MATHEMATICS - Code No. 041 MARKING SCHEME CLASS - XII (2025-26)

	SECTION-A (MCQs of 1 mark each)		
Sol. N.	Hint / Solution	Marks	
1	Clearly from the graph Domain is $\left[-\frac{1}{2}, \frac{1}{2}\right]$ So graph is of the function $\sin^{-1}(2x)$ Answer is (B) $\sin^{-1}(2x)$	1	
1 (V.I.)	Domain is $\left[-\frac{1}{3}, \frac{1}{3}\right]$ So the function is $\cos^{-1}(3x)$ Answer is (C) $\cos^{-1}(3x)$	1	
2	AB is defined so n=4 AC is defined so p=4 AB and AC are square matrices of same order so $m \times 3 = m \times q \Rightarrow q = 3 = m$ Answer is (A) $m = q = 3$ and $n = p = 4$	1	
3	As A is skew symmetric So $p = 0, q = 2, r = -3, t = 4$ So $\frac{q+t}{p+r} = \frac{6}{-3} = -2$ Answer is (A) -2	1	
4	$ adj A = 27 \Rightarrow A ^3 = 27 = 3^3 \Rightarrow A = 3$ A (adj A) = A I = 3 I Answer is (C) 3 I	1	
5	Inverse of the matrix $\begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 5 \end{bmatrix} = \begin{bmatrix} \frac{1}{3} & 0 & 0 \\ 0 & \frac{1}{2} & 0 \\ 0 & 0 & \frac{1}{5} \end{bmatrix}$ Answer is (B)	1	
6	$\begin{vmatrix} \cos 67^o & \sin 67^o \\ \sin 23^o & \cos 23^o \end{vmatrix} = \cos 67^o \cos 23^o - \sin 67^o \sin 23^o = \cos(67^o + 23^o) = \cos 90^o = 0$ Answer is (A) 0	1	
7	$f(x) \text{ is continuous at } x = \pi$ $\Rightarrow \lim_{x \to \pi^{-}} (kx+1) = \lim_{x \to \pi^{+}} \cos x = f(\pi)$ $\Rightarrow \lim_{h \to 0} [k(\pi-h)+1] = \lim_{h \to 0} \cos(\pi+h) = k\pi+1$ $\Rightarrow k\pi+1 = -1 \qquad \Rightarrow k = \frac{-2}{\pi}$ Answer is (D) $\frac{-2}{\pi}$	1	

	$f(x) = x \tan^{-1} x$	
8	$f'(x) = 1 \cdot \tan^{-1} x + x \cdot \frac{1}{1+x^2}$ $f'(1) = 1 \cdot \tan^{-1} 1 + \frac{1}{1+1} = \frac{\pi}{4} + \frac{1}{2}$ Answer is (B) $\frac{\pi}{4} + \frac{1}{2}$	1
9	$f(x) = 10 - x - 2x^{2}$ $\Rightarrow f'(x) = -1 - 4x$ For increasing function $f'(x) \ge 0$ $\Rightarrow -(1 + 4x) \ge 0$ $\Rightarrow (1 + 4x) \le 0$ $\Rightarrow x \le -\frac{1}{4}$ $\Rightarrow x \in \left(-\infty, -\frac{1}{4}\right]$ Answer is (A) $\left(-\infty, -\frac{1}{4}\right]$	1
10	$xdx + ydy = 0$ $\Rightarrow \int xdx = -\int ydy$ $\Rightarrow \frac{x^2}{2} = -\frac{y^2}{2} + k$ $\Rightarrow x^2 + y^2 = 2k$ Solution is $x^2 + y^2 = 2k$, k being an arbitrary constant. Answer is (C) Circles	1
11	$I = \int_{a}^{b} x f(x) dx = \int_{a}^{b} (a+b-x) f(a+b-x) dx$ $\Rightarrow I = \int_{a}^{b} (a+b-x) f(x) dx (given \ f(a+b-x) = f(x))$ $\Rightarrow I = \int_{a}^{b} (a+b) f(x) dx - \int_{a}^{b} x f(x) dx$ $\Rightarrow 2I = (a+b) \int_{a}^{b} f(x) dx$ $\Rightarrow I = \frac{1}{2} (a+b) \int_{a}^{b} f(x) dx$ Answer is (D) $\frac{a+b}{2} \int_{a}^{b} f(x) dx$	1
12	Let $I = \int x^3 \sin^4(x^4) \cos(x^4) dx$ Let $\sin(x^4) = t \Rightarrow 4x^3 \cos(x^4) dx = dt \Rightarrow x^3 \cos(x^4) = \frac{1}{4} dt$ Thus $I = \int t^4 \left(\frac{1}{4} dt\right) = \frac{1}{20} t^5 + C = \frac{1}{20} \sin^5(x^4) + C$ $\Rightarrow I = \frac{1}{20} \sin^5(x^4) + C = a \sin^5(x^4) + C$ So, $a = \frac{1}{20}$ Answer is (B) $\frac{1}{20}$	1
13	The projection of the vector $\hat{\imath}+2\hat{\jmath}+\hat{k}$ on the line $\vec{r}=\left(3\hat{\imath}-\hat{\jmath}\right)+\lambda(\hat{\imath}+2\hat{\jmath}+3\hat{k}$) is $\frac{1\times1+2\times2+1\times3}{\sqrt{1^2+2^2+3^2}}=\frac{8}{\sqrt{14}}$ units Answer is (C) $\frac{8}{\sqrt{14}}$ units	1

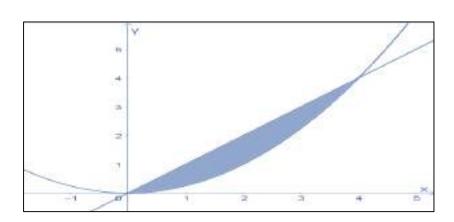
14	The distance of the point (a, b, c) from the y-axis is $\sqrt{a^2+c^2}$ So, the distance is $\sqrt{3^2+5^2}=\sqrt{34}$ units. Answer is (B) $\sqrt{34}$ units	1
15	$(2\vec{a}.\hat{\imath})\hat{\imath} - (\vec{b}.\hat{\jmath})\hat{\jmath} + (\vec{c}.\hat{k})\hat{k} = (2 \times 3)\hat{\imath} - (1)\hat{\jmath} + (2)\hat{k}$ = $6\hat{\imath} - \hat{\jmath} + 2\hat{k} = \vec{c}$ Answer is (D) \vec{c}	1
16	The points (1,0) and (0,2) satisfy the equation $2x + y = 2$ And shaded region shows that (0,0) doesn't lie in the feasible solution region So, the inequality is $2x + y \ge 2$ Answer is (B) $2x + y \ge 2$	1
16 (V.I.)	$(4,0)$ and $(0,3)$ gives maximum value so $Z_{(4,0)}=Z_{(0,3)}\Rightarrow 4a+c=3b+c\Rightarrow 4a=3b$ Answer is (A) $4a=3b$	1
17	The student may read the point $(2,9)$ from the line on the graph. The student may find the equation $3x + y = 15$ joining $(5,0)$ and $(0,15)$ and then verify the point $(2,9)$ satisfies it. Answer is (A) $(2,9)$	1
17 (V.I.)	Answer is (C) Open Half plane that contains origin, but not the points of the line $3x + 5y = 10$	1
18	Answer is (B) $\frac{1}{100}$ The person knows the first 4 digits. So the person has to guess the remaining two digits. P (guessing the PIN)=1×1×1×1× $\frac{1}{10}$ × $\frac{1}{10}$ = $\frac{1}{100}$	1
19	$\sin^{-1}\left(\frac{\sqrt{3}}{2}\right) + \tan^{-1}1 - \sec^{-1}\left(\sqrt{2}\right) = \frac{\pi}{3} + \frac{\pi}{4} - \frac{\pi}{4} = \frac{\pi}{3} \neq \frac{\pi}{4}$ So, A is false. Principal Value branch of $\sin^{-1}x$ is $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$ and that of $\sec^{-1}x$ is $\left[0, \pi\right] - \left\{\frac{\pi}{2}\right\}$. So, R is true Answer is (D)Assertion is false, but Reason is true	1
20	C. $\vec{r} \times (\vec{a} + \vec{b}) = \vec{0} \Rightarrow \vec{r}$ is parallel to $(\vec{a} + \vec{b})$ and $(\vec{a} + \vec{b})$ lies on the plane of \vec{a} and \vec{b} . So, \vec{r} is parallel to the plane of \vec{a} and $\vec{b} \Rightarrow \vec{r}$ is perpendicular to $(\vec{a} \times \vec{b})$. So, Assertion is true But $(\vec{a} + \vec{b})$ lies on the plane of \vec{a} and \vec{b} , so $(\vec{a} + \vec{b})$ is not perpendicular to the plane of \vec{a} and \vec{b} Therefore, Reason is false. Answer is (C) Assertion is true, but Reason is false	1

SECTION B (VSA type questions of 2 marks each) $\tan\left(\tan^{-1}(-1) + \frac{\pi}{3}\right) = \tan\left(-\frac{\pi}{4} + \frac{\pi}{3}\right)$ $= \frac{\tan\frac{\pi}{3} - \tan\frac{\pi}{4}}{1 + \tan\frac{\pi}{3}\tan\frac{\pi}{4}}$ 21A 1/2 1 $=\frac{\sqrt{3}-1}{1+\sqrt{2}}$ or $2-\sqrt{3}$ 1/2 OR **OR** 21B 1/2 For domain, $-1 \le 3x - 2 \le 1$ 1/2 $\Rightarrow 1 < 3x < 3$ 1/2 $\Rightarrow \frac{1}{2} \le x \le 1$ So, domain of $\cos^{-1}(3x-2)$ is $\left[\frac{1}{2},1\right]$ 1/2 $y = \log \tan \left(\frac{\pi}{4} + \frac{x}{2} \right)$ 22 Differentiating with respect to x $\frac{dy}{dx} = \frac{1}{\tan\left(\frac{\pi}{4} + \frac{x}{2}\right)} .sec^2\left(\frac{\pi}{4} + \frac{x}{2}\right) .\frac{1}{2}$ 1/2 $= \frac{\cos(\frac{\pi}{4} + \frac{x}{2})}{\sin(\frac{\pi}{4} + \frac{x}{2})} \cdot \frac{1}{\cos^2(\frac{\pi}{4} + \frac{x}{2})} \cdot \frac{1}{2}$ $= \frac{1}{2\sin(\frac{\pi}{4} + \frac{x}{2})\cos(\frac{\pi}{4} + \frac{x}{2})} = \frac{1}{\sin(\frac{\pi}{2} + x)} = \frac{1}{\cos x}$ 1 1/2 $\int \frac{(x-3)e^x}{(x-1)^3} dx = \int \frac{(x-1-2)e^x}{(x-1)^3} dx$ 23A $= \int \left(\frac{1}{(x-1)^2} - \frac{2}{(x-1)^3}\right) e^x \ dx = \int \left(\frac{1}{(x-1)^2} + \frac{d}{dx}\left(\frac{1}{(x-1)^2}\right)\right) e^x \ dx$ 1 (as $\int (f(x) + f'(x))e^x dx = e^x f(x) + c$) $=\frac{e^x}{(x-1)^2}+c$ 1 **OR** OR $A = \int_0^4 x \, dy = \int_0^4 \sqrt{y} \, dy$ 23B 1 $=\frac{2}{3} \times y^{3/2}\Big|_{y=0}^{y=4} = \frac{16}{3}$ sq. units 1 23B For Visually Impaired: $A = \int_0^3 y \ dx = \int_0^3 \sqrt{x} \ dx$ 1 1 $=\frac{2}{3} \times x^{3/2}\Big|_{x=0}^{x=3} = 2\sqrt{3}$ sq. units

24	Given $f(x + y) = f(x)f(y)$	
	f(0+5) = f(0)f(5)	1/
	$\Rightarrow f(0) = 1$ $f(5+h)-f(5) = f(5)f(h)-f(5) = f(5)f(h)-f(f(h)-f(h)-f(f(h)-f(h)-f(h)-f(h)-$	1/2
	$f'(5) = \lim_{h \to 0} \frac{f(5+h) - f(5)}{h} = \lim_{h \to 0} \frac{f(5)f(h) - f(5)}{h} \left[\because f(x+y) = f(x)f(y) \right]$	
	$= \lim_{h \to 0} \frac{2f(h) - 2}{h} \qquad [:: f(5) = 2]$	1
	$h \to 0$ h $h \to 0$ h $h \to 0$ h	
	$=2\lim_{h\to 0}\frac{f(h)-1}{h}=2\lim_{h\to 0}\frac{f(h)-f(0)}{h}=2f'(0)$	
	$= 2 (3) [\because f'(0) = 3]$	1/2
	= 6	
25	-	1/
25	The vector $\overrightarrow{OP} = \frac{1}{2}(4\hat{\imath} + 4\hat{k}) = 2\hat{\imath} + 2\hat{k}$	1/2
	Area of the parallelogram formed by the two adjacent sides as OA and OP	
	$ \hat{i} \hat{j} \hat{k} $	1/2
	$= \left (\overrightarrow{OA} \times \overrightarrow{OP}) \right = \begin{vmatrix} \hat{\imath} & \hat{\jmath} & \hat{k} \\ 1 & 1 & 1 \\ 2 & 0 & 2 \end{vmatrix}$, 2
	$= 2\hat{i}-2\hat{k} $	1/2
	$= 2\sqrt{2}$ square units.	1/2
	SECTION C	
	SECTION C (SA type questions of 3 marks each)	
	(OA type questions of a marks each)	
26A	$x^y = e^{x-y}$	
	Taking log of both sides	
	$y \log x = (x - y) \log e$	
	$y \log x + y = x \text{ (since } \log e = 1)$ $\Rightarrow y = \frac{x}{1 + \log x}$	1
		1
	Differentiating with respect to x	
	$\frac{dy}{dx} = \frac{(1 + \log x) \cdot 1 - x \cdot \frac{1}{x}}{(1 + \log x)^2}$	
	$\frac{dx}{\log x}$	
	$= \frac{\log x}{(\log e + \log x)^2}$	
	$=\frac{\log x}{(\log(xe))^2}$	1
	Now $\frac{dy}{dx}\Big _{x=e} = \frac{\log e}{(\log e^2)^2} = \frac{1}{(2\log e)^2} = \frac{1}{2^2} = \frac{1}{4}$ (as $\log e = 1$)	1
	$\frac{110W}{dx}\Big _{x=e} - \frac{1}{(\log e^2)^2} - \frac{1}{(2\log e)^2} - \frac{1}{2^2} - \frac{1}{4} $ (as $\log e = 1$)	1
	Alternative Solution:	
	Alternative Solution.	
	$x^y = e^{x-y}$	
	Taking log of both sides	
	$y\log x = (x-y)\log e$	
	$y \log x + y = x \text{ (since } \log e = 1)$	
	Differentiating both sides w.r.t. x	
	$\log x \frac{dy}{dx} + \frac{y}{x} + \frac{dy}{dx} = 1$	
	$\Rightarrow \frac{dy}{dx}(1 + \log x) = 1 - \frac{y}{x}$	
	test st	
	$\Rightarrow \frac{dy}{dx} = \frac{x - y}{x(1 + \log x)} = \frac{x - \frac{x}{1 + \log x}}{x(1 + \log x)} = \frac{x(1 + \log x) - x}{x(1 + \log x)^2} = \frac{x(1 + \log x - 1)}{x(\log e + \log x)^2} = \frac{\log x}{(\log(xe))^2}$	
	Now $\frac{dy}{dx}\Big _{x=e} = \frac{\log e}{(\log e^2)^2} = \frac{1}{(2\log e)^2} = \frac{1}{2^2} = \frac{1}{4}$ (as $\log e = 1$)	

	OR	OR
26B	$\frac{dx}{d\theta} = a(1 - \cos\theta), \frac{dy}{d\theta} = a(0 + \sin\theta),$	1
	$\Rightarrow \frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{a\sin\theta}{a(1-\cos\theta)}$ $= \frac{2\sin(\frac{\theta}{2})\cos(\frac{\theta}{2})}{2\sin^2(\frac{\theta}{2})} = \cot\frac{\theta}{2}$	1
	$\Rightarrow \frac{d^2y}{dx^2} = -\frac{1}{2} \csc^2\left(\frac{\theta}{2}\right) \frac{d\theta}{dx}$ $= -\frac{1}{2a} \csc^2\left(\frac{\theta}{2}\right) \frac{1}{2\sin^2\left(\frac{\theta}{2}\right)}$ $= -\frac{1}{4a} \csc^4\left(\frac{\theta}{2}\right)$	1
27	Let r be the radius of ice ball at time t. $V = \frac{4}{3}\pi r^3 \dots (1)$	1/2
	$S = 4\pi r^2$ (2) Given $\frac{dV}{dt} \propto S$	72
	$\Rightarrow \frac{dV}{dt} = - \text{ k S (where k is some positive constant)(3)}$ Differentiating (1) w.r.t. t, we get	1/2
	$\frac{dV}{dt} = \frac{4}{3} \pi \cdot (3 r^2) \frac{dr}{dt}$ $\frac{dV}{dt} = 4\pi r^2 \frac{dr}{dt} \dots \dots \dots (4)$	1
	$\Rightarrow - k S = 4\pi r^2 \frac{dr}{dt} \text{(from (3) and (4))}$ $\Rightarrow - k S = S \frac{dr}{dt} \text{(using (2))}$	1/2
	$\Rightarrow -k S = S \frac{dr}{dt} \qquad \text{(using (2))}$ $\Rightarrow \frac{dr}{dt} = -k$	1/2
	\Rightarrow radius of the ice-ball decreases at a constant rate	
28A	y = -x - 1 $y = x + 1$	1
	$\int_{-4}^{2} x+1 dx = \int_{-4}^{-1} (-x-1) dx + \int_{-1}^{2} (x+1) dx$	1/2
	$= -\frac{(x+1)^2}{2} \Big]_{-4}^{-1} + \frac{(x+1)^2}{2} \Big]_{-1}^{2}$	1/2
	$= -\left(0 - \frac{9}{2}\right) + \left(\frac{9}{2} - 0\right) = 9$ It represent the area of shaded region bounded by the curve $y = x + 1 $,	1/2
	x – axis and the lines $x = -4$ and $x = 2$	1/2

28B



1

1

1/2

1/2

1

1

1

OR

Required Area =
$$\int_0^4 x \, dx - \int_0^4 \frac{x^2}{4} \, dx$$

= $\frac{x^2}{2} \Big|_0^4 - \frac{1}{12} [x^3]_0^4$
= $\frac{1}{2} (16 - 0) - \frac{1}{12} (64 - 0) = 8 - \frac{16}{3} = \frac{8}{3}$ sq. units

For Visually Impaired:

$$y = |x+1| = f(x) = \begin{cases} -x - 1, & x < -1 \\ x + 1, & x \ge -1 \end{cases}$$

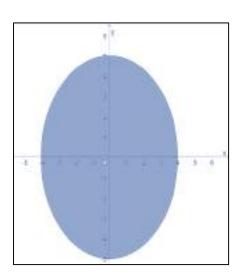
$$\int_{-4}^{2} |x+1| dx = \int_{-4}^{-1} (-x - 1) dx + \int_{-1}^{2} (x + 1) dx$$

$$= -\frac{(x+1)^{2}}{2} \Big|_{-4}^{-1} + \frac{(x+1)^{2}}{2} \Big|_{-1}^{2}$$

$$= -\left(0 - \frac{9}{2}\right) + \left(\frac{9}{2} - 0\right) = 9$$
It represent the area of shaded region bounded by the curve $x = |x+1|$

It represent the area of shaded region bounded by the curve y = |x + 1|, x - axis and the lines x = -4 and x = 2

OR



	$25x^{2} + 16y^{2} = 400 \implies \frac{x^{2}}{16} + \frac{y^{2}}{25} = 1 \implies \frac{x^{2}}{4^{2}} + \frac{y^{2}}{5^{2}} = 1 \implies y = \frac{5}{4}\sqrt{4^{2} - x^{2}}$	
	Required Area = $4 \int_0^4 \frac{5}{4} \sqrt{4^2 - x^2} dx$	1
	$= 5 \left[\frac{x\sqrt{4^2 - x^2}}{2} + \frac{4^2}{2} \sin^{-1} \left(\frac{x}{4} \right) \right]_0^4$	1
	$= 5 \begin{bmatrix} 2 & \frac{1}{2} & \frac{3}{10} & \frac{1}{4} \end{bmatrix}_0$ = 5[0 + 8 sin ⁻¹ (1) - 0]	
		1
	$=40\times\frac{\pi}{2}=20\pi \text{ sq. units}$	1
29A	The line through $(2, -1,3)$ parallel to the z-axis is given by	1
	$\vec{r} = (2\hat{\imath} - \hat{\jmath} + 3\hat{k}) + \lambda(\hat{k})$ Any point on this line is $P(2, 1, 2, 1, 3)$	1 1/2
	Any point on this line is $P(2, -1, 3 + \lambda)$ Any point on the given line $\vec{r} = (2\hat{\imath} - \hat{\jmath} + 2\hat{k}) + \mu(3\hat{\imath} + 6\hat{\jmath} + 2\hat{k})$ is	/2
	Q $(2 + 3\mu, -1 + 6\mu, 2 + 2\mu)$	
	For the intersection point	1/2
	Q $(2 + 3\mu, -1 + 6\mu, 2 + 2\mu) = P(2, -1, 3 + \lambda) \Rightarrow 2 = 2 + 3\mu \Rightarrow \mu = 0$	1/ ₂ 1/ ₂
	The point of intersection is $(2, -1,2)$	/2
	The distance from $(2, -1,3)$ to $(2, -1,2)$ is clearly 1 unit.	
	Alternative Solution:	
	Any point on the line through $(2, -1, 3)$ parallel to the z-axis is $(2, -1, \lambda)$	1
	Any point on the given line is $(2 + 3\mu, -1 + 6\mu, 2 + 2\mu)$ Therefore, $2 = 2 + 3\mu \Rightarrow \mu = 0$	
	The point of intersection is $(2, -1, 2)$	1 1/2
	The distance from $(2,-1,3)$ to $(2,-1,2)$ is clearly 1 unit.	1/2
29B	OR	
	The line through $(2,-1,1)$ parallel to the z-axis is $\vec{r} = (2\hat{\imath} - \hat{\jmath} + \hat{k}) + \lambda(\hat{k})$	1
	Any point on this line is $P(2, -1, 1+ \lambda)$	
	Any point on the given line is A $(3 + \mu, \mu, 1 + \mu)$	
	A $(3 + \mu, \mu, 1 + \mu)$ = P $(2, -1, 1 + \lambda) \Rightarrow \mu = -1$ The point of intersection is $(2, -1, 0)$	1 1/2
	The distance of $(2, -1, 0)$ from the z-axis is $\sqrt{2^2 + (-1)^2} = \sqrt{5}$ units.	1/2
30	Sketching the graph	1
		$1\frac{1}{2}$
	1000	
	800	
	0.00	
	C = (800 400)	
	D=(400, 38	
	200	
	×	
	-200 0 200 400 600 800 1000 1204 1400 1600 1800 A = (600, 0) B = (1200, 0)	
	-200 0 400 A = (600, 0) 1000 1204 1400 1600 1806 -200	

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	Corner points A(600,0), B(1200,0), C(800,400), D(400,200) Values of Z: $Z_A = 1200, Z_B = 2400, Z_C = 2000, Z_D = 1000$ Maximum $Z = 2400$ when $x = 1200$ and $y = 0$	1/ ₂ 1/ ₂ 1/ ₂
	For Visually Impaired:	/2
30	At Corner points A(600,0), B(1200,0), C(800,400), D(400,200) Values of Z are $Z_A = 1800, Z_B = 3600, Z_C = 3200, Z_D = 1600$ Maximum Value of Z = 3600 at B(1200,0) And Minimum Value of Z= 1600 at D(400,200)	1 1 1
31	Let the events be: A: Mehul is selected B: Rashi is selected Then according to the question, A and B are independent events and $P(A) = 0.4, P(A \cap \overline{B}) + P(B \cap \overline{A}) = 0.5$ Let $P(B) = x$ Then $P(A \cap \overline{B}) + P(B \cap \overline{A}) = 0.5$ $\Rightarrow P(A)P(\overline{B}) + P(B)P(\overline{A}) = 0.5$ $\Rightarrow 0.4(1-x) + x(1-0.4) = 0.5$ $\Rightarrow 0.4 - 0.4x + 0.6x = 0.5$ $\Rightarrow 0.2x = 0.5 - 0.4 = 0.1$ $\Rightarrow x = \frac{0.1}{0.2} = \frac{1}{2} = 0.5$	1
	So, probability of selection of Rashi = 0.5 Probability of selection of at least one of them = $1 - P(\bar{A} \cap \bar{B})$	
	$= 1 - P(\bar{A})P(\bar{B})$ $= 1 - 0.6 \times 0.5$ $= 1 - 0.3 = 0.7$	1
	SECTION D (LA type questions of 5 marks each)	
32	$AB = \begin{bmatrix} 3 & -6 & -1 \\ 2 & -5 & -1 \\ -2 & 4 & 1 \end{bmatrix} \begin{bmatrix} 1 & -2 & -1 \\ 0 & -1 & -1 \\ 2 & 0 & 3 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = I$	1
	So, $A^{-1} = B$ and $B^{-1} = A$ Given system of equations is	1/2
	3x - 6y - z = 3, $2x - 5y - z + 2 = 0$, $-2x + 4y + z = 5$	
	In matrix form it can be written as: $AX = C$,	1/2
	where $X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ and $C = \begin{bmatrix} 3 \\ -2 \\ 5 \end{bmatrix}$	1/2
	Here $ A = -3 - 0 + 2 = -1 \neq 0$	1/2
	So, the system is consistent and has unique solution given by the expression $X = A^{-1}C = BC$	1/2
		72
	$\Rightarrow X = \begin{bmatrix} 1 & -2 & -1 \\ 0 & -1 & -1 \\ 2 & 0 & 3 \end{bmatrix} \begin{bmatrix} 3 \\ -2 \\ 5 \end{bmatrix} \Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ -3 \\ 21 \end{bmatrix}$	1 1/2
	Thus $x = 2, y = -3, z = 21$	72

33A	Let $x = \tan \theta \implies dx = sec^2\theta \ d\theta$	1/2
	$I = \int_0^{\frac{\pi}{4}} \frac{\log(1 + tan\theta)}{1 + tan^2\theta} \cdot sec^2\theta \ d\theta$	
	$I = \int_0^{\frac{\pi}{4}} \log \left(1 + \tan \theta \right) d\theta = \int_0^{\frac{\pi}{4}} \log \left[1 + \tan \left(\frac{\pi}{4} - \theta \right) \right] d\theta$	1
	$= \int_0^{\frac{\pi}{4}} \log \left[1 + \frac{1 - \tan \theta}{1 + \tan \theta} \right] d\theta$	1
	$= \int_0^{\frac{\pi}{4}} \log \left[\frac{1 + \tan \theta + 1 - \tan \theta}{1 + \tan \theta} \right] d\theta$	1
	$= \int_0^{\pi/4} \log \left[\frac{2}{1 + \tan \theta} \right] d\theta$	
	T T	
	$= \int_0^{\frac{n}{4}} \log 2 \ d\theta - \int_0^{\frac{n}{4}} \log[1 + \tan \theta] \ d\theta$	1
	$= \log 2 \times x \Big]_0^{\frac{\pi}{4}} - I$	1
	$\Rightarrow 2I = \frac{\pi}{4} \log 2$ $\Rightarrow I = \frac{\pi}{8} \log 2$	1
	- 1 8 105 L	1/2
33B	OR	OR
	(2 sin (1 2) see (1 2) see (1 2) see (1 2)	
	$I = \int \frac{(3\sin\theta - 2)\cos\theta}{5 - \cos^2\theta - 4\sin\theta} d\theta = \int \frac{(3\sin\theta - 2)\cos\theta}{5 - (1 - \sin^2\theta) - 4\sin\theta} d\theta$	1/2
	Let $\sin \theta = t \implies \cos \theta \ d\theta = dt$	
	$I = \int \frac{(3t-2)}{5-(1-t^2)-4t} dt$	1
	$= \int \frac{(3t-2)}{t^2-4t+4} dt = \int \frac{3t-2}{(t-2)^2} dt$	
	Let $\frac{3t-2}{(t-2)^2} = \frac{A}{(t-2)} + \frac{B}{(t-2)^2}$	
	3t - 2 = A(t - 2) + B Comparing the coefficients of t and constant terms on both sides	1/
	A = 3, -2A + B = -2, B = 4	1/ ₂ +1/ ₂
	$\int \frac{(3\sin\theta - 2)\cos\theta}{5 - \cos^2\theta - 4\sin\theta} d\theta = \int \frac{3}{t - 2} dt + \int \frac{4}{(t - 2)^2} dt$	
	$= 3\log t - 2 - \frac{4}{t-2} + C$	1+1
	$= 3 \log \sin \theta - 2 - \frac{4}{\sin \theta - 2} + C$, 2
34A	$y + \frac{d}{dx}(xy) = x(\sin x + x)$	
	$\Rightarrow y + (x\frac{dy}{dx} + y) = x (\sin x + x)$	1
	$\Rightarrow 2y + x \frac{dy}{dx} = x \left(\sin x + x \right)$	•
	$\Rightarrow \frac{dy}{dx} + \frac{2y}{x} = (\sin x + x)$	
	This a linear differential equation of the form $\frac{dy}{dx} + Py = Q$	
	P= $\frac{2}{x}$,Q= $(\sin x + x)$ LF = $e^{\int \frac{2}{x} dx} = e^{2 \log x} = e^{\log x^2} = x^2$	1
	Solution will be $y \cdot I.F = \int Q \cdot IF \ dx$	1
	$yx^{2} = \int (\sin x + x) x^{2} dx$ $yx^{2} = \int \sin x \cdot x^{2} dx + \int x^{3} dx$	
	$yx - \int \sin x \cdot x \cdot dx + \int x^{-} dx$	

	x^2	1
	$\Rightarrow yx^2 = -x^2 \cos x + 2 \int x \cos x dx + \frac{x^4}{4} + C$	1
	$\Rightarrow yx^2 = -x^2\cos x + 2(x\sin x + \cos x) + \frac{x^4}{4} + C$	
	Which is the required solution	1
	OR	
	$2y e^{x/y} dx + (y - 2x e^{x/y}) dy = 0$	
34B	, , , , , , , , , , , , , , , , , , ,	
	$\Rightarrow \frac{dx}{dy} = \frac{2x e^{x/y} - y}{2x e^{x/y}} = \frac{2\frac{x}{y} e^{\frac{x}{y}} - 1}{2x e^{x/y}}$	
	It is a homogeneous differential equation.	1
		1
	Let $x = vy \Rightarrow \frac{dx}{dy} = v + y \frac{dv}{dy}$	1
	$v + y \frac{dv}{dy} = \frac{2ve^v - 1}{2e^v}$	
	$\Rightarrow y \frac{dv}{dv} = \frac{2ve^{v} - 1}{2e^{v}} - v = \frac{2ve^{v} - 1 - 2ve^{v}}{2e^{v}}$	
	$\Rightarrow y \frac{dy}{dy} = \frac{2e^{y}}{2e^{y}}$	
	$\Rightarrow 2e^{v} dv = -\frac{dy}{y}$	1
	$\int 2e^{v} dv = -\int \frac{dy}{y}$	
	$\Rightarrow 2e^{v} = -\log y + C$	
	$\Rightarrow 2e^{\frac{x}{y}} + \log y = C$	1
	When $x = 0$, $y = 1$, $C = 2$	
	Required solution $2e^{\frac{x}{y}} + \log y = 2$	
25	x-1 y-0 z+1	1
35	Let $\frac{x-1}{3} = \frac{y-0}{-1} = \frac{z+1}{0} = \lambda$ \Rightarrow Any point on it is $(3 \ \lambda + 1, -\lambda, -1)$	1/2
	For the point where $y = 1 \implies \lambda = -1$	1 1/2
	\Rightarrow The point is $(-2, 1, -1)$	1
	The directions of the two lines are $\vec{m} = 3\hat{\imath} - \hat{\jmath}$	1/2
	and $\vec{n} = -2\hat{\imath} + 2\hat{\jmath} + \hat{k}$,,,
	$\vec{m} \times \vec{n} = \begin{vmatrix} \hat{\imath} & \hat{\jmath} & \hat{k} \\ 3 & -1 & 0 \\ 2 & 2 & 1 \end{vmatrix} = -\hat{\imath} - 3\hat{\jmath} + 4\hat{k}$	1
	$\begin{bmatrix} & & & & & & & & & & & & & & & & & & &$	
	The equation of the required line is	
	$\vec{r} = (-2\hat{\imath} + \hat{\jmath} - \hat{k}) + \mu(-\hat{\imath} - 3\hat{\jmath} + 4\hat{k})$	1/2
	Alternative Solution:	
	Let $\frac{x-1}{3} = \frac{y-0}{-1} = \frac{z+1}{0} = \lambda \Rightarrow$ Any point on it is $(3 \lambda + 1, -\lambda, -1)$	1/2
	For the point where $y = 1 \implies \lambda = -1$	1
	\Rightarrow The point is $(-2, 1, -1)$	1/2
	Let the direction ratios of the required line be a, b, c	
	Then $3a - b = 0$	1
	-2a + 2b + c = 0	1
	Solving we get $\frac{a}{-1} = \frac{-b}{3} = \frac{c}{4} \Rightarrow \frac{a}{-1} = \frac{b}{-3} = \frac{c}{4}$	1
	The required line is $\frac{x+2}{-1} = \frac{y-1}{-3} = \frac{z+1}{4} = \mu$	1/2
	In vector form $\vec{r} = (-2\hat{\imath} + \hat{\jmath} - \hat{k}) + \mu(-\hat{\imath} - 3\hat{\jmath} + 4\hat{k})$	1/2
	1. (201) 1/4(1. 0) 1 110)	j

	SECTION- E	
26	(3 case-study/passage-based questions of 4 marks each)	
36	I. Traffic flow is not reflexive as $(A, A) \notin R$ (or no major spot is connected with itself)	1
	II. Traffic flow is not transitive as $(A, B) \in R$ and $(B, E) \in R$, but $(A, E) \notin R$	1
	III A. $R = \{(A, B), (A, C), (A, D), (B, C), (B, E), (C, E), (D, E), (D, C)\}$	1
	$Domain = \{A, B, C, D\}$	1/2 +
	$Range = \{B, C, D, E\}$	1/2
	OR	
	III B. No, the traffic flow doesn't represent a function as A has three images.	1+1
37	I. $P(x) = R(x) - C(x) = -0.3x^2 + 20x - (0.5x^2 - 10x + 150)$	
	$= -0.8x^2 + 30x - 150$ For critical points $P(x) = 0$ 1.6x + 30 = 0	1
	II. For critical points $P'(x) = 0 \Rightarrow -1.6x + 30 = 0$ $\Rightarrow x = \frac{30}{16} = \frac{300}{16} = 18.75$	1
	1.0 10	1
	III A. Now $P''(x) = -1.6$	1
	In particular $P''(18.75) = -1.6 < 0$ So, critical value $x = 18.75$ corresponds to a maximum profit.	1
	$\chi = 10.75$ corresponds to a maximum profit.	
	OR	
	III B. As x is the number of bulbs, so practically 18 bulbs correspond to a	1
	maximum profit.	1
	Maximum profit is $P(18) = -0.8 \times 18^2 + 30 \times 18 - 150$	1
	= -259.2 + 540 - 150 $= 540 - 409.2 = ₹130.80$	_
- 00		
38	Let the events be	
	E ₁ : the student is in the first group (time spent on screen is more than 4 hours) E ₂ : the student is in the second group (time spent on screen is 2 to 4 hours)	
	E ₃ : the student is in third group (time spent on screen is less than 2 hours)	
	A: the event of the student showing symptoms of anxiety and low retention	
	$P(E_1) = \frac{60}{100}$ $P(E_2) = \frac{30}{100}$ and $P(E_3) = \frac{10}{100}$	
	$P(A E_1) = \frac{80}{100}$ $P(A E_2) = \frac{70}{100}$ and $P(A E_3) = \frac{30}{100}$	
	I. $P(A)= P(E_1) \times P(A E_1) + P(E_2) \times P(A E_2) + P(E_3) \times P(A E_3)$	
	$= \frac{60}{100} \times \frac{80}{100} + \frac{30}{100} \times \frac{70}{100} + \frac{10}{100} \times \frac{30}{100} = \frac{72}{100} = 72\%$	2
	II. $P(E_1 A) = \frac{P(E_1 \cap A)}{P(A)}$	
		2
	$=\frac{\left(\frac{60}{100} \times \frac{80}{100}\right)}{\left(\frac{72}{100}\right)} = \frac{48}{72} = \frac{2}{3}$	