PRE BOARD EXAM - II (2025-26)

Class 10 - Mathematics

Section A

1.

(b) 0

Explanation:

$$1080=2^3\times 3^3\times 5$$

On comparing

$$x = 3, y = 3$$

$$x - y = 3 - 3 = 0$$

2.

(d)
$$-\frac{3}{4}$$
, $\frac{3}{4}$
Explanation:

$$16x^2 - 9 = 0$$

$$(4x - 3)(4x + 3) = 0$$

$$\therefore x = \pm \frac{3}{4}$$

(a) $10x^2 - x - 3$ 3.

Explanation:

$$\alpha+\beta=\left(\frac{3}{5}-\frac{1}{2}\right)=\frac{1}{10}, \alpha\beta=\frac{3}{5}\times\left(\frac{-1}{2}\right)=\frac{-3}{10}$$
 Required polynomial is $x^2-\frac{1}{10}x-\frac{3}{10}$, i.e., $10x^2-x-3$

(a) 18 sq. units 4.

Explanation:

The triangle formed by the lines y = x, x = 6 and y = 0 is shaded.

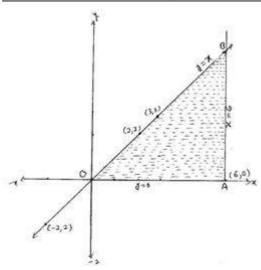
The area of the shaded region, i.e., x = y

We got a right-angled triangle with base 6 units and height 6 units

Triangle OAB =
$$\frac{1}{2}$$
 × OA × AB

Hence the area of triangle = $\frac{1}{2} \times 6 \times 6 = 18$ sq.units

x	2	-2	3
y	2	-2	3



- 5.
- **(b)** $\frac{b^2}{4a}$

Explanation:

Since the roots are equal, we have D = 0

$$\therefore b^2 - 4ac = 0 \Rightarrow 4ac = b^2 \Rightarrow c = \frac{b^2}{4a} .$$

- 6.
- **(d)** n²

Explanation:

1, 3, 5, 7, are n odd numbers

Where
$$a = 1$$
, and $d = 2$

$$\therefore S_n = rac{n}{2}[2a + (n-1)d]$$

$$=\frac{n}{2}[2 \times 1 + (n-1) \times 2]$$

$$= \frac{n}{2}[2 \times 1 + (n-1) \times 2]$$

$$\frac{n}{2}[2 + 2n - 2] = \frac{n}{2} \times 2n$$

- $= n^2$
- 7.
- **(b)** 5

Explanation:

$$a_n = 5n - 1$$

$$a_4 = 5(1) - 1$$

$$a_2 = 5(2) - 1$$

∴
$$d = a_2 - a_4$$

- 8.
- (d) $\angle B = \angle P$

Explanation:

$$\angle B = \angle P$$

- 9.
- (d) 5 units

Explanation:

$$AB = \sqrt{(2+1)^2 + (-1+5)^2}$$

$$=\sqrt{3^2+4^2}$$

$$=\sqrt{9+16}$$

$$=\sqrt{25}$$

$$AB = 5$$
 units

- 10.
- **(d)** 20°

Explanation:

$$2\cos 3 heta=1\Rightarrow\cos 3 heta=rac{1}{2}=\cos 60^\circ \ \ \Rightarrow 3 heta=60^\circ \Rightarrow heta=20^\circ$$

11.

(d)
$$\frac{60}{\pi}$$
 cm

Explanation:

Given: Length of arc = 20 cm

$$\Rightarrow \frac{60^{\circ}}{360^{\circ}} \times 2\pi r = 20$$

$$\Rightarrow \frac{60^{\circ}}{360^{\circ}} \times 2\pi r = 20$$

$$\Rightarrow \frac{\pi r}{3} = 20$$

$$\Rightarrow \frac{\pi r}{3} = 20$$

$$\Rightarrow r\left(\frac{\pi}{3}\right) = 20$$

$$\Rightarrow r\left(\frac{\pi}{3}\right) = 20$$

$$\Rightarrow r = \frac{60}{\pi} \text{ cm}$$

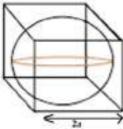
$$\Rightarrow r\left(\frac{\pi}{3}\right) = 20$$

$$\Rightarrow$$
 r = $\frac{60}{\pi}$ cm

12.

(d)
$$\frac{4}{3}\pi a^3$$

Explanation:



: Spherical ball is inside the cubical box.

∴ diameter = 2a.

radius = a

Volume of sphere = $\frac{4}{3}\pi r^3$ Volume of sphere = $\frac{4}{3}\pi r^3$ cubic units.

13.

(c) mode

Explanation:

The most frequent value in the data is known as the Mode. e.g let us consider the following data set: 3,5,7,5,9,5,8,4 the mode is 5 since it occurs most often in data set.

14. (a) \overline{x} + a

Let terms be x_1 , x_2 , x_3 , ..., x_n

$$\therefore \text{ Mean } (\overline{x}) = \frac{x_1 + x_2 + x_3 + \dots + x_n}{n}$$

New observations are $x_1 + a, x_2 + a, x_3 + a, ..., x_n + a$

∴ New Mean =
$$\frac{x_1 + a + x_2 + a + x_3 + a + \dots + x_n + a}{n}$$

= $\frac{x_1 + x_2 + x_3 + \dots + x_n + na}{n}$
= $\overline{x} + a$

15.

(d)
$$\frac{9}{25}$$

Explanation:

A number is selected from the numbers 1 to 25

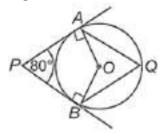
Probability of prime number which are 2, 3, 5, 7, 11, 13, 17, 19, 23 = 9

$$\therefore P(E) = \frac{m}{n} = \frac{9}{25}$$

16.

(d)
$$50^{\circ}$$

Explanation:



Since, PA and PB are tangents.

Also, tangent is perpendicular to radius at the point of contact.

$$\therefore \angle PAO = 90^{\circ} \text{ and } \angle PBO = 90^{\circ}$$

In quadrilateral APBO;

$$\angle APB + \angle PAO + \angle PBO + \angle AOB = 360^{\circ}$$

$$80^{\circ} + 90^{\circ} + 90^{\circ} + \angle AOB = 360^{\circ}$$

$$\Rightarrow \angle AOB = 100^{\circ} \Rightarrow \angle AQB = \frac{1}{2} \angle AOB = 50^{\circ}$$

17.

(c) 15 cm

Explanation:

Let PQ be the tangent.

Since OP is perpendicular to PQ, then \angle OPQ = 90°

Now, in right-angled triangle OPQ,

$$OQ^2 = OP^2 + PQ^2$$

$$\Rightarrow$$
 (17)² = (8)² + PQ²

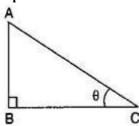
$$\Rightarrow$$
 PQ² = 289 - 64

$$\Rightarrow$$
 PQ² = 225

$$\Rightarrow$$
 PQ = 15 cm

18. (a) 60°

Explanation:



Let the height of the pole AB = 60 m, the length of the shadow BC = $20\sqrt{3}$ m and angle of elevation be heta

$$\therefore \tan \theta = \frac{AB}{BC}$$

$$\therefore \tan \theta = \frac{AB}{BC}$$

$$\Rightarrow \tan \theta = \frac{60}{20\sqrt{3}}$$

$$\Rightarrow an heta = rac{3}{\sqrt{3}} imes rac{\sqrt{3}}{\sqrt{3}}$$

$$\Rightarrow \tan \theta = \sqrt{3}$$

$$\Rightarrow \tan \theta = \tan 60^{\circ}$$

$$\Rightarrow \theta = 60^{\circ}$$

19.

(b) Both A and R are true but R is not the correct explanation of A.

Explanation:

For assertion, given equation has no solution if

$$\frac{1}{2} = \frac{1}{k} \neq \frac{-4}{-3}$$
 i.e. $\frac{4}{3}$

$$k = 2 \left[\frac{1}{2} \neq \frac{4}{3} \text{ holds} \right]$$

Assertion is true. Reason does not give the result of assertion.

20.

(d) A is false but R is true.

Explanation:

A is false but R is true.

Section B

21. We have,
$$(k-12)x^2 + 2(k-12)x + 2 = 0$$
.

$$a = k - 12, b = 2(k - 12)$$
 and $c = 2$.

The given equation will have equal roots, if

$$D = b^2 - 4ac = 0$$

$$\Rightarrow$$
 4(k - 12)² - 4 (k - 12)× 2 = 0

$$\Rightarrow$$
4(k-12) [(k-12) - 2] = 0

$$\Rightarrow$$
4(k - 12)(k - 14) = 0

$$\Rightarrow$$
4(k - 12) (k - 14) = 0 \Rightarrow k - 12 = 0 or, k - 14 = 0 \Rightarrow k = 12 or, k = 14

OR

Given,
$$3x^2 + 5\sqrt{5}x - 10 = 0$$

By splitting the middle term, we have

$$3x^2 + 6\sqrt{5}x - \sqrt{5}x - 10 = 0$$

$$\Rightarrow 3x(x+2\sqrt{5})-\sqrt{5}(x+2\sqrt{5})=0$$

$$\Rightarrow (3x - \sqrt{5})(x + 2\sqrt{5}) = 0$$

$$\therefore 3x - \sqrt{5} = 0 \text{ or } x + 2\sqrt{5} = 0$$

$$\therefore x = \frac{\sqrt{5}}{3} \text{ or } x = -2\sqrt{5}$$

22. At mid-point of AB =
$$\left(\frac{\frac{x}{2} + x + 1}{2}\right) = 5$$

or,
$$x = 6$$

$$\left(\frac{\frac{y+1}{2}+y-3}{2}\right) = -2$$

or,
$$y + 1 + 2y - 6 = -8$$

$$y = -1$$

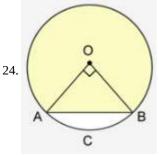
23.
$$LHS = \frac{\cos A}{1 + \sin A} + \frac{1 + \sin A}{1 + \cos A}$$

$$= \frac{\cos^2 A + (1+\sin A)^2}{(1+\sin A)\cos A} = \frac{\cos^2 A + (1+\sin A)^2}{(1+\sin A)\cos A} = \frac{\cos^2 A + 1 + \sin^2 A + 2\sin A}{(1+\sin A)\cos A} \therefore \sin^2 A + \cos^2 A = 1$$

$$= \frac{1+1+2\sin A}{(1+\sin A)\cos A}$$
: $\sin^2 A + \cos^2 A = 1$

$$=\frac{2+2\sin A}{(1+\sin A)\cos A}=\frac{2(1+\sin A)}{(1+\sin A)\cos A}$$

$$= \frac{2+2\sin A}{(1+\sin A)\cos A} = \frac{2(1+\sin A)}{(1+\sin A)\cos A} = \frac{2}{\cos A} = 2 \cdot \frac{1}{\cos A} = 2 \sec A = RHS$$



Let O be the centre of the circle and AB be the chord.

Now, Area of the minor segment $= Area \ of \ the \ sector \ OACBO - Area \ of \ \triangle AOB$

$$= 3.14 imes 10 imes 10 imes rac{90}{360} - rac{1}{2} imes 10 imes 10$$

$$=78.5-50$$

= $28.5cm^2$

OR

Here,
$$r = 14$$
 cm and $\theta = \frac{90^{\circ}}{3} = 30^{\circ}$
 \therefore Area swept = $\frac{\theta}{360^{\circ}} \times \pi r^2$
 $= \frac{30^{\circ}}{360^{\circ}} \times \frac{22}{7} \times 14 \times 14$
 $= \frac{154}{3}$ cm²

25. If two cubes are joined end to end, we get a cuboid such that

l = Length of the resulting cuboid = 10 cm +10 cm = 20 cm

b = Breadth of the resulting cuboid = 10 cm

h = Height of the resulting cuboid = 10 cm

∴ Surface area of the cuboid = 2 (lb + bh + Ih)

 \Rightarrow Surface area of the cuboid = $2(20 \times 10 + 10 \times 10 + 20 \times 10)$ cm 2 = 1000 cm 2

Section C

26. Let
$$p(x) = 6x^2 - 3 - 7x$$

For zeroes of p(x),

$$p(x) = 0$$

$$\Rightarrow$$
 6x² - 3 - 7x = 0

$$\Rightarrow$$
 6x² - 7x - 3 = 0

$$\Rightarrow$$
 6x² - 9x + 2x - 3 = 0

$$\Rightarrow$$
 3x(2x - 3) + (2x - 3) = 0

$$\Rightarrow$$
 (2x - 3) (3x + 1) = 0

$$\Rightarrow 2x - 3 = 0 \text{ or } 3x + 1 = 0$$

$$\Rightarrow x = \frac{3}{2} \text{ or } x = -\frac{1}{3} \Rightarrow x = \frac{3}{2}, -\frac{1}{3}$$

$$\Rightarrow x=rac{3}{2} ext{ or } x=-rac{1}{3} \Rightarrow x=rac{3}{2},-rac{1}{3}$$
 So, the zeroes of p(x) are $rac{3}{2}$ and $-rac{1}{3}$

We observe that Sum of its zeroes

$$=\frac{3}{2}+\left(-\frac{1}{3}\right)=\frac{3}{2}-\frac{1}{3}$$

$$= \frac{9-2}{6} = \frac{7}{6} = \frac{-(-7)}{6} = -\frac{\text{Coefficient of } x}{\text{Coefficient of } x^2}$$

Product of its zeroes =
$$\left(\frac{3}{2}\right) \times \left(-\frac{1}{3}\right)$$

$$=-\frac{1}{2}=-\frac{3}{6}=\frac{\text{Constant term}}{\text{Coefficient of }\mathbf{x}^2}$$

27. Let the digits at units and tens place of the given number be x and y respectively

Thus, the number is 10y + x.

The sum of the two digits of the number is 9.

Thus, we have
$$x + y = 9$$
(i)

After interchanging the digits, the number becomes 10x + y.

Also, 9 times the number is equal to twice the number obtained by reversing the order of the digits.

Thus, we have

$$9(10y + x) = 2(10x + y)$$

$$\Rightarrow 90y + 9x = 20x + 2y$$

$$\Rightarrow 20x + 2y - 90y - 9x = 0$$

$$\Rightarrow 11x - 88y = 0$$

$$\Rightarrow 11(x - 8y) = 0$$

$$\Rightarrow x - 8y = 0$$
....(ii)

So, we have the systems of equations

$$x + y = 9,$$

$$x - 8y = 0$$

Here x and y are unknowns.

Substituting x = 8y from the second equation to the first equation, we get

$$8y + y = 9$$

$$\Rightarrow 9y = 9$$

$$\Rightarrow y = \frac{9}{9}$$

$$\Rightarrow y = 1$$

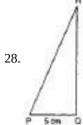
Substituting the value of y in the second equation, we have

$$x - 8 \times 1 = 0$$

$$\Rightarrow x - 8 = 0$$

$$\Rightarrow x = 8$$

 \therefore the number is $10 \times 1 + 8 = 18$



In $\triangle PQR$, by Pythagoras theorem

$$PR^2 = PO^2 + OR^2$$

$$\Rightarrow (25 - QR)^2 = 5^2 + QR^2 [\because PR + QR = 25 \text{ cm} \Rightarrow PR = 25 - QR]$$

$$625 - 50QR + QR^2 = 25 + QR^2$$

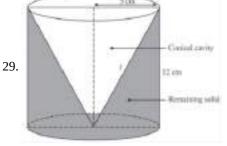
$$\Rightarrow 600 - 50QR = 0$$

$$\Rightarrow QR = \frac{600}{50} = 12 \text{ cm}$$

Now,
$$PR + QR = 25 \text{ cm}$$

$$\Rightarrow$$
 PR = 25 - Q R = 25 - 12 = 13 cm

Hence,
$$\sin P = \frac{QR}{PR} = \frac{12}{13}$$
, $\cos P = \frac{PQ}{PR} = \frac{5}{13}$ and, $\tan P = \frac{QR}{PQ} = \frac{12}{5}$



Radius of common base = 5 cm

Height of cylinder = 12 cm

$$l^2 = r^2 + h^2$$

$$\Rightarrow l^2 = 5^2 + 12^2$$

$$\Rightarrow$$
 $l^2 = 25 + 144 = 169$

$$\Rightarrow$$
l= $\sqrt{169}$ =13cm

Whole surface area of remaining cylinder

=
$$\{\text{tex}\}2\pi\text{rh}+\pi\text{r}^2+\pi\text{rl}\{/\text{tex}\}$$

=
$$\{\text{tex}\}2\pi(5)(12)+\pi(5)^2+\pi(5)(13)=210\pi \text{ cm}^2\{/\text{tex}\}$$

Volume of the remaining part of cylinder

=Volume of cylinder-volume of cone

$$=\pi r^2h-rac{1}{3}\pi r^2h$$

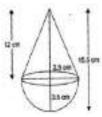
$$=\pi imes5 imes5 imes12-rac{1}{3}\pi imes5 imes5 imes12$$

$$=\pi imes5 imes5 imes12\left[1-rac{1}{3}
ight]$$

$$=\pi imes5 imes5 imes5 imes12 imesrac{2}{3}$$

$$= 200\pi \text{ cm}^3$$

OR



Radius of the cone = 3.5 cm

.: Radius of the hemisphere = 3.5 cm

Total height of the toy = 15.5 cm

 \therefore Height of the cone = 15.5 - 3.5 = 12 cm

Slant height of the cone =
$$\sqrt{{(3.5)}^2 + {(12)}^2} = \sqrt{12.25 + 144}$$

$$=\sqrt{156.25}$$
 = 12.5 cm

... Total surface area of the toy = Curved surface area of hemisphere + Curved surface area of cone

$$=2\pi r^2+\pi r l=2\pi (3.5)^2+\pi (3.5)(12.5)$$

$$=24.5\pi+43.75\pi=68.25\pi=68.25 imesrac{22}{7}$$
 = 214.5 cm²

30. The total number of marbles = 54.

As per given condition

P(getting a blue marble) = $\frac{1}{3}$ and P(getting a green marble) = $\frac{4}{9}$

Let P(getting a white marble) be x.

Since, there are only 3 types of marbles in the jar, the sum of probabilities of all three marbles must be 1.

Therefore,
$$\frac{1}{3} + \frac{4}{9} + x = 1$$

$$\Rightarrow \frac{3+4}{9} + x = 1$$
$$\Rightarrow \frac{7}{9} + x = 1$$

$$\Rightarrow \frac{7}{9} + x = 1$$

$$\Rightarrow$$
 x = 1-

$$\Rightarrow x = 1 - \frac{7}{9}$$

$$\Rightarrow x = \frac{9 - 7}{9}$$

$$\Rightarrow x = \frac{2}{9}$$

$$\Rightarrow x = \frac{2}{9}$$

Therefore, P(getting a white marble) = $\frac{2}{9}$ (1)

Let the number of white marbles be n.

$$Probability = \frac{\textit{Number of favourable outcome}}{\textit{Total Number of outcomes}}$$

Then, P(getting a white marbles) = $\frac{n}{54}$ (2)

From (1) and (2),

$$\frac{n}{54} = \frac{2}{9}$$

$$\Rightarrow$$
 n = $\frac{2 \times 54}{9}$

$$\Rightarrow n = \frac{9}{9}$$

$$\Rightarrow n = \frac{108}{9}$$

$$\Rightarrow$$
 n = 12

Thus, there are 12 white marbles in the jar.

OR

We know that in a leap year there are 366 days and, 366 days = 52 weeks and two days.

Therefore, a leap year has always 52 Sundays.

Therefore, the remaining two days can be:

- i. Sunday and Monday
- ii. Monday and Tuesday
- iii. Tuesday and Wednesday
- iv. Wednesday and Thursday
- v. Thursday and Friday
- vi. Friday and Saturday
- vii. Saturday and Sunday.

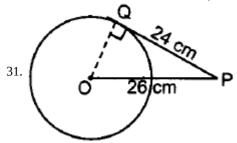
Therefore, From the above we observe that there are seven elementary events associated with this random experiment.

Let A be the event that a leap year has 53 Sundays.

Therefore, the event A will happen if the last two days of the leap year are either Sunday and Monday or Saturday and Sunday.

Therefore, favourable number of elementary events = 2

Therefore, required probability = $\frac{2}{7}$



According to the question, $OP = 26 \ cm \ and \ PQ = 24 \ cm$

In \triangle OQP, we have \angle Q = 90°

$$\begin{aligned} &{
m OP}^2 = {
m OQ}^2 + {
m PQ}^2 \ \Rightarrow (26)^2 = {
m OQ}^2 + (24)^2 \ \Rightarrow {
m OQ}^2 = 676 - 576 = 100 \ \Rightarrow & OQ = 10{
m cm} \end{aligned}$$

 \therefore Radius of the circle= 10cm

Section D

32. Given:-

Speed of boat =18 km/hr

Distance = 24 km

Let x be the speed of stream.

Let t₁ and t₂ be the time for upstream and downstream As we know that,

$$speed = \frac{\frac{distance}{time}}{time}$$

$$\Rightarrow time = \frac{\frac{distance}{speed}}{speed}$$

For upstream, Speed = (18 - x) km/hr

Distance =24 km

Time = t_1

Therefore,

$$t_1 = \frac{24}{18 - x}$$

For downstream,

Speed = (18 + x) km/hr

Distance = 24 km

Time = t_2

Therefore,

$$t_2 = \frac{24}{18 + x}$$

Now according to the question-

$$t_1 = t_2 + 1$$

$$\frac{24}{18-x} = \frac{24}{18+x} + 1$$

$$\Rightarrow \frac{1}{18-x} - \frac{1}{18+x} = \frac{1}{24}$$

$$\Rightarrow \frac{(18+x)-(18-x)}{(18-x)(18+x)} = \frac{1}{24}$$

$$\Rightarrow 48x = (18-x)(18+x)$$

$$\Rightarrow 48x = 324 + 18x - 18x - x^2$$

$$\Rightarrow$$
 48x = 324 + 18x - 18x - x²

$$\Rightarrow$$
 x² + 48x - 324 = 0

$$\Rightarrow x^2 + 54x - 6x - 324 = 0$$

$$\Rightarrow$$
 x(x + 54) -6(x + 54) = 0

$$\Rightarrow (x + 54)(x - 6) = 0$$

$$\Rightarrow$$
 x = -54 or x = 6

Since speed cannot be negative.

$$\Rightarrow$$
 x \neq -54

$$\therefore x = 6$$

Thus the speed of stream is 6 km/hr.

Total time of Journey = $t_1 + t_2$

$$= \frac{24}{18-x} + \frac{24}{18+x}$$
$$= \frac{24}{12} + \frac{24}{24} = 2 + 1 = 3 \text{ hrs.}$$

OR

Let the average speed of truck be x km/h.

$$\frac{150}{x} + \frac{200}{x+20} = 5$$

or,
$$150x + 3000 + 200x = 5x(x + 20)$$

or,
$$x^2 - 50x - 600 = 0$$

or,
$$x^2 - 60x + 10x - 600 = 0$$

or,
$$x(x-60) + 10(x-60) = 0$$

or,
$$(x-60)(x+10)=0$$

or,
$$x = 60$$
; or $x = -10$

as, speed cannot be negative

Therefore, x=60 km/h

Hence, first speed of the truck = 60 km/h

33. $\Delta PAC \sim \Delta QBC$

$$\therefore \frac{x}{y} = \frac{AC}{BC} \text{ or } \frac{y}{x} = \frac{BC}{AC} \dots (i)$$

$$\Delta RCA \sim \Delta QBA$$

 $\therefore \frac{z}{y} = \frac{AC}{AB} \text{ or } \frac{y}{z} = \frac{AB}{AC} ...(ii)$

Adding (i) and (ii)

$$\frac{y}{x} + \frac{y}{z} = \frac{BC + AB}{AC}$$

$$\Rightarrow \frac{1}{x} + \frac{1}{z} = \frac{1}{y}$$

$$\Rightarrow \frac{1}{x} + \frac{1}{z} = \frac{1}{y}$$

	x - z - y						
34.	Class	х _і	f _i	$\mathbf{u_i} = \frac{\mathbf{x_i} - 57 \cdot 5}{5}$	f_iu_i		
	40 - 45	42.5	5	-3	-15		
	45 - 50	47·5	11	-2	-22		
	50 - 55	52·5	20	-1	-20		
	55 - 60	57·5=a	24	0	0		
	60 - 65	62·5	28	1	28		
	65 - 70	67·5	12	2	24		
			100		-5		

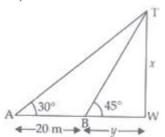
Mean = a +
$$\frac{\sum f_i u_i}{\sum f_i}$$
 × h
= 57.5 + $\frac{-5}{100}$ × 5 = 57.25
Mode = $l + \left(\frac{f_1 - f_0}{2f_1 - f_0 - f_2}\right)$ × h
= 60 + $\frac{28 - 24}{2(28) - 24 - 12}$ × 5 = 61

35. Let the height of the vertical tower (TW) = x m

When a observer at A, makes angle of elevation at the top of tower is 30°.

Now, angle of elevation of the top of tower is increased by 15° when observer moves 20m towards the tower.

i.e., it becomes $30^{\circ} + 15^{\circ} = 45^{\circ}$.



In \triangle TWB,

$$\tan 45^\circ = \frac{P}{B} = \frac{x}{y}$$

$$\Rightarrow 1 = \frac{x}{y}$$

$$\Rightarrow$$
 x = y(i)

Now, \triangle TWA, we have

$$\tan 30^{\circ} = \frac{P}{B} = \frac{x}{20+y}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{x}{20+x} \text{ [From (i)]}$$

$$\Rightarrow \sqrt{3}x = 20 + x$$

$$\Rightarrow \sqrt{3}x - x = 20$$

$$\Rightarrow x(\sqrt{3}-1)$$
 = 20

$$\Rightarrow x(\sqrt{3-1}) - 20$$

$$\Rightarrow x = \frac{20}{(\sqrt{3}-1)} \times \frac{\sqrt{3}+1}{(\sqrt{3}+1)}$$

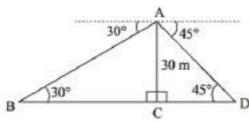
$$\Rightarrow x = \frac{20(\sqrt{3}+1)}{3-1} = \frac{20(\sqrt{3}+1)}{2}$$

$$\Rightarrow x = 10(1.732 + 1)$$

$$\Rightarrow x = 10 \times 2.732 = 27.32m$$

Hence, the height of the tower (TW) is 27.32 m.

OR



In
$$\triangle$$
ABC, $\frac{AC}{BC}$ = tan 30°

$$\Rightarrow$$
 BC = $30\sqrt{3}$ m

In
$$\triangle ACD$$
, $\frac{AC}{CD}$ = tan 45°

$$\Rightarrow$$
 CD = 30 m

Width of river = BD

$$= BC + CD$$

$$=30(\sqrt{3}+1)$$
m = 30 × 2.73m = 81.9m

Section E

36. i. HCF (96, 240, 336) = 48

ii. Number of stacks =
$$\frac{336}{48}$$
 = 7

iii. Total number of stacks =
$$\frac{96}{48} + \frac{240}{48} + \frac{336}{48}$$

= 14

OR

Height of each stack of History = $48 \times 1.8 = 86.4$ cm

Height of each stack of Science = $48 \times 2.2 = 105.6$ cm

Height of each stack of Mathematics = $48 \times 2.5 = 120$ cm

37. i. 8 coins

ii. Money in the piggy bank day wise 5, 10, 15, 20 \dots

Money after 8 days = ₹ 180

iii. a. We can have at most 120 coins.

$$\frac{n}{2}[2(1)+(n-1)1]=120$$

$$n^2 + n - 240 = 0$$

Solving for n, we get, n = 15 as n \neq -16

 \therefore Number of days = 15

OR

b. Total money saved = $120 \times 5 = 700$

38. i. Mid point of FG is
$$\left(\frac{-3+1}{2}, \frac{0+4}{2}\right) = (-1, 2)$$

ii. a.
$$AC = \sqrt{(-1-3)^2 + (-2-4)^2}$$
 $= \sqrt{52} \text{ or } 2\sqrt{13}$

OR

b. The coordinates of required point are $\left(\frac{1\times 3+3\times 3}{1+3},\frac{1\times 2+3\times 4}{1+3}\right)$ i.e. $\left(3,\frac{7}{2}\right)$

iii. D(-2, -5)