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Section _____

Roll No. _____

CRPF PUBLIC SCHOOL, ROHINI, DELHI
PRE-BOARD - 1 EXAMINATION (2024-25)
CLASS XII
MATHEMATICS (SET-A)

Time Allowed: 3 hours**Maximum Marks: 80****General Instructions:**

1. This Question paper contains - **five sections** A, B, C, D and E. Each section is compulsory. However, there are internal choices in some questions.
2. **Section A** has **18 MCQ's** and **02 Assertion Reasoning based questions** of 1 mark each.
3. **Section B** has **5 Very Short Answer (VSA)-type questions** of 2 marks each.
4. **Section C** has **6 Short Answer (SA)-type questions** of 3 marks each.
5. **Section D** has **4 Long Answer (LA)-type questions** of 5 marks each.
6. **Section E** has **3 source based/case based/passage based/integrated units of assessment** (4 marks each) with sub parts.

| SECTION – A (MCQ) 1 Mark Questions | |
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| Q1 | Let R be a relation in the set N given by $R = \{(a, b) : a = b - 2, b > 6\}$. Then (a) $(8, 7) \in R$ (b) $(6, 8) \in R$ (c) $(3, 8) \in R$ (d) $(2, 4) \in R$ |
| Q2 | If A is a square matrix of order 3 such that $ adj A = 144$, the value of $ A^T $ is: (a) 0 (b) 144 (c) ± 12 (d) 12 |
| Q3 | If $A = \begin{bmatrix} 0 & x+2 \\ 2x-3 & 0 \end{bmatrix}$ is a skew-symmetric matrix, then x is equal to: (a) $\frac{1}{3}$ (b) 5 (c) 3 (d) 1 |
| Q4 | The function $f(x) = \tan x - x$ (a) always increases (b) always decreases (c) never increases (d) sometimes increases and sometimes decreases |
| Q5 | If $A = \begin{bmatrix} 3 & 4 \\ 5 & 2 \end{bmatrix}$ and $2A + B$ is a null matrix, then B is equal to : (a) $\begin{bmatrix} 6 & 8 \\ 10 & 4 \end{bmatrix}$ (b) $\begin{bmatrix} -6 & -8 \\ -10 & -4 \end{bmatrix}$ (c) $\begin{bmatrix} 5 & 8 \\ 10 & 3 \end{bmatrix}$ (d) $\begin{bmatrix} -5 & -8 \\ -10 & -3 \end{bmatrix}$ |

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| Q6 | <p>If $A = \begin{bmatrix} x & 1 \\ 1 & 0 \end{bmatrix}$ and A^2 is the identity matrix, then x is equal to</p> <p>(a) 0 (b) 1 (c) 2 (d) -1</p> |
| Q7 | <p>Sum of order and degree of the differential equation $\left(\frac{d^2y}{dx^2}\right)^3 + \left(\frac{dy}{dx}\right)^5 + 4x = 0$ is</p> <p>(a) 6 (b) 3 (c) 4 (d) 5</p> |
| Q8 | <p>$\int_{-\pi/4}^{\pi/4} x^3 \cos^2 x \, dx$ is equal to</p> <p>(a) 0 (b) -1 (c) 1 (d) 2</p> |
| Q9 | <p>The greatest integer function defined by $f(x) = [x]$, $1 < x < 3$ is not differentiable at $x =$</p> <p>(a) 0 (b) 1 (c) 2 (d) $\frac{3}{2}$</p> |
| Q10 | <p>The solution of the differential equation $\frac{dx}{x} + \frac{dy}{y} = 0$ is :</p> <p>(a) $\frac{1}{x} + \frac{1}{y} = C$ (b) $\log x - \log y = C$</p> <p>(c) $xy = C$ (d) $x + y = C$</p> |
| Q11 | <p>The minimum value of $z = 3x + 8y$ subject to the constraints $x \leq 20$, $y \geq 10$ and $x \geq 0$, $y \geq 0$ is :</p> <p>(a) 80 (b) 140</p> <p>(c) 0 (d) 60</p> |
| Q12 | <p>Corner points of feasible region for an LPP are (0,2), (3,0), (6,0), (6,8) and (0,5). Let $F = 4x + 6y$ be the objective function. Minimum value of F occurs at</p> <p>(a) (0,2)</p> <p>(b) (3,0)</p> <p>(c) The mid-point of the line segment joining the points (0,2) and (3,0) only</p> <p>(d) Any point on the line segment joining the points (0,2) and (3,0)</p> |
| Q13 | <p>For the function $f(x) = x^3$, $x = 0$ is a point of</p> <p>(a) local maxima (b) local minima</p> <p>(c) non-differentiability (d) inflexion</p> |
| Q14 | <p>If $P(A \cap B) = \frac{1}{8}$ and $P(\bar{A}) = \frac{3}{4}$, then $P\left(\frac{B}{A}\right)$ is equal to :</p> <p>(a) $\frac{1}{2}$ (b) $\frac{1}{3}$</p> <p>(c) $\frac{1}{6}$ (d) $\frac{2}{3}$</p> |

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| Q15 | <p>If a vector makes an angle of $\frac{\pi}{4}$ with the positive directions of both x-axis and y-axis, then the angle which it makes with positive z-axis is :</p> <p>(a) $\frac{\pi}{4}$ (b) $\frac{3\pi}{4}$</p> <p>(c) $\frac{\pi}{2}$ (d) 0</p> |
| Q16 | <p>$\int 2^{x+2} dx$ is equal to :</p> <p>(a) $2^{x+2} + C$ (b) $2^{x+2} \log 2 + C$</p> <p>(c) $\frac{2^{x+2}}{\log 2} + C$ (d) $2 \cdot \frac{2^x}{\log 2} + C$</p> |
| Q17 | <p>$\int \frac{x+3}{(x+4)^2} e^x dx = ?$</p> <p>(a) $\frac{e^x}{x+4} + c$ (b) $\frac{e^x}{x+3} + c$ (c) $\frac{1}{(x+4)^2} + c$ (d) $\frac{e^x}{(x+4)^2} + c$</p> |
| Q18 | <p>Direction cosines of a line perpendicular to both x – axis and z – axis are</p> <p>(a) 1, 0, 1 (b) 1, 1, 1 (c) 0, 0, 1 (d) 0, 1, 0</p> |

Assertion Reasoning Based Questions

Given below are two statements: one is labelled as **Assertion A** and the other is labelled as **Reason R**.

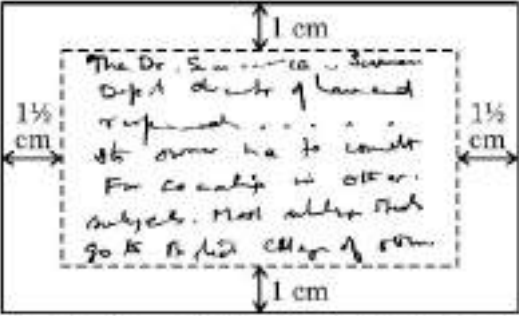
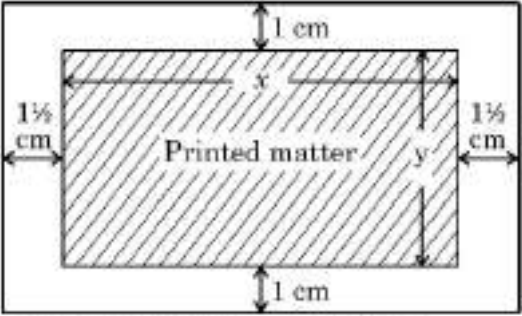

In the light of the above statements, choose the *most appropriate* answer from the options given below

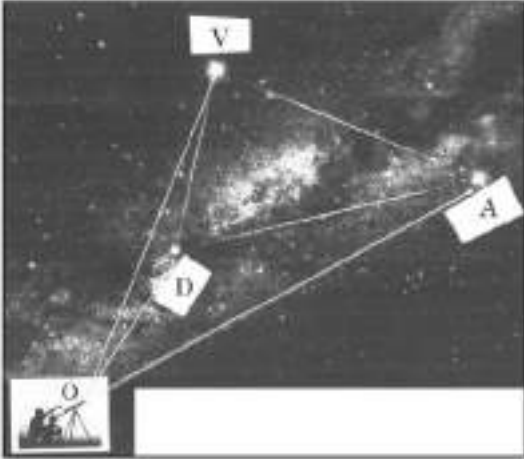
- Both **A** and **R** are correct and **R** is the correct explanation of **A**
- Both **A** and **R** are correct but **R** is **NOT** the correct explanation of **A**
- A** is correct but **R** is not correct
- A** is not correct but **R** is correct

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| Q19 | <p><i>Assertion (A) :</i> For matrix $A = \begin{bmatrix} 1 & \cos \theta & 1 \\ -\cos \theta & 1 & \cos \theta \\ -1 & -\cos \theta & 1 \end{bmatrix}$, where $\theta \in [0, 2\pi]$,</p> <p>$A \in [2, 4]$.</p> <p><i>Reason (R) :</i> $\cos \theta \in [-1, 1], \forall \theta \in [0, 2\pi]$.</p> |
| Q20 | <p><i>Assertion (A) :</i> A line through the points (4, 7, 8) and (2, 3, 4) is parallel to a line through the points (– 1, – 2, 1) and (1, 2, 5).</p> <p><i>Reason (R) :</i> Lines $\vec{r} = \vec{a}_1 + \lambda \vec{b}_1$ and $\vec{r} = \vec{a}_2 + \mu \vec{b}_2$ are parallel if $\vec{b}_1 \cdot \vec{b}_2 = 0$.</p> |

| SECTION – B (Very Short Answer (VSA)-type questions) 2 Marks Each | | | | | | | | | | | | | |
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| Q21 | Evaluate $\sin^{-1}\left(\sin \frac{3\pi}{4}\right) + \cos^{-1}(\cos \pi) + \tan^{-1}(1)$. OR Evaluate the following: $\sin\left(\frac{\pi}{6} - \sin^{-1}\left(-\frac{\sqrt{3}}{2}\right)\right)$ | | | | | | | | | | | | |
| Q22 | If $\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}$, $\vec{b} = 2\hat{i} + 4\hat{j} - 5\hat{k}$ represents two adjacent sides of a parallelogram, find a unit vectors parallel to the diagonal of the parallelogram. | | | | | | | | | | | | |
| Q23 | The area of the circle is increasing at a uniform rate of $2 \text{ cm}^2/\text{sec}$. How fast is the circumference of the circle increasing when the radius $r = 5 \text{ cm}$? OR Show that the function f given by $f(x) = \sin x + \cos x$, is strictly decreasing in the interval $\left(\frac{\pi}{4}, \frac{5\pi}{4}\right)$. | | | | | | | | | | | | |
| Q24 | Show that the function $f(x) = 4x^3 - 18x^2 + 27x - 7$ has neither maxima nor minima. | | | | | | | | | | | | |
| Q25 | If $y = (\sin^{-1}x)^2$, then find $(1 - x^2)\frac{d^2y}{dx^2} - x\frac{dy}{dx}$. | | | | | | | | | | | | |
| SECTION – C (Short Answer (SA)-type questions) 3 Marks Each | | | | | | | | | | | | | |
| Q26 | Solve the following L.P.P. graphically : Maximise $Z = 60x + 40y$ Subject to $x + 2y \leq 12$ $2x + y \leq 12$ $4x + 5y \geq 20$ $x, y \geq 0$ | | | | | | | | | | | | |
| Q27 | Two balls are drawn at random one by one with replacement from an urn containing equal number of red balls and green balls. Find the probability distribution of number of red balls. Also, find the mean of the random variable. OR The random variable X has the following probability distribution where a and b are some constants : <table border="1"><tr><td>X</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>P(X)</td><td>0.2</td><td>a</td><td>a</td><td>0.2</td><td>b</td></tr></table> If the mean $E(X) = 3$, then find values of a and b and hence determine $P(X \geq 3)$. | X | 1 | 2 | 3 | 4 | 5 | P(X) | 0.2 | a | a | 0.2 | b |
| X | 1 | 2 | 3 | 4 | 5 | | | | | | | | |
| P(X) | 0.2 | a | a | 0.2 | b | | | | | | | | |

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| Q28 | <p>Find : $\int \frac{2x}{(x^2 + 1)(x^2 - 4)} dx$.</p> <p style="text-align: center;">OR</p> <p>Evaluate : $\int \frac{2x + 1}{\sqrt{3 + 2x - x^2}} dx$</p> |
| Q29 | <p>Find the general solution of the differential equation :</p> $(x^2 + 1) \frac{dy}{dx} + 2xy = \sqrt{x^2 + 4}$ <p style="text-align: center;">OR</p> <p>Find the particular solution of the differential equation</p> $(xe^x + y) dx = x dy, \text{ given that } y = 1 \text{ when } x = 1.$ |
| Q30 | <p>Find the area of the region bounded by the lines $x - 2y = 4$, $x = -1$, $x = 6$ and x-axis, using integration.</p> |
| Q31 | <p>Differentiate the following function with respect to x</p> $y = (\sin x)^x + \sin^{-1} \sqrt{x}$ |
| SECTION – D (Long Answer (LA)-type questions) 5 Marks Each | |
| Q32 | <p>Find the inverse of matrix $A = \begin{bmatrix} 2 & 3 & 4 \\ 3 & -2 & 2 \\ 4 & 2 & -3 \end{bmatrix}$</p> <p>Hence solve the given system of equations:</p> $2x + 3y + 4z = 17, \quad 3x - 2y + 2z = 11, \quad 4x + 2y - 3z = 8.$ |
| Q33 | <p>Find the shortest distance between the lines whose vector equations are :</p> $\vec{r} = \hat{i} + 2\hat{j} - 4\hat{k} + \lambda(2\hat{i} + 3\hat{j} + 6\hat{k}) \text{ and}$ $\vec{r} = 3\hat{i} - 3\hat{j} - 5\hat{k} + \mu(-2\hat{i} + 3\hat{j} + 8\hat{k})$ <p style="text-align: center;">OR</p> <p>Find the co-ordinates of the foot of the perpendicular drawn from the point $(2, 3, -8)$ to the line $\frac{4-x}{2} = \frac{y}{6} = \frac{1-z}{3}$.</p> <p>Also, find the perpendicular distance of the given point from the line.</p> |

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| Q34 | <p>Evaluate : $\int_{-5}^0 (x + x+2 + x+5) dx$</p> <p style="text-align: center;">OR</p> <p>Evaluate : $\int_0^{\frac{\pi}{2}} \sin 2x \tan^{-1}(\sin x) dx$</p> |
| Q35 | <p>Let $f : \mathbb{R} - \left\{-\frac{4}{3}\right\} \rightarrow \mathbb{R}$ be a function defined as $f(x) = \frac{4x}{3x+4}$. Show that f is a one-one function. Also, check whether f is an onto function or not.</p> |
| SECTION – E (Case Study Based Questions) 4 Marks Each | |
| Q36 | <p>A rectangular visiting card is to contain 24 sq.cm. of printed matter. The margins at the top and bottom of the card are to be 1 cm and the margins on the left and right are to be $1\frac{1}{2}$ cm as shown below :</p> <div style="display: flex; justify-content: space-around; align-items: center;">   </div> <p>On the basis of the above information, answer the following questions :</p> <ol style="list-style-type: none"> Write the expression for the area of the visiting card in terms of x. Obtain the dimensions of the card of minimum area. |
| Q37 | <p>A shopkeeper sells three types of flower seeds A1, A2, A3. They are sold in the form of a mixture, where the proportions of these seeds are 4:4:2 respectively. The germination rates of three types of seeds are 45%, 60%, and 35% respectively.</p> <div style="text-align: center;">  </div> |

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| | <p>Based on the above information:</p> <p>(a) Calculate the probability that a randomly chosen seed will germinate.</p> <p>(b) Calculate the probability that the seed is of type A2, given that a randomly chosen seed germinates.</p> |
| Q38 | <p>An instructor at the astronomical centre shows three among the brightest stars in a particular constellation. Assume that the telescope is located at $O(0, 0, 0)$ and the three stars have their locations at the points D, A and V having position vectors $2\hat{i} + 3\hat{j} + 4\hat{k}$, $7\hat{i} + 5\hat{j} + 8\hat{k}$ and $-3\hat{i} + 7\hat{j} + 11\hat{k}$ respectively.</p>  <p>Based on the above information, answer the following questions :</p> <p>(i) How far is the star V from star A ? 1</p> <p>(ii) Find a unit vector in the direction of \vec{DA} . 1</p> <p>(iii) Find the measure of $\angle VDA$. 2</p> <p style="text-align: center;">OR</p> <p>(iii) What is the projection of vector \vec{DV} on vector \vec{DA} ? 2</p> |