## CHAPTER-15 STATISTICS 03 MARK TYPE QUESTIONS

Q. NO	QUESTION	MARK
1.	Normal brain section Hunfington's disease  H	3
	The annual incidence rates of Huntington's Disease per 100,000 individuals were recorded	
	over a span of five years. The data is as follows: 4, 7, 8, 9, 10. Calculate the mean deviation	
	about the mean for these rare disease rates.	
2.	A group of athletes participated in a practice session for a particular exercise routine over	3
	the course of several days. The recorded practice times (in minutes) for each athlete were	
	as follows: 38, 70, 48, 40, 42, 55, 63, 46, 54, 44.	
	Calculate the mean deviation about the mean for the athletes' practice times.	_
3.	A group of cars went through a series of servicing sessions at a garage. The recorded	3
	mileage before each servicing session (in thousands of kilometers) for each car were as follows: 36, 72, 46, 42, 60, 45, 53, 46, 51, 49.	
	Calculate the mean deviation about the median for the recorded mileages of the cars before their servicing sessions.	
4.	The mean and standard deviation of 20 observation is found to be 10 and 2, respectively.	3
	On rechecking, it was found that an observation 8 was incorrect. Calculate the correct mean and standard deviation in case of the wrong item is omitted.	
5.	Find the mean and standard deviation of first n terms of an A.P. whose first term is a and the common difference is d.	3
6.	Calculate the mean deviation about median for the daily wages of 12 labours getting wages (in Rs.) 48, 45, 60, 50, 46, 48, 50, 45, 70, 65,47,50	3
7.	The mean life of a sample of 60 bulbs was 650 hours and the standard deviation was 8 hours. A second sample of 80 bulbs has a mean life of 660 hours and standard deviation 7 hours. Find the overall standard deviation.	3
8.	Mean and standard deviation of 100 items are 50 and 4, respectively. Find the sum of all the item and the sum of the squares of the items.	3
9.	The mean and standard deviation of a group of 100 observations were found	3

10.	to be 20 and 3, respectively. Later on it was found that three observations were incorrect, which were recorded as 21, 21 and 18. Find the mean and standard deviation if the incorrect observations are omitted. If $a$ is a positive integer and the frequency distribution has a variance of 160 . Determine the value of $a$ .					3				
	x	а	2 <i>a</i>	3 <i>a</i>	4a	5a	ι	6a	]	
	f	2	1	1	1	1		1		
11.	An analysis of monthly wages paid to wor industry, gives the following results:  No.of wages earners  Mean of monthly wages			Firm 586 Rs.52	A 6		Firm B 648 Rs.5253	longing to the same	3	
	Variance	100	)		121					
	(i) Which	firm A or I	B pays out	larger amo	ount as mo	nthly v	wag	es?		
	(ii) which firm A or B is shows greater variability in individual wages?									
12.	The mean and variance of 7 observations are 8 and 16 respectively.  If 5 of the observations are 2, 4, 10, 12, 14. Find the remaining two observations.					3				

## **ANSWERS:**

Q. NO	ANSWER	MARKS
1.	To calculate the mean deviation about the mean, follow these steps:	3
	Calculate the mean: $(4 + 7 + 8 + 9 + 10) / 5 = 7.6$	
	Calculate the deviations from the mean for each value:	
	Deviations: -3.6, -0.6, 0.4, 1.4, 2.	
	Calculate the absolute values of the deviations: 3.6, 0.6, 0.4, 1.4, 2.4	
	Calculate the mean of the absolute deviations: $(3.6 + 0.6 + 0.4 + 1.4 + 2.4) / 5 = 1.64$	
	So, the mean deviation about the mean is approximately 1.64	
2.	Let's calculate the mean deviation about the mean for the athletes' practice times:	3
	Calculate the mean practice time: (38 + 70 + 48 + 40 + 42 + 55 + 63 + 46 + 54 + 44) /	
	10 = 50.	
	Calculate the deviations from the mean for each practice time:	
	Deviations: -12, 20, -2, -10, -8, 5, 13, -4, 4, -6.	
	Calculate the absolute values of the deviations: 12, 20, 2, 10, 8, 5, 13, 4, 4, 6.	
	Calculate the mean of the absolute deviations:	
	(12 + 20 + 2 + 10 + 8 + 5 + 13 + 4 + 4 + 6) / 10 = 8.4.	
	The mean deviation about the mean for the athletes' practice times is indeed 8.4.	
3.	To calculate the mean deviation about the median for the recorded mileages, follow	3
	these steps:	
	1. Arrange the mileages in ascending order: 36, 42, 45, 46, 46, 49, 51, 53, 60, 72.	
	2. Find the median: In this case, the median is the average of the fifth sixth values,	
	which is (46 + 49) / 2 = 47.5.	
	3. Calculate the deviations from the median for each mileage:	
	Deviations: -11.5, -5.5, -2.5, -1.5, -1.5, 1.5, 3.5, 5.5, 12.5, 24.5.	
	4. Calculate the absolute values of the deviations: 11.5, 5.5, 2.5, 1.5, 1.5, 1.5, 3.5, 5.5,	
	12.5, 24.5.	
	5. Calculate the mean of the absolute deviations:	
	(11.5 + 5.5 + 2.5 + 1.5 + 1.5 + 1.5 + 3.5 + 5.5 + 12.5 + 24.5) / 10 = 10.5.	
	So, the mean deviation about the median for the recorded mileages of the cars is	
	indeed 10.5.	
4.	Here $n=20, \bar{x}=10$ and $\sigma=2$	3

Therefore Incorrect  $\Sigma x_i = 200$ 

$$\operatorname{Now}_{\overline{n}}^{1} \Sigma x_{i}^{2} - (\bar{x})^{2} = \sigma^{2}$$

$$\Rightarrow \frac{1}{20} \Sigma x_i^2 - (10)^2 = 4 \Rightarrow \Sigma x_i^2 = 2080$$

If wrong item is omitted.

When wrong item 8 is omitted from the data then we have 19 observations.

Therefore Correct  $\Sigma x_i = \text{Incorrect } \Sigma x_i - 8$ 

Correct  $\Sigma x_i = 200 - 8 = 192$ 

Therefore Correct mean  $=\frac{192}{19}=10.1$ 

Also correct  $\Sigma x_i^2 = \text{Incorrect } \Sigma x_i^2 - (8)^2$ 

$$\Rightarrow$$
 Correct  $\Sigma x_i^2 = 2080 - 64 = 2016$ 

Hence Correct variance =  $\frac{1}{19}$ (correct  $\Sigma x_i^2$ ) – (correct mean)<sup>2</sup>

$$= \frac{1}{19} \times 2016 - \left(\frac{192}{19}\right)^{2}$$

$$= \frac{2016}{19} - \frac{36864}{361} = \frac{38304 - 36864}{361} = \frac{1440}{361}$$

Correct S.D. 
$$=\sqrt{\frac{1440}{361}} = \sqrt{3.99} = 1.997$$

5. The terms of the A.P. are: a, a + d, a + 2d, a + 3d, ..., a + (r - 1)d, ..., a + (n - 1)d.

Suppose  $\bar{X}$  be the mean of these terms.

$$\bar{X} = \frac{1}{n} \left\{ a + (a+d) + (a+2d) + \dots + (a+(n-1)d) = \frac{1}{n} \left[ \frac{n}{2} \{ 2a + (n-1)d \} \right] \right\}$$
$$= a + (n-1)\frac{d}{2}$$

Suppose  $\sigma$  be the standard deviation of n terms of the A.P.

	$\sigma^2 = \frac{1}{n} \sum_{r=1}^{n} \left[ \{ a + (r-1)d \} - \bar{X} \right]^2 \left[ \text{Using: } \sigma^2 = \frac{1}{n} \sum_{i=1}^{n} (x_i - \bar{X})^2 \right]$	
	$\Rightarrow \sigma^2 = \frac{1}{n} \sum_{r=1}^{n} \left[ \{ a + (r-1)d \} - \left\{ a + (n-1)\frac{d}{2} \right\} \right]^2$	
	$\Rightarrow \sigma^2 = \frac{d^2}{4n} \left[ \sum_{r=1}^n (2r - 2 - n + 1)^2 \right]$	
	$\Rightarrow \sigma^2 = \frac{d^2}{4n} \left[ \sum_{r=1}^n (2r - (n+1))^2 \right]$	
	$\Rightarrow \sigma^2 = \frac{d^2}{4n} \left[ \sum_{r=1}^n \left\{ 4r^2 - 4(n+1)r + (n+1)^2 \right\} \right]$	
	$\Rightarrow \sigma^2 = \frac{d^2}{4n} \left[ \left\{ 4 \left( \sum_{r=1}^n r^2 \right) - 4(n+1) \left( \sum_{r=1}^n r \right) + \sum_{r=1}^n (n+1)^2 \right] \right]$	
	$\Rightarrow \sigma^2 = \frac{d^2}{4n} \left\{ \frac{4n(n+1)(2n+1)}{6} - \frac{4(n+1)n(n+1)}{2} + n(n+1)^2 \right\}$	
	$\Rightarrow \sigma^2 = \frac{d^2}{4n} \left\{ \frac{2n(n+1)(2n+1)}{3} - n(n+1)^2 \right\}$	
	$\Rightarrow \sigma^2 = \frac{d^2}{12n} n(n+1) \{ 2(2n+1) - 3(n+1) \} = \frac{(n^2 - 1)d^2}{12}$	
	$\Rightarrow \sigma = d\sqrt{\frac{n^2 - 1}{12}}$	
6.	Arranging the wages in ascending order, we get	3
	45,45,46,47,48,48,50,50,50,60,65,70	
	Here, $n = 12$ , which is even.	
	$\therefore M = Median = Mean of \left(\frac{n}{2}\right) th and \left(\frac{n}{2} + 1\right) th observations = \frac{6th + 7th}{2}$	
	$\therefore M = \frac{48 + 50}{2} = 49$	
	Here, $n = 12, \sum  x_i - M  = 66$	
	$\therefore$ Mean deviation about median $=\frac{\sum  x_i-M }{n}=\frac{66}{12}=5.5$	
	Hence, the mean deviation about median is 5.5	
7.	We have,	3
	$n_1$ =60, $\bar{x}_1$ =650, $s_1$ =8	
	$n_2$ =80, $\bar{x}_2$ =660, $s_2$ =7	
	$\sigma = \sqrt{\frac{n_1 s_1^2 + n_2 s_2^2}{n_1 + n_2} + \frac{n_1 n_2 (\bar{x}_1 - \bar{x}_2)^2}{(n_1 + n_2)^2}}$	
	$\sigma = \sqrt{\frac{60(64) + 80(49)}{60 + 80} + \frac{60 \times 80(650 - 660)^2}{(60 + 80)^2}}$	
	$\sigma = \sqrt{(3916/49)}$	

	σ=√79.9						
8.	Hence, the overall standard deviation is 8.9 Here $\bar{x}$ =50, n = 100 and $\sigma$ =4					3	
0.		0, 11 – 100	Janu 0-4			3	
	$\frac{1}{n}\sum_{i}x_{i}=\overline{x}$						
	$\Rightarrow \sum x_i = 50$						
	$\Rightarrow \sum x_i = 50$						
	$\sigma^2 = \frac{1}{n} \sum_{i} x_i$	11					
	$\Rightarrow 16 = \frac{1}{100}$	$\sum x_i^2 - (50)$	2				
	$\Rightarrow \sum x_i^2 = 2!$						
	Hence, su	um of all i	tems is 5000	and sum of s	quares of all items is 251600.		
9.	Here n =	100, <del>x</del> −20	and $\sigma=3$			3	
	$\therefore \overline{X} = \frac{1}{n} \sum X_i$						
	⇒∑x <sub>i</sub> =n x	≅=100×2	0=2000				
	∴ Incorre	ct ∑x <sub>i</sub> = 20	000				
	Now $\frac{1}{n}\sum x_i$	$^{2}$ -( $\bar{x}$ ) $^{2}$ =9					
	$\Rightarrow \sum x_i^2 = 40$						
	_		s 21, 21 and	18 are omitte	d from the data then we		
	have 97 d						
	Correct ∑	$x_i = Incor$	rect ∑x <sub>i</sub> - 21	- 21 -18 = 194	0		
	∴ Correct mean = 1940/97 = 20						
	Also						
	Correct $\sum x_i^2 = \text{Incorrect } \sum x_i^2 - (21)^2 - (21)^2 - (18)^2$						
	= 40900 - 441 -441 324 = 39694						
	$\therefore \text{ Correct variance} = 197(\text{correct}\sum_{i}x_{i}^{2} - (\text{correct mean})^{2}$						
	$= 197 \times 39694 - (20)^{2}$ $= 409.22 - 400 = 9.22$						
			22 = 3.036				
10.	x	f	fx	$fx^2$		3	
	а	2	2a	$2a^2$			
	2 <i>a</i>	1	2a	$4a^2$			
	3 <i>a</i> 4 <i>a</i>	<u>1</u> 1	3a 4a	$\frac{9a^2}{16a^2}$			
	5 <i>a</i>	1	5 <i>a</i>	$25a^2$			
	6a	1	6a	$36a^2$			
	$\Sigma f = 7  \Sigma f x = 22a  \Sigma f x^2 = 92a^2$						
	$\sum fx^2 \qquad (\sum fx)^2$						
	Variance = $\frac{\Sigma f x^2}{\Sigma f} - \left(\frac{\Sigma f x}{\Sigma f}\right)^2$						
	$160 = \frac{92a^2}{7} - \left(\frac{22a}{7}\right)^2 \Rightarrow a = 7$						
11.	(i)	Firm A:				3	

r			
		Mean of monthly wages = $\frac{Total\ monthly\ wage}{Number\ of\ workers}$	
		$5253 = \frac{Total\ monthly\ wage}{}$	
		586	
		Total monthly wages = $5253 \times 586 = Rs.3078258$	
		Firm B:	
		Mean of monthly wages = $\frac{Total\ monthly\ wage}{Number\ of\ workers}$	
		$5253 = \frac{Total\ monthly\ wage}{648}$	
		Total monthly wages = $5253 \times 648 = \text{Rs}.3403944$	
		Clearly, firm B pays out larger amount as monthly wages.	
		(ii) Since A and B have the same mean. Therefore, the firm with greater	
		variance will have more variability. Thus, firm B has greater variability in	
		individual wages.	
	12.	Let x and y be remaining two observations.	3
		$(2+4+10+12+14+x+y)/7 = 8 \Rightarrow x + y = 14 \rightarrow (i)$	
		And $\frac{1}{7}(2^2 + 4^2 + 10^2 + 12^2 + x^2 + y^2) - Mean^2 = 16$	
		$x^2 + y^2 = 100$	
		Now, $(x + y)^2 + (x - y)^2 = 2(x^2 + y^2)$	
		$x - y = \pm 2 \rightarrow (ii)$	
		Hence the remaining two observations are 6 and 8.	
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