

CHENNAI SAHODAYA SCHOOLS COMPLEX

(General Instructions)

- This question paper contains 9 printed pages.
- ❖ This question paper contains 38 questions.
- ❖ Write down the question number before attempting.
- ❖ An additional reading time of 15 minutes.
- ❖ This question paper contains 5 sections A, B, C, D and E.
- Each section is compulsory. However there are internal choices in some questions.
- ❖ Section A has 18 MCQ's and 2 Assertion-Reason based questions of 1 mark each.
- ❖ Section B has 5 Very Short Answer (VSA)-type questions of 2 marks each.
- ❖ Section C has 6 Short Answer (SA)-type questions of 3 marks each.
- ❖ Section D has 4 Long Answer (LA)-type questions of 5 marks each.
- ❖ Section E has 3 case based questions of 4 marks each.

COMMON EXAMINATION Class –12

(MATHEMATICS-041/SET-1)

Time Allowed: 3 hours Maximum Marks: 80

Roll No: Date:

SECTION - A

(In this section there are 18 MCQ's and 2 Assertion-Reason based questions of 1 mark each)

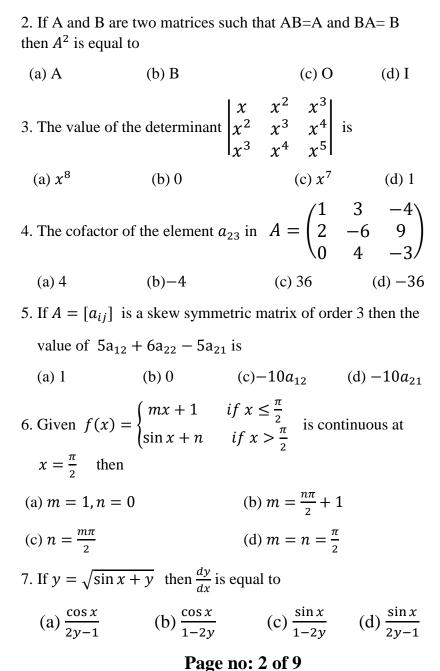
1. Given a matrix $A = \begin{pmatrix} x & y \\ z & t \end{pmatrix}$ then the value of $|4AA^{-1}|$ is

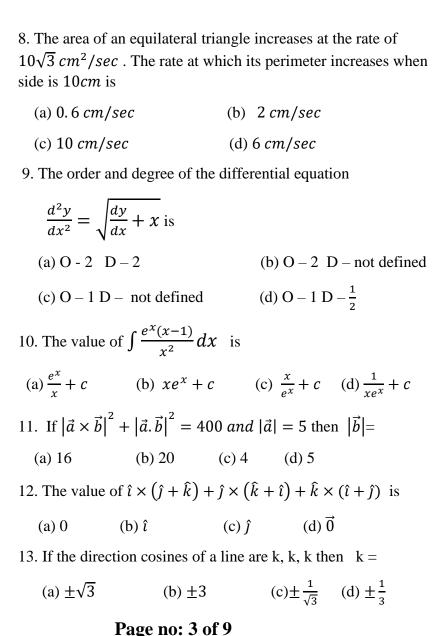
(a) 4

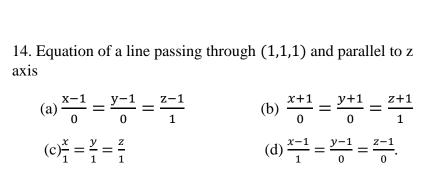
(b) 4(xt - yz)

(c) 0

(d) 16







15. The angle between the vectors $(\hat{\imath} - \hat{\jmath})$ and $(\hat{\jmath} - \hat{k})$ is

16. The value of
$$\cos\{\cos^{-1}\left(-\frac{\sqrt{3}}{2}\right) + \frac{\pi}{6}\}$$
(a) $-\frac{\pi}{3}$ (b) -1 (c) 0 (d) 1

(a) $\frac{2\pi}{3}$ (b) $\frac{\pi}{3}$ (c) $\frac{\pi}{4}$

17. If A and B are any two events having $P(A \cup B) = \frac{2}{3}$ and

$$P(\overline{B}) = \frac{1}{2} \text{ then } P(A \cap \overline{B}) \text{ is}$$

$$(a) \frac{1}{2} \qquad (b) \frac{2}{3} \qquad (c) \frac{1}{6} \qquad (d) \frac{1}{3}$$

18. E and F are mutually exclusive and exhaustive events. The odds against the event E is 2:3 then odds in favour of F is

These type of questions consist of two statements.

Statement I is called Assertion (A) and statement II is called Reason (R) Choose the correct answer out of the following choices

- (a) Both A and R are true and R is the correct explanation of A
- (b) Both A and R are true and R is not correct explanation of A

Page no: 4 of 9

- (c) A is true but R is false
- (d) **A** is false but **R** is true.
- 19. **Assertion (A):** The corner points of the feasible region for an L.P.P. are (0,0), (0,40), (30,20) and (60,0). The objective function Z = x + y has maximum value at (60,0).

Reason (**R**): If the feasible region for an L.P.P. is bounded then the objective function Z = ax + by has both minimum and maximum values.

20. **Assertion** (A): The modulus function f(x) = |x| is differentiable for all $x \in R$

Reason (\mathbf{R}): A function f(x) is said to be differentiable if it is differentiable at every point on its domain.

SECTION - B

(This section comprises of VSA questions of 2 marks each.)

- 21. Write $\tan^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right)$, $x \neq 0$ in its simplest form. **(OR)** Given set $A = \{1,2,3\}$. R_1 and R_2 are relations on A given by $R_1 = \{(1,1), (1,2), (1,3), (2,2), (3,3)\}$ and $R_2 = \{(1,1), (2,2), (1,3), (3,1)\}$ Determine whether R_1 and R_2 are reflexive, symmetric and transitive.
- 22. Prove that the function $f(x) = x^3 6x^2 + 12x 18$ is increasing on R
- 23. Solve the differential equation $y \log y \, dx x \, dy = 0$ (OR) Solve the differential equation $y - \frac{dy}{dx} + \frac{y}{x} = 0$

Page no: 5 of 9

24. Find the shortest distance between the lines

$$\vec{r} = \hat{\imath} + 2\hat{\jmath} - 4\hat{k} + \lambda(2\hat{\imath} + 3\hat{\jmath} + 6\hat{k})$$
 and $\vec{r} = 3\hat{\imath} + 3\hat{\jmath} - 5\hat{k} + \mu(2\hat{\imath} + 3\hat{\jmath} + 6\hat{k})$

25. Find the value of λ when scalar projection of

$$\vec{a} = \lambda \hat{\imath} + \hat{\jmath} + 4\hat{k}$$
 on $\vec{b} = 2\hat{\imath} + 6\hat{\jmath} + 3\hat{k}$ is 4 units.

SECTION - C

(This section comprises of SA questions of 3 marks each.)

- 26. A circular blot of ink in a blotting paper increases in area in such a way that the radius r cm at time 't' seconds is given by $r = 2t^2 \frac{t^3}{4}$. Find the rate of increase of area when t=2
- 27. Bag I contains 4 white and 2 black balls. Bag II contains 3 white and 5 black balls. One ball is transferred from Bag I to Bag II and then a ball is drawn from bag II. The ball so drawn is found to be black in colour. Find the probability that the transferred ball is black.
- 28. Two cards are drawn successively without replacement from a well shuffled pack of 52. Find the probability distribution of the number of kings. Also find its mean.
- 29. Evaluate $\int \frac{x^2}{x^4 x^2 12} dx$ (**OR**) Evaluate: $\int \frac{x+7}{3x^2 + 25x + 28} dx$
- 30. Evaluate: $\int_2^5 (|x-1| + |x-3|) dx$ (**OR**) $\int_2^3 \frac{dx}{x(x^3-1)}$
- 31. Solve the differential equation $(3x^2 + y)\frac{dx}{dy} = x$, x > 0

when
$$x = 1, y = 1$$

Page no:6 of 9

SECTION - D

(This section comprises of LA questions of 5 marks each.)

32. On the set of integers Z consider the relation

 $R = \{(a, b): (a - b) \text{ is divisible by 5} \}$.Show that R is an equivalence relation on Z .Write the equivalence class of 4.

(OR)

The function $f: N \to N$, defined by

$$f(x) = \begin{cases} x+1 & \text{if } x \text{ is odd} \\ x-1 & \text{if } x \text{ is even} \end{cases}$$

Show that the function f is both one-one and onto.

33. A diet is to contain 30 units of vitamin A, 40 units of vitamin B and 20 units of vitamin C. Three types of foods F1, F2 and F3 are available. One unit of Food F1 contain 3 units of vitamin A, 2 units of vitamin B and 1 unit of vitamin C. One unit of food F2 contains 1 unit of vitamin A, 2 units of vitamin B and 1 unit of vitamin C. One unit of food F3 contains 5 units of vitamin A, 3 units of vitamin B and 2 units of vitamin C.

If the diet contains x units of food F1, y units of food F2 and z units of Food F3, find the values of x, y and z using matrix method.

Page no: 7 of 9

34. Using integration find the area bounded by the curve

$$y^2 = x$$
 and $x = 2y + 3$ in the second quadrant and x axis. (OR)

Using integration find the area of the region

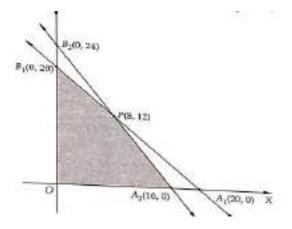
$$\{(x, y): x^2 + y^2 \le 4, x \ge -1, x + y \le 2, y \ge 0\}$$

35. Find the foot of the perpendicular and image of the point P(1,6,3) with respect to line $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$. Also find the equation of the perpendicular to the line from P.

SECTION - E

(This section contains 3 case study questions 4 marks each)

36. The feasible region for an L.P.P is shown in the figure;



- (i) Write all the constraints representing the feasible region.in the above L.P.P. (2 marks)
- (ii) Find the point at which the maximum value of the objective function z = 10x + 5y occurs. (2 marks)

Page no:8 of 9

37. A cable network provider in a small town has 500 subscribers and he used to collect ₹300 per month from each subscriber. He proposes to increase the monthly charges and it is believed from the past experience that for every increase of ₹1 one subscriber will discontinue the service. If ₹x is the monthly increase in subscription amount then find the

(i) the number of subscribers

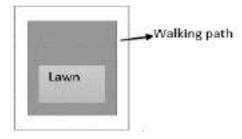
(1 mark)

(ii) revenue function.

(1 mark)

- (iii) maximum revenue using first derivative test (OR)
- (iii) maximum revenue using second derivative test. (2 marks)
- 38. A gardener wants to develop a rectangular lawn with an area $800m^2$. He also wants to construct a walking path of width 1m surrounding the lawn.

(Refer figure)



If the length of the lawn is 'x' metres then

- (i) find the area of the walking path
- (1 mark)
- (ii) If the cost of developing lawn is ₹50 per sq.m. and cost of constructing walking path is ₹100 per sq.m. then find the total cost function. (1 mark)
- (iii) Find 'x' at the least construction cost. (2 marks)

"End of paper"