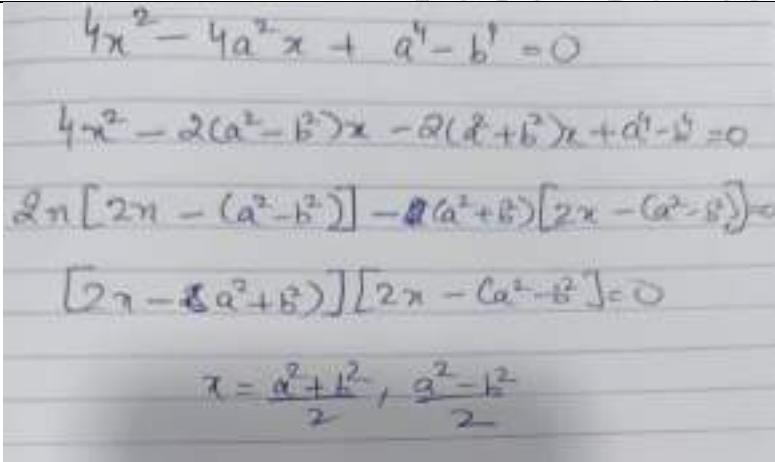
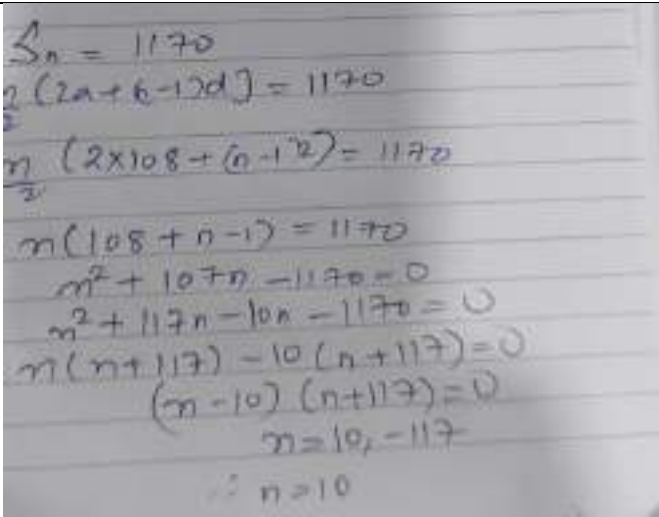


ANSWER KEY

1	(B)2
2	(C)-1
3	(D)c and a have same signs
4	(C)23
5	(B)
6	(D)
7	(C)
8	(D)
9	(A)
10	(D)
11(A) 11(B)	If α and β are the zeros of $p(x) = (a^2 + 16)x^2 + 16x + 8$ then $\alpha\beta = \frac{8a}{a^2+16} = 1 \Rightarrow a^2 + 16 = 8a \Rightarrow a^2 - 8a + 16 = 0 \Rightarrow (a - 4)^2 = 0 \Rightarrow a = 4$ Or $\alpha + \beta = -\frac{b}{a} = -\frac{-2}{3} = \frac{2}{3}, \alpha\beta = \frac{c}{a} = -\frac{1}{3}$ $(1 - \alpha)(1 - \beta) = 1 - (\alpha + \beta) + \alpha\beta = 1 - \frac{2}{3} - \frac{1}{3} = 0$
12	 $4x^2 - 4a^2x + a^4 - b^4 = 0$ $4x^2 - 2(a^2 - b^2)x - 2(a^2 + b^2)x + a^4 - b^4 = 0$ $2x[2x - (a^2 - b^2)] - 2(a^2 + b^2)[2x - (a^2 - b^2)] = 0$ $[2x - 2(a^2 + b^2)][2x - (a^2 - b^2)] = 0$ $x = \frac{a^2 + b^2}{2}, \frac{a^2 - b^2}{2}$
13(A)	 $S_n = 1170$ $\frac{n}{2}(2a + (n-1)d) = 1170$ $\frac{n}{2}(2 \times 108 + (n-1)2) = 1170$ $n(108 + n - 1) = 1170$ $n^2 + 107n - 1170 = 0$ $n^2 + 117n - 10n - 1170 = 0$ $n(n + 117) - 10(n + 117) = 0$ $(n - 10)(n + 117) = 0$ $n = 10, -117$ $\therefore n = 10$

OR

Sum of integers between 1 and 200 which any multiply of 3.

13(B)

Sequence = 3, 6, 9, ... 198

 $a=3, d=3$

$$S = \frac{n}{2}(a_1 + l_n) = \frac{66}{2}(3 + 198) \\ = 33 \times 201 = 6633$$

14(A)
)Let the usual speed be x km/h and the usual time be t h. Distance $D = xt$.

From the two altered cases:

$$(x+6)(t-4) = xt \Rightarrow -4x + 6t - 24 = 0 \Rightarrow -2x + 3t - 12 = 0,$$

$$(x-6)(t+6) = xt \Rightarrow 6x - 6t - 36 = 0 \Rightarrow x - t - 6 = 0.$$

From $x - t - 6 = 0$ we get $t = x - 6$. Substitute into $-2x + 3t - 12 = 0$:

$$-2x + 3(x - 6) - 12 = 0 \Rightarrow -2x + 3x - 18 - 12 = 0 \Rightarrow x = 30 \text{ km/h.}$$

Then $t = x - 6 = 24$ h, so the distance is

$$D = xt = 30 \times 24 = 720 \text{ km.}$$

Or

Let the number of chocolates in lot A be x and in lot B be y .

14(B)

From the first selling method: ₹2 for 3 chocolates (so price per chocolate = $2/3$ ₹) on lot A, and ₹1 each on lot B, total ₹400:

$$\frac{2}{3}x + 1 \cdot y = 400 \Rightarrow 2x + 3y = 1200.$$

From the second selling method: ₹1 each on lot A, and ₹4 for 5 chocolates on lot B (price per chocolate = $4/5$ ₹), total ₹460:

$$1 \cdot x + \frac{4}{5}y = 460 \Rightarrow 5x + 4y = 2300.$$

Solve the linear system

$$\begin{cases} 2x + 3y = 1200, \\ 5x + 4y = 2300. \end{cases}$$

Eliminate x : multiply the first by 5 and the second by 2,

$$10x + 15y = 6000, \quad 10x + 8y = 4600,$$

subtracting gives $7y = 1400$, so $y = 200$. Substitute in $2x + 3y = 1200$:

$$2x + 600 = 1200 \Rightarrow 2x = 600 \Rightarrow x = 300.$$

Total chocolates = $x + y = 300 + 200 = \boxed{500}$.

15

$$\alpha + \beta = 5, \alpha\beta = 4$$

$$\frac{1}{\alpha^2} + \frac{1}{\beta^2} - 2\alpha\beta$$

$$\frac{\alpha^2 + \beta^2}{\alpha^2\beta^2} - 2\alpha\beta$$

$$\frac{(\alpha + \beta)^2 - 2\alpha\beta}{\alpha^2\beta^2} - 2\alpha\beta = \frac{(5)^2 - 2(4)}{(4)^2} - 2(4)$$

$$= \frac{25 - 8}{16} - 8$$

$$= \frac{17}{16} - 8 = \frac{17 - 128}{16} = \frac{-111}{16}$$

16

- (i) 40 km/hr
 (ii) 50 km/hr
 (iii)(A) 15hrs
 (iii)(B) 12hrs

17

- (i) 250
 (ii) 110 rollers per year
 (iii)

— To find in which year production was 1350: solve $a + (n - 1)d = 1350$:

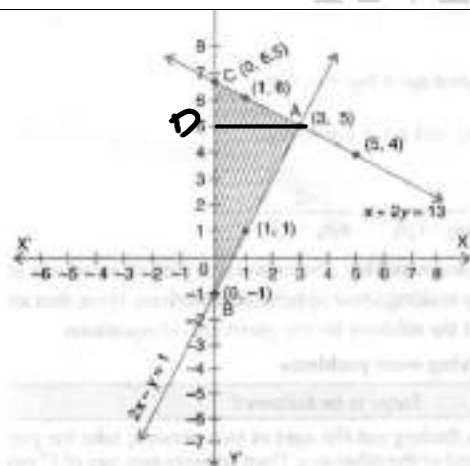
$$250 + (n - 1) \cdot 110 = 1350 \Rightarrow (n - 1) \cdot 110 = 1100 \Rightarrow n - 1 = 10 \Rightarrow n = 11.$$

So production reached 1350 rollers in the 11th year.

— Production in the 8th year:

$$a_8 = a + 7d = 250 + 7(110) = 250 + 770 = \boxed{1020 \text{ rollers}}.$$

18



Area of triangle ABC = $\frac{1}{2} \times BC \times AD = \frac{1}{2} \times 7.5 \times 3 = 11.25$ sq units.

19

Given $S_4 = 40$ and $S_{14} = 280$:

$$S_4 = \frac{4}{2}(2a + 3d) = 40 \Rightarrow 2a + 3d = 20,$$

$$S_{14} = \frac{14}{2}(2a + 13d) = 280 \Rightarrow 2a + 13d = 40.$$

Subtract the first equation from the second:

$$(2a + 13d) - (2a + 3d) = 40 - 20 \Rightarrow 10d = 20 \Rightarrow d = 2.$$

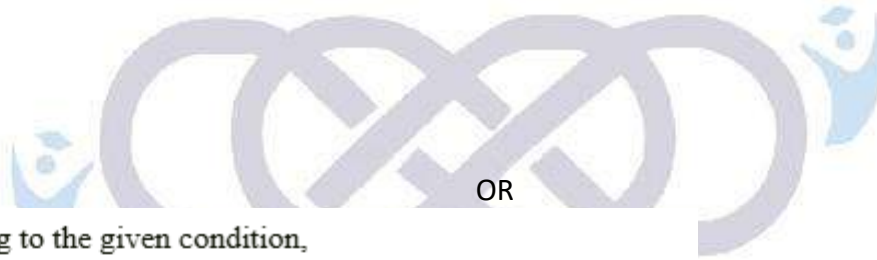
Plug $d = 2$ into $2a + 3d = 20$:

$$2a + 6 = 20 \Rightarrow 2a = 14 \Rightarrow a = 7.$$

Now form S_n :

$$S_n = \frac{n}{2}(2a + (n-1)d) = \frac{n}{2}(14 + 2(n-1)) = \frac{n}{2}(2n + 12) = n(n+6).$$

Quick checks: $S_4 = 4(4+6) = 4 \cdot 10 = 40$ and $S_{14} = 14(14+6) = 14 \cdot 20 = 280$



OR

According to the given condition,

$$\Rightarrow mt_m = nt_n$$

$$\Rightarrow m\{a + (m-1)d\} = n\{a + (n-1)d\}$$

$$\Rightarrow ma + md(m-1) = na + nd(n-1)$$

$$\Rightarrow ma + m^2d - md = na + n^2d - nd$$

$$\Rightarrow ma + m^2d - md - na - n^2d + nd = 0$$

$$\Rightarrow (ma - na) + (m^2d - n^2d) - (md - nd) = 0$$

$$\Rightarrow a(m-n) + d(m^2 - n^2) - d(m-n) = 0$$

$$\Rightarrow a(m-n) + d(m+n)(m-n) - d(m-n) = 0$$

$$\Rightarrow (m-n)[a + (m+n-1)d] = 0$$

$$\Rightarrow [a + (m+n-1)d] = 0 \quad \dots [\text{Dividing both sides by } (m-n)]$$

$$\Rightarrow t(m+n) = 0$$

Hence, the $(m+n)^{\text{th}}$ term of the given A.P. is zero