questions based of the information given below:

Scientist want to know the Oil- Reserves in sea so they travel over the sea along the curve  $f(x) = (x+1)^3 (x-3)^3$  by an helicopter. A student of class XII discuss the characteristic of the curve:

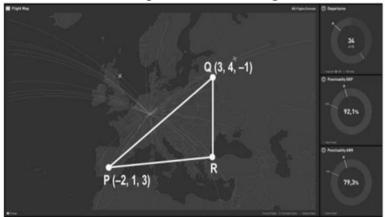


- (i) Find the first order derivative of the given function.
- (ii) **Find the critical point of the given function.**
- (iii) Find the intervals in which the function is strictly increasing. OR
- (iv) Find the intervals in which the function is decreasing.



**37.** Answer the questions based on the given information.

The flight path of two airplanes in a flight simulator game are shown below. The coordinates of the airports P and Q are given.



Airplane 1 flies directly from P to Q.

Airplane 2 has a layover at R and then flies to Q.

The path of Airplane 2 from P to R can be represented by the vector  $5\hat{\imath}+\hat{\jmath}-2\hat{k}$ . (Note: Assume that the flight path is straight and fuel is consumed uniformly throughout the flight.)

- (i) Find the vector that represents the flight path of Airplane 1.
- (ii) Write the vector representing the path of Airplane 2 from R to Q. Show your steps.
- (iii) What is the angle between the flight paths of Airplane 1 and Airplane 2 just after take-off ?

### OR

- (iv) Consider that Airplane 1 started the flight with a full fuel tank.Find the position vector of the point where a third of the fuel runs out if the entire fuel is required for the flight.
- 38. In a play zone, Aastha is playing crane game. It has 12 blue balls, 8 red balls, 10 yellow balls and 5 green balls. If Aastha draws two balls one after the other without replacement, then answer the following questions.



- (i) What is the probability that the first ball is blue and the second ball is green?
- (ii) What is the probability that both the balls are red?
- (iii) What is the probability that both the balls are not blue? OR
- (iv) What is the probability that the first ball is green and the second ball is not yellow?