

## CHAPTER – 10

### VECTORS

#### TRUE / FALSE QUESTIONS

SL NO	QUESTIONS
1	Mathematically a vector is defined as a “directed line segment.”
2	If vectors are equal then their magnitudes are equal but the converse may not be true.
3	If $\vec{AB} = 2\hat{i} + \hat{j} - 2\hat{k}$ and $\vec{BC} = 6\hat{i} + 3\hat{j} - 6\hat{k}$ then the points A, B, C are collinear.
4	The projection of the vector $2\hat{i} - \hat{j} + \hat{k}$ on the vector $\hat{i} - 2\hat{j} + \hat{k}$ is $\frac{4}{\sqrt{6}}$ unit.
5	$\vec{a}$ and $-\vec{a}$ are collinear.
6	Two collinear vectors are always equal in magnitudes.
7	Two vectors having same magnitude are collinear.
8	If for three non-zero vectors, $\vec{a}, \vec{b}, \vec{c}$ , $[\vec{a}\vec{b}\vec{c}] = 0$ then the vectors are coplanar.
9	Two or more vectors are equal if they have same magnitude and direction.
10	For any non-zero vector $\vec{a}$ , $\vec{a} = (\vec{a} \cdot \hat{i})\hat{i} + (\vec{a} \cdot \hat{j})\hat{j} + (\vec{a} \cdot \hat{k})\hat{k}.$
11	If two vectors have the same magnitude and direction regardless of the positions of their initial points, then they are unit vectors.
12	The value of $\hat{i} \cdot (\hat{j} \times \hat{k}) + \hat{j} \cdot (\hat{i} \times \hat{k}) + \hat{k} \cdot (\hat{i} \times \hat{j})$ is 1
13	If $\vec{a}, \vec{b}$ and $\vec{c}$ are unit vectors such that $\vec{a} + \vec{b} + \vec{c} = \vec{0}$ , then the value of $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} = -\frac{3}{2}$
14	If $ \vec{a}  = 10,  \vec{b}  = 2$ and $\vec{b} \cdot \vec{a} = 12$ , then the value of $ \vec{b} \times \vec{a}  = 16$
15	The vector $\lambda\hat{i} + \hat{j} + 2\hat{k}, \hat{i} + \lambda\hat{j} - \hat{k}$ and $2\hat{i} - \hat{j} + \lambda\hat{k}$ are coplanar, if $\lambda = 0$
16	If $ \vec{a}  = 4$ and $-3 \leq \lambda \leq 2$ , then the range of $ \lambda\vec{a}  = 12$
17	The number of vectors of unit length perpendicular to the vectors $\vec{a} = 2\hat{i} + \hat{j} + 2\hat{k}$ and $\vec{b} = \hat{j} + \hat{k}$ are two
18	If $\theta$ is the angle between two vectors $\vec{a}$ and $\vec{b}$ , then $\vec{a} \cdot \vec{b} \geq 0$ only when $0 \leq \theta \leq \frac{\pi}{2}$ .
19	For a given vector $\vec{a}$ , the vector $\hat{a} = \frac{\vec{a}}{ \vec{a} }$ gives the unit vector in the direction of $\vec{a}$
20	If $\vec{a} = \vec{b} + \vec{c}$ then always $ \vec{a}  =  \vec{b}  +  \vec{c} $ .
21	If $\theta = \frac{\pi}{2}$ then $\vec{a} \times \vec{b} =  \vec{a}  \vec{b} $ .
22	$\vec{a} \times \vec{b}$ is a scalar.
23.	If $ \vec{a} + \vec{b}  =  \vec{a} - \vec{b} $ , then $\vec{a}$ and $\vec{b}$ are perpendicular. State true or false.

24	Direction cosines and direction ratios of a vector are always equal.
25	The direction cosines of $\vec{a}$ are unique but direction ratios of lines are not unique.
26	For any two vectors $\vec{a}$ and $\vec{b}$ , $ \vec{a} + \vec{b}  >  \vec{a}  +  \vec{b} $ .
27	For any vector $\vec{AB}$ , $\vec{AB} \neq \vec{BA}$ but $ \vec{AB}  =  \vec{BA} $ .
28	If two vectors are perpendicular to each other then vector product of the vectors is equal to zero.
29	For two vectors $\vec{a}$ and $\vec{b}$ , $\vec{a} \times \vec{b} = \vec{b} \times \vec{a}$ .
30	Direction of vector $\vec{a} \times \vec{b}$ is perpendicular to the plane containing both vector $\vec{a}$ and vector $\vec{b}$
31	$\vec{a}$ and $\vec{b}$ represents Two adjacent sides of a triangle then its area is given by $ \vec{a} \times \vec{b} $
32	If $ \vec{a}  =  \vec{b} $ then necessarily it implies $\vec{a} = \pm \vec{b}$
33	Position vector of a point $P$ is a vector whose initial point is origin.
34	If $\vec{a}$ and $\vec{b}$ are adjacent sides of a rhombus, then $\vec{a} \cdot \vec{b} = 0$
35	For any non-zero vector $\vec{a}$ , $\vec{a} = (\vec{a} \cdot \hat{i})\hat{i} + (\vec{a} \cdot \hat{j})\hat{j} + (\vec{a} \cdot \hat{k})\hat{k}$ .
36	If $\vec{a} \times \vec{b} = \hat{i} + \hat{j} + \hat{k}$ and $ \vec{a}  = 2,  \vec{b}  = 1$ , then angle between $\vec{a}$ and $\vec{b}$ is $60^\circ$ .
37	If $\vec{a}$ and $\vec{b}$ are unit vectors, then $\vec{a} \cdot \vec{b}$ can be $\sqrt{3}$ .
38	For any two non-zero vector $\vec{a}$ and $\vec{b}$ , $ \vec{a} \vec{b} +  \vec{b} \vec{a}$ is parallel to $ \vec{a} \vec{b} -  \vec{b} \vec{a}$ .
39	For vector $\vec{a}$ and $\vec{b}$ ; $\vec{a} \cdot \vec{b} = 0 \Leftrightarrow \vec{a} = \vec{0}, \vec{b} = \vec{0}$ or $\vec{a} \perp \vec{b}$ .
40	For a scalar $\lambda$ , $\lambda(\vec{a} \times \vec{b}) = (\lambda \vec{a}) \times \vec{b} = \vec{a} \times (\lambda \vec{b})$ , where $\vec{a}$ and $\vec{b}$ are given vectors.
41	If we want to show that two non-zero vectors $\vec{a}$ and $\vec{b}$ are parallel, then we should show that $\vec{a} \times \vec{b} = \vec{0}$ .
42	The value of $(\hat{i} \times \hat{j}) \cdot \hat{k} + (\hat{j} \times \hat{k}) \cdot \hat{i} = 2$
43	The value of $p = \frac{2}{3}$ for which $\vec{a} = 3\hat{i} + 2\hat{j} + 9\hat{k}$ and $\vec{b} = \hat{i} + p\hat{j} + 3\hat{k}$ are parallel vectors
44	If $\theta$ is the angle between two vectors $\hat{i} - 2\hat{j} + 3\hat{k}$ and $3\hat{i} - 2\hat{j} + \hat{k}$ then $\sin \theta = \frac{2\sqrt{6}}{7}$
45	If $\vec{X} \cdot \vec{A} = 0, \vec{X} \cdot \vec{B} = 0, \vec{X} \cdot \vec{C} = 0$ for some non-zero vector Then $[\vec{A} \vec{B} \vec{C}] = 0$
46	The value of the expression $ \vec{a} \times \vec{b} ^2 + (\vec{a} \cdot \vec{b})^2 =  \vec{a} ^2 \cdot  \vec{b} ^2$ .
47	The area of triangle whose adjacent sides are $3\hat{i} + \hat{j} + 4\hat{k}$ and $\hat{i} - \hat{j} + \hat{k}$ is 42.

48	The projection of $2\hat{i} - \hat{j} + \hat{k}$ on $\hat{i} - 2\hat{j} + \hat{k}$ is $\frac{5}{\sqrt{6}}$ .
49	If $(\vec{a} + \vec{b}) \cdot (\vec{a} - \vec{b}) = 0$ then $ \vec{a}  =  \vec{b} $ .
50	If $ \vec{a} \times \vec{b} ^2 + (\vec{a} \cdot \vec{b})^2 = 144$ and $ \vec{a}  = 4$ , then $ \vec{b}  = 8$ .
51	A vector quantity has only magnitude.
52	A scalar quantity has only magnitude.

### **ANSWERS**

<b>True False Questions</b>	
Q.No.	Answer
1	false
2	true
3	true
4	false
5	true
6	false
7	false
8	true
9	false
10	True
11	false
12	true
13	true
14	true
15	false
16	true
17	true
18	T
19	T
20	F
21	T
22	F
23	True
24	False
25	True
26.	False
27.	True
28.	False
29.	False
30	T
31	F
32	T

33	T
34	F
35	T
36	T
37	F
38	F
39	F
40	T
41	F
42	True
43	True
44	True
45	True
46	True
47	False
48	True
49	True
50	False
51	False
52	True

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