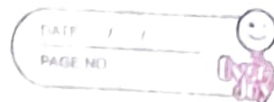


27th November 2025

PBMT-04



Syllabus: Trigonometry and Applications of Trigonometry.

Section-A

① 1. (option-d)

② $\frac{1}{2}$ (option-b)

③ $\sin \theta + \sin^2 \theta = 1$
 $\Rightarrow \sin \theta = 1 - \sin^2 \theta$
 $\Rightarrow \sin \theta = \cos^2 \theta$

Now, $\cos^2 \theta + \cos^4 \theta$
 $\Rightarrow \cos^2 \theta (1 + \cos^2 \theta)$

$\Rightarrow \sin \theta (1 + \sin \theta)$ [$\because \sin \theta = \cos^2 \theta$]
 $= \sin \theta + \sin^2 \theta = 1$.

ans: 1 (option-b)

④ $\frac{1}{2}$ (option-c).

⑤ 16 (option-a).

⑥ 30. (option-a).

⑦ 1 (option-a).

⑧ 10. (option-d).

⑨ 2 (option-a).



- (10) Both (A) and (R) are true and (R) is the correct explanation of (A) [option-a].

Section-B

(11) $x = \frac{\operatorname{cosec} \theta}{2}$

$$\Rightarrow x^2 = \frac{\operatorname{cosec}^2 \theta}{4} \quad \text{--- (1)}$$

$$\cot \theta = \frac{2}{x} \quad [\text{given}].$$

$$\Rightarrow x = \frac{2}{\cot \theta}$$

$$\Rightarrow x^2 = \frac{4}{\cot^2 \theta}$$

$$\Rightarrow \frac{1}{x^2} = \frac{\cot^2 \theta}{4} \quad \text{--- (2)}$$

To find $2 \left(x^2 - \frac{1}{x^2} \right)$

$$2 \left(\frac{\operatorname{cosec}^2 \theta}{4} - \frac{\cot^2 \theta}{4} \right) \quad [\text{putting 1 \& 2}].$$

$$2 \left(\frac{\operatorname{cosec}^2 \theta - \cot^2 \theta}{4} \right) = \frac{1}{2}$$

$$\therefore 2 \left(x^2 - \frac{1}{x^2} \right) = \frac{1}{2}$$

$$Q. 12(A) \quad \sin A + \cos A = \sqrt{2}$$

Sq.

$$\sin^2 A + \cos^2 A + 2\sin A \cos A = 2$$

$$2\sin A \cos A = 2 - 1$$

$$\sin A \cos A = \frac{1}{2}$$

Now, $\frac{\sin A + \cos A}{\sin A \cos A}$

$$\frac{\sin^2 A + \cos^2 A}{\sin A \cos A} = \frac{1}{\sin A \cos A} = 2$$

(12)

$$(B) \tan(A+B) = \sqrt{3}$$

$$\Rightarrow \tan(A+B) = \tan 60^\circ$$

$$\Rightarrow A+B = 60^\circ \quad \text{--- (1)}$$

$$\tan(A-B) = \frac{1}{\sqrt{3}}$$

$$\tan(A-B) = \tan 30^\circ$$

$$A-B = 30^\circ \quad \text{--- (2)}$$

Eliminating (1) and (2)

$$\begin{array}{r} A+B=60^\circ \\ A+B=30^\circ \\ \hline (-) \quad (-) \quad (-) \end{array}$$

$$A+B=60^\circ$$

$$A-B=30^\circ$$

$$2A=90^\circ$$

$$A=45^\circ$$

$$\text{putting } A=45^\circ \text{ in (1)}$$

$$B=15^\circ$$

$$\therefore A=45^\circ \text{ and } B=15^\circ$$

(13)

$$1 + \sin^2 \theta = 3 \sin \theta \cos \theta$$

divide both sides by $\cos^2 \theta$

$$\frac{1}{\cos^2 \theta} + \frac{\sin^2 \theta}{\cos^2 \theta} = \frac{3 \sin \theta \cos \theta}{\cos^2 \theta}$$

$$\Rightarrow \sec^2 \theta + \tan^2 \theta = 3 \tan \theta$$

$$\Rightarrow 1 + \tan^2 \theta + \tan^2 \theta - 3 \tan \theta = 0$$

$$\Rightarrow 2 \tan^2 \theta - 3 \tan \theta + 1 = 0$$

$$\Rightarrow 2 \tan^2 \theta - 2 \tan \theta - \tan \theta + 1 = 0$$

$$\Rightarrow 2 \tan \theta (\tan \theta - 1) - 1(\tan \theta - 1) = 0$$

$$\Rightarrow (2 \tan \theta - 1)(\tan \theta - 1) = 0$$

$$\Rightarrow \tan \theta = \frac{1}{2} \text{ or } \tan \theta = 1. \text{ Hence, proved.}$$

Section-C

$$(14) \quad \frac{(\sec A - \tan A)^2 + 1}{\sec A - \tan A} = 2 \sec A$$

L.H.S $\frac{(\sec A - \tan A)^2 + 1}{\sec A - \tan A} \times \frac{\sec A + \tan A}{\sec A + \tan A}$

$$\frac{\sec^2 A - \tan^2 A + 1}{\sec A - \tan A} \times \frac{\sec A + \tan A}{\sec A + \tan A}$$

$$\frac{\sec^2 A - \tan^2 A + 1}{\sec A - \tan A}$$

$$\frac{(\sec A - \tan A) + \sec A + \tan A}{\sec A - \tan A}$$

$$\frac{\sec A - \tan A + \sec A + \tan A}{\sec A - \tan A}$$

$$2 \sec A$$

15. (A) $(\operatorname{cosec} A - \sin A)(\sec A - \cos A) = \frac{1}{\tan A + \cot A}$

L.H.S.

$$\left(\frac{1}{\sin A} - \sin A \right) \left(\frac{1}{\cos A} - \cos A \right)$$

$$\Rightarrow \left(\frac{1 - \sin^2 A}{\sin A} \right) \left(\frac{1 - \cos^2 A}{\cos A} \right)$$

$$\Rightarrow \frac{\cos^2 A}{\sin A} \times \frac{\sin^2 A}{\cos A}$$

$$\Rightarrow \cos A \sin A$$

R.H.S.

$$\frac{1}{\tan A + \cot A}$$

$$\Rightarrow \frac{1}{\frac{\sin A}{\cos A} + \frac{\cos A}{\sin A}}$$

$$\Rightarrow \frac{1}{\frac{\sin^2 A + \cos^2 A}{\cos A \sin A}}$$

$$\Rightarrow \cos A \sin A$$

$$\therefore \text{L.H.S.} = \text{R.H.S.}$$

Hence, proved.

$$(B) \frac{\sin \theta}{\cot \theta + \operatorname{cosec} \theta} = 2 + \frac{\sin \theta}{\cot \theta - \operatorname{cosec} \theta}$$

L.H.S

$$\rightarrow \frac{\sin \theta}{\frac{\cos \theta}{\sin \theta} + \frac{1}{\sin \theta}}$$

$$\Rightarrow \frac{\sin^2 \theta}{\cos \theta + 1}$$

$$\Rightarrow \frac{1 - \cos^2 \theta}{\cos \theta + 1}$$

$$\Rightarrow \frac{(1 + \cancel{\cos \theta})(1 - \cancel{\cos \theta})}{\cancel{\cos \theta} + 1}$$

$$\Rightarrow 1 - \cos \theta$$

R.H.S

$$\rightarrow 2 + \frac{\sin \theta}{\frac{\cos \theta}{\sin \theta} - \frac{1}{\sin \theta}}$$

$$\Rightarrow 2 + \frac{\sin^2 \theta}{\cos \theta - 1}$$

$$\Rightarrow 2 + \frac{1 - \cos^2 \theta}{\cos \theta - 1}$$

$$\Rightarrow 2 + \frac{(1 - \cancel{\cos \theta})(1 + \cancel{\cos \theta})}{\cancel{\cos \theta} - 1}$$

$$\Rightarrow 1 + \cos \theta = -2$$

$$\Rightarrow \cos \theta = -1$$



Section-D

$$\Rightarrow 2 + \frac{(1 - \cos \theta)(1 + \cos \theta)}{-(1 - \cos \theta)}$$

$$\Rightarrow \frac{1 + \cos \theta}{-1} + 2 \Rightarrow -1 - \cos \theta + 2 \Rightarrow 1 - \cos \theta$$

$\therefore L.H.S = R.H.S$
Hence, proved.

Section-D

16. $BC = d =$ distance b/w building & tower.

16. $AB = 60m =$ height of building.

$DE = h =$ height of tower.

$x =$ difference b/w heights

In $\triangle ABC$,

$$\tan 60^\circ = \frac{P}{B}$$

$$\sqrt{3} = \frac{d}{60}$$

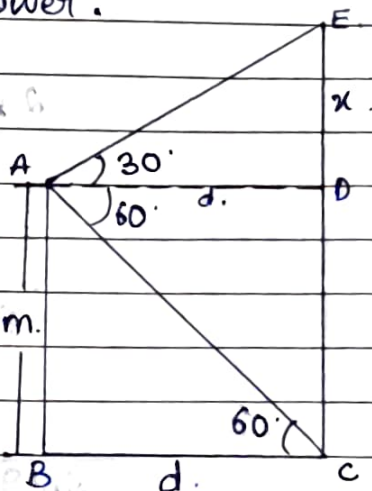
$$d = 60 \times \sqrt{3}$$

$$d = 60 \times 1.732$$

$$d = 103.928$$

$$d = \frac{60 \times \sqrt{3}}{\sqrt{3}}$$

$$d = 20\sqrt{3}m. = 20 \times 1.732 = 34.640$$





In $\triangle ADE$,

$$\tan 30^\circ = \frac{d'}{x} \quad \frac{x}{d}$$

$$\frac{1}{\sqrt{3}} = \frac{x}{20\sqrt{3}}$$

$$x = 20m$$

$\therefore$ Difference between heights of building is 40m & distance b/w them is 34.64m.

$$(17) (A) \frac{\sin \theta + \cos \theta}{\sin \theta - \cos \theta} + \frac{\sin \theta - \cos \theta}{\sin \theta + \cos \theta} = \frac{2}{\sin^2 \theta - 1}$$

$$\frac{(\sin \theta + \cos \theta)^2 + (\sin \theta - \cos \theta)^2}{\sin^2 \theta - \cos^2 \theta}$$

$$\frac{\sin^2 \theta + 2\sin \theta \cos \theta + \cos^2 \theta + \sin^2 \theta - 2\cos \theta \sin \theta + \cos^2 \theta}{\sin^2 \theta - \cos^2 \theta}$$

$$\frac{2\sin^2 \theta + 2\cos^2 \theta}{\sin^2 \theta - \cos^2 \theta}$$

$$\frac{2(1)}{\sin^2 \theta - \cos^2 \theta}$$

$$\frac{2}{\sin^2 \theta - (1 - \sin^2 \theta)}$$

$$\frac{2}{\sin^2 \theta + \sin^2 \theta} \Rightarrow \frac{2}{2\sin^2 \theta - 1}$$

$\therefore L.H.S = R.H.S$
Hence proved.



(OR) (B.) $\left(1 + \frac{1}{\tan^2 A}\right) \left(1 + \frac{1}{\cot^2 A}\right) = \frac{1}{\cos^2 A} - \cos^2 A$

L.H.S

$$\left(1 + \frac{1}{\tan^2 A}\right) \left(1 + \frac{1}{\cot^2 A}\right)$$

$$\left(\frac{\tan^2 A + 1}{\tan^2 A}\right) \left(\frac{\cot^2 A + 1}{\cot^2 A}\right)$$

$$\left(\frac{\sec^2 A}{\tan^2 A}\right) \left(\frac{\operatorname{cosec}^2 A}{\cot^2 A}\right)$$

$$\frac{1}{\cos^2 A} \times \frac{\cos^2 A}{\sin^2 A} \times \frac{1}{\sin^2 A} \times \frac{\sin^2 A}{\cos^2 A}$$

R.H.S

$$\frac{1}{\cos^2 A \times \sin^2 A}$$

$$\frac{1}{\cos^2 A - \cos^4 A}$$

$$\frac{1}{\cos^2 A (1 - \cos^2 A)}$$

$$\frac{1}{\cos^2 A \times \sin^2 A}$$

$$\therefore \text{L.H.S} = \text{R.H.S}$$

Hence, proved

ertion.

Section E

(18) (i) $\tan \theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{15}{15} = 1$

$\therefore$ angle is 45°

(ii) $x^2 = 15^2 + 15^2$
 $= 225 + 225$
 $= 450$

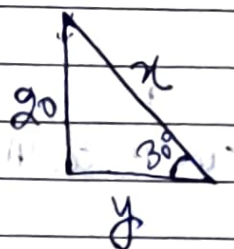
$\therefore x = 15\sqrt{2} \text{ ft}$

(iii) (a) $\sin 60^\circ = \frac{h}{20}$

$\frac{\sqrt{3}}{2} \times 20 = h$

$\therefore h = 10\sqrt{3} \text{ ft}$

(OR) (b) $\sin 30^\circ = \frac{20}{x}$



$\frac{1}{2} = \frac{20}{x}$

$x = 40 \text{ feet}$

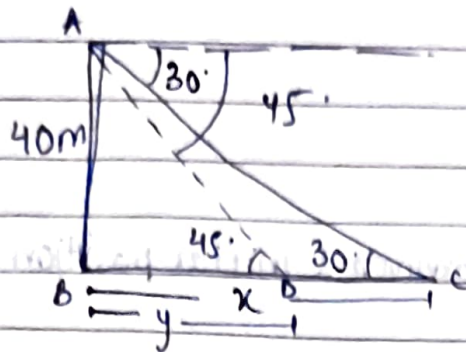
$\cos 30^\circ = \frac{y}{x}$

$\frac{\sqrt{3}}{2} = \frac{y}{40}$

$20\sqrt{3} \text{ feet} = y$



19. i.



ii. a. In $\triangle ABD$,

$$\tan 45^\circ = \frac{AB}{BD}$$

$$1 = \frac{40}{BD}$$

$$BD = 40\text{m.}$$

In $\triangle ABC$,

$$\tan 30^\circ = \frac{AB}{BC}$$

$$\frac{1}{\sqrt{3}} = \frac{40}{BC}$$

$$BC = 40\sqrt{3}\text{m.}$$

$$\therefore \text{distance} = 40\sqrt{3} - 40$$

$$= 40(\sqrt{3} - 1)$$

$$= 40(1.73 - 1)$$

$$= 40 \times 0.73$$

$$CD = 29.2\text{m.}$$

$$\textcircled{b} \quad \sin 30^\circ = \frac{AB}{AC}$$

$$\frac{1}{2} = \frac{40}{AC}$$

$$AC = 80 \text{ m}$$

$\therefore$ distance b/w observer & initial position of ship is 80m

$$\textcircled{iii} \quad \text{speed} = \frac{\text{distance}}{\text{time}}$$

$$= \frac{80}{8}$$

$$= \frac{29.2}{8}$$

$$= 3.65 \text{ m/s}$$

$$3.65 \times \frac{18}{5}$$

$$3.65 \times 3.6$$

$$\therefore \text{speed} = 13.14 \text{ km/h}$$