

CHAPTER-10
VECTORS
01 MARK TYPE QUESTIONS

Q. NO	QUESTION	MARK
1.	If points A ($60\hat{i} + 3\hat{j}$), ($40\hat{i} - 8\hat{j}$) and C ($a\hat{i} - 52\hat{j}$) are collinear, then 'a' is equal to a) 40 b) -40 c) 20 d) -20	1
2.	The value of $\hat{i} \cdot (\hat{j} \times \hat{k}) + \hat{j} \cdot (\hat{i} \times \hat{k}) + \hat{k} \cdot (\hat{i} \times \hat{j})$ is a) 0 b) -1 c) 1 d) 3	1
3.	If $ \vec{a} = 2$, $ \vec{b} = 5$ and $ \vec{a} \times \vec{b} = 8$, find $\vec{a} \cdot \vec{b}$ a) 6 b) 1 c) 7 d) 0	1
4.	Find the area of the Δ whose adjacent sides are represented by the vectors $\vec{a} = 3\hat{i} + \hat{j} - 2\hat{k}$, $\vec{b} = \hat{i} - 3\hat{j} + 4\hat{k}$ a) 10 b) $10\sqrt{3}$ c) 8 d) 12	1
5.	\vec{a} is a unit vector and $(\vec{x} - \vec{a})(\vec{x} + \vec{a}) = 8$, then find $ \vec{x} $ a) 2 b) 5 c) 3 d) 1	1
6.	If $ \vec{a} \times \vec{b} = 4$, $ \vec{a} \cdot \vec{b} = 2$, then $ \vec{a} $ 2 $ \vec{b} $ 2 is a) 6 b) 2 c) 20 d) 8	1
7.	If $ \vec{a} = 2$, $ \vec{b} = 7$ and $\vec{a} \times \vec{b} = 3\hat{i} + 2\hat{j} + 6\hat{k}$, find the angle between \vec{a} and \vec{b} a) $\pi/6$ b) π c) 0 d) none	1
8.	Find a vector of magnitude $3\sqrt{2}$ units which makes an angle of $\pi/4$, $\pi/2$ with y and z-axes, respectively. a) $\pm 3\hat{i} + 3\hat{j}$ b) $3\hat{i} - 3\hat{j}$ c) $\pm 5\hat{i} + 3\hat{j}$ d) none	1
9.	If points A ($60\hat{i} + 3\hat{j}$), ($40\hat{i} - 8\hat{j}$) and C ($a\hat{i} - 52\hat{j}$) are collinear, then 'a' is equal to a) 40 b) -40 c) 20 d) -20	1
10.	If $\vec{a} = 2\hat{i} + 2\hat{j} + 3\hat{k}$, $\vec{b} = -\hat{i} + 2\hat{j} + \hat{k}$, $\vec{c} = 3\hat{i} + \hat{j}$ are such that $\vec{a} + \lambda \vec{b}$ is perpendicular to \vec{c} , then find the value of λ . a) 9 b) 8 c) 5 d) 1	1
11.	Let $\vec{a} = 2\hat{i} + 3\hat{j} + c\hat{k}$. The value of c if $ \vec{a} = 5$ is (a) 0 (b) $2\sqrt{3}$ (c) 1 (d) 12	1
12.	If $\vec{a} = (2\hat{i} - 4\hat{j} + 5\hat{k})$ then the value of h so that $h\vec{a}$ may be unit vector is (a) $\frac{1}{5}$ (b) $\frac{1}{\sqrt{3}}$ (c) $\frac{1}{3\sqrt{5}}$ (d) $\frac{1}{5\sqrt{3}}$	1
13.	If $\vec{AB} = (2\hat{i} + \hat{j} - 3\hat{k})$ and A(1,2,-1) is the given point, then the coordinates of B are (a) (3,-3,4) (b) (3,3,4) (c) (-3,-3,-4) (d) (3,3,-4)	1
14.	If $ \vec{a} \times \vec{b} = 4$, $\vec{a} \cdot \vec{b} = 2$, then $ \vec{a} ^2 \vec{b} ^2 =$ (a) 6 (b) 20 (c) 8 (d) 2	1
15.	If \vec{a} is any vector, then $\vec{a} \cdot \vec{a}$ is (a) 0 (b) $\neq 0$ (c) $\vec{0}$ (d) $ \vec{a} ^2$	1
16.	If \vec{a} and \vec{b} are two vectors of magnitude 3 and $\frac{2}{3}$ respectively such that $\vec{a} \times \vec{b}$ is a unit vector, then the angle between \vec{a} and \vec{b} is (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{4}$ (c) $\frac{\pi}{6}$ (d) $\frac{\pi}{8}$	1
17.	A vector of magnitude 9 units in the direction of the vector $(-2\hat{i} + \hat{j} + 2\hat{k})$ is	1

	(a)(-3 \hat{i} +6 \hat{j} +6 \hat{k}) (b)(-6 \hat{i} +3 \hat{j} +3 \hat{k}) (c)(-6 \hat{i} +3 \hat{j} +6 \hat{k}) (d)(6 \hat{i} +6 \hat{j} -3 \hat{k})	
18.	The value of $\hat{i} \cdot (\hat{j} \times \hat{k}) + \hat{j} \cdot (\hat{i} \times \hat{k}) + \hat{k} \cdot (\hat{i} \times \hat{j})$ is (a)-1 (b) 1 (c) -2 (d) 2	1
19.	If $ \vec{a} \times \vec{b} ^2 + \vec{a} \cdot \vec{b} ^2 = 144$ and $ \vec{a} = 4$, then $ \vec{b} $ is equal to (a)1 (b)2 (c)3 (d)4	1
20.	If \vec{a} and \vec{b} are two collinear vectors, then which of the following is incorrect? (a) $\vec{b} = h\vec{a}$, for som scalar h (b) $\vec{a} = \pm \vec{b}$ (c) the respective components of \vec{a} and \vec{b} are proportional (d) both the vector \vec{a} and \vec{b} have same direction, but different magnitudes.	1
21.	The vector in the direction of the vector $\vec{a} = \hat{i} - 2\hat{j} + 2\hat{k}$ that has a magnitude 9 is: (a) $\hat{i} - 2\hat{j} + 2\hat{k}$ (b) $\frac{1}{3}(\hat{i} - 2\hat{j} + 2\hat{k})$ (c) $3(\hat{i} - 2\hat{j} + 2\hat{k})$ (d) $9\hat{i} - 2\hat{j} + 2\hat{k}$	1
22.	The position vectors of the points A, B, C are $2\hat{i} + \hat{j} - \hat{k}$, $3\hat{i} - 2\hat{j} + \hat{k}$ and $\hat{i} + 4\hat{j} - 3\hat{k}$ respectively. These points : (a) form an isosceles triangle (b) form a right triangle (c) are collinear (d) form a scalene triangle	1
23.	The projection of the vector $\vec{a} = 2\hat{i} - \hat{j} + \hat{k}$ on $\vec{b} = \hat{i} - 2\hat{j} + \hat{k}$ is: (a) $\frac{\sqrt{5}}{2}$ (b) $\frac{5}{\sqrt{2}}$ (c) $\frac{\sqrt{5}}{6}$ (d) $\frac{\sqrt{6}}{5}$	1
24.	If θ is the angle between any two vectors \vec{a} and \vec{b} , then $ \vec{a} \times \vec{b} = \vec{a} \cdot \vec{b} $ when θ is: (a) $\frac{\pi}{3}$ (b) $\frac{\pi}{4}$ (c) $\frac{2\pi}{3}$ (d) none of these	1
25.	If $\hat{a}, \hat{b}, \hat{c}$ are mutually perpendicular unit vectors, then value of $ \hat{a} + \hat{b} + \hat{c} $ is: (a) 1 (b) $\sqrt{2}$ (c) $\sqrt{3}$ (d) 2	1
26.	The vector $\vec{b} = 3\hat{i} + 4\hat{k}$ is to be written as the sum of a vector α parallel to $\vec{a} = \hat{i} + \hat{j}$ and a vector $\vec{\beta}$ perpendicular to \vec{a} . Then \vec{a} is: (a) $\frac{3}{2}(\hat{i} + \hat{j})$ (b) $\frac{2}{3}(\hat{i} + \hat{j})$ (c) $\frac{1}{2}(\hat{i} + \hat{j})$ (d) $\frac{1}{3}(\hat{i} + \hat{j})$	1
27.	If the position vectors of P and Q are $\hat{i} + 3\hat{j} - 7\hat{k}$ and $5\hat{i} - 2\hat{j} + 4\hat{k}$ then cosine of the angle between \vec{PQ} and y-axis is: (a) $\frac{5}{\sqrt{162}}$ (b) $\frac{4}{\sqrt{162}}$ (c) $\frac{11}{\sqrt{162}}$ (d) $-\frac{5}{\sqrt{162}}$	1
28.	\vec{a} and \vec{b} are two unit vectors and θ is the angle between them then $\cos \frac{\theta}{2} =$ (a) $\frac{1}{2} \vec{a} + \vec{b} $ (b) $ \vec{a} + \vec{b} $ (c) $ \vec{a} - \vec{b} $ (d) $\frac{1}{2} \vec{a} - \vec{b} $	1
29.	\vec{a}, \vec{b} , and \vec{c} are three unit vectors such that $\vec{a} + \vec{b} + \vec{c} = \vec{0}$, then $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} =$ 3 (b) $-\frac{3}{2}$ (c) $\frac{3}{2}$ (d) 3	1
30.	In the following questions, a statement of assertion followed by a statement of reason is given. Choose the correct answer out of the following choice as follows: a) Assertion and reason both are correct statements and reason is correct explanation for assertion. b) Assertion and reason both are correct statements but reason is not correct explanation for assertion. c) Assertion is correct statement but reason is wrong statement. d) Assertion is wrong statement but reason is correct statement.	1

	<p>Assertion(A): The area of parallelogram with diagonals \vec{a} and \vec{b} is $\vec{a} \times \vec{b}$.</p> <p>Reason(R): If \vec{a} and \vec{b} represent the adjacent sides of a triangle, then the area of a triangle, then the area of triangle can be obtained by evaluating $\vec{a} \times \vec{b}$.</p>	
31.	Classify the following as scalar and vectors: (i) 20 kg weight (ii) $50m/s^2$.	1
32.	Find the position vector of the point which divides the join of the points $2\vec{a} - 3\vec{b}$ and $3\vec{a} - 2\vec{b}$ internally.	1
33.	Let $\vec{a} = \hat{i} + 2\hat{j}$ and $\vec{b} = 2\hat{i} + \hat{j}$. Is $ \vec{a} = \vec{b} $? Are the vectors equal?	1
34.	Find the projection of the vector $7\hat{i} + \hat{j} - 4\hat{k}$ on $2\hat{i} + 6\hat{j} + 3\hat{k}$.	1
35.	Find the value of p for which the vectors $\vec{a} = 3\hat{i} + 2\hat{j} + 9\hat{k}$ and $\vec{b} = \hat{i} + p\hat{j} + 3\hat{k}$ are (i) Perpendicular (ii) Parallel	1
36.	Find the angle between two vectors \vec{a} and \vec{b} having the same length $\sqrt{2}$ and their scalar product is -1 .	1
37.	If $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$, find the value of $(\vec{r} \times \hat{i}) \cdot (\vec{r} \times \hat{j}) + xy$.	1
38.	Find a unit vector perpendicular to both the vectors $\hat{i} - 2\hat{j} + 3\hat{k}$ and $\hat{i} + 2\hat{j} - \hat{k}$.	1
39.	If $\vec{a} = \hat{i} + 3\hat{j} - 2\hat{k}$ and $\vec{b} = -\hat{i} + 3\hat{k}$ then find $ \vec{a} \times \vec{b} $.	1
40.	Find $\hat{i} \cdot \hat{i}, \hat{j} \cdot \hat{j}$, and $\hat{k} \cdot \hat{k}$. Also find $\hat{i} \times \hat{i}, \hat{j} \times \hat{j}$ and $\hat{k} \times \hat{k}$	1
41.	The value of expression $ \vec{a} \times \vec{b} ^2 + (\vec{a} \cdot \vec{b})^2$ is (a) $\vec{a} \cdot \vec{b}$ (b) $ \vec{a} \cdot \vec{b} $ (c) $ \vec{a} ^2 \vec{b} ^2$ (d) $(\vec{a} \cdot \vec{b})$	1
42.	If is any non zero vector then $(\vec{a} \cdot \hat{i})\hat{i} + (\vec{a} \cdot \hat{j})\hat{j} + (\vec{a} \cdot \hat{k})\hat{k}$ is equal to (a) $\vec{a} \cdot \vec{b}$ (b) \vec{a} (c) 0 (d) None of these	1
43.	The vector in the direction of the vector $(\hat{i} - 2\hat{j} + 2\hat{k})$ has the magnitude 9 is (a) $(\hat{i} - 2\hat{j} + 2\hat{k})$ (b) $\frac{\hat{i} - 2\hat{j} + 2\hat{k}}{3}$ (c) $3(\hat{i} - 2\hat{j} + 2\hat{k})$ (d) $9(\hat{i} - 2\hat{j} + 2\hat{k})$	1
44.	The direction cosine of vector \vec{BA} , where the coordinates of A and B are (1,2,-1) and (3,4,0) respectively, are (a) -2,-2,-1 (b) $-\frac{2}{3}, -\frac{2}{3}, -\frac{1}{3}$ (c) 2,2,1 (d) $\frac{2}{3}, \frac{2}{3}, \frac{1}{3}$	1
45.	Angle between two vectors \vec{a} and \vec{b} with magnitude $\sqrt{3}$ and 4 respectively and $\vec{a} \cdot \vec{b} = 2\sqrt{3}$ is (a) $\frac{\pi}{6}$ (b) $\frac{\pi}{3}$ (c) $\frac{\pi}{2}$ (d) $\frac{5\pi}{2}$	1
46.	The value of p for which the vectors $2\hat{i} + p\hat{j} + \hat{k}$ and $-4\hat{i} - 6\hat{j} + 26\hat{k}$ are perpendicular to each other, is (a) 3 (b) -3 (c) $-\frac{17}{3}$ (d) $\frac{17}{3}$	1
47.	Two vectors $\vec{a} = A\hat{i} + B\hat{j} + C\hat{k}$ and $\vec{b} = L\hat{i} + M\hat{j} + N\hat{k}$ are collinear if	1

	(a) $AL + BM + CN = 0$ (b) $\frac{A}{L} = \frac{B}{M} = \frac{C}{N}$ (c) $A=L, B=M, C=N$ (d) None of these	
48.	The value of $(\hat{i} \times \hat{j}) \cdot \hat{j} + (\hat{j} \times \hat{i}) \cdot \hat{k}$ is (a) 2 (b) 0 (c) 1 (d) -1	1
49.	If $ \vec{a} = 4$ and $-3 \leq \delta \leq 2$ then the range of $ \delta \vec{a} $ is (a) $[0, 8]$ (b) $[-12, 8]$ (c) $[0, 12]$ (d) $[8, 12]$	1
50.	In $\triangle ABC$, $\vec{AB} = \hat{i} + \hat{j} + 2\hat{k}$ and $\vec{AC} = 3\hat{i} - \hat{j} + 4\hat{k}$. If D is mid- point of BC, then, \vec{AD} is equal to (a) $4\hat{i} + 6\hat{k}$ (b) $2\hat{i} - 2\hat{j} + 2\hat{k}$ (c) $\hat{i} - \hat{j} + \hat{k}$ (d) $2\hat{i} + 3\hat{k}$	1

ANSWERS:

Q. NO	ANSWER	MARKS
1.	b	1
2.	d	1
3.	a	1
4.	b	1
5.	c	1
6.	c	1
7.	a	1
8.	a	1
9.	b	1
10.	b	1
11.	b	1
12.	c	1
13.	d	1
14.	b	1
15.	d	1
16.	c	1
17.	c	1
18.	b	1
19.	c	1
20.	d	1
21.	C. $3(\hat{i} - 2\hat{j} + 2\hat{k})$	1
22.	A. form an isosceles triangle	1
23.	C. $\frac{\sqrt{5}}{6}$	1
24.	B. $\frac{\pi}{4}$	1
25.	C. $\sqrt{3}$	1
26.	A. $\frac{3}{2}(\hat{i} + \hat{j})$	1
27.	D. $-\frac{5}{\sqrt{162}}$	1
28.	A. $\frac{1}{2} \vec{a} + \vec{b} $	1

29.	B. $-\frac{3}{2}$	1
30.	C. Assertion is correct statement but reason is wrong statement.	1
31.	(i) Scalar (ii) Vector	1
32.	$\frac{12}{5}\vec{a} - \frac{13}{5}\vec{b}$	1
33.	Magnitude is equal ($\sqrt{5}$) of both vectors but since components if the vectors are not equal both vectors are not same.	1
34.	8/7	1
35.	(i) P=-15 (ii) P=2/3	1
36.	$\frac{2\pi}{3}$	1
37.	0	1
38.	$4\sqrt{3}$	1
39.	$\sqrt{91}$	1
40.	1,1,1 AND 0,0,0	1
41.	(c)	1
42.	(b)	1
43.	(c)	1
44.	(b)	1
45.	(b)	1
46.	(a)	1
47.	(b)	1
48.	(d)	1
49.	(c)	1
50.	(d)	1