

CHAPTER 5

PARALLEL AND INTERSECTING LINES

Complete Notes with Detailed Step-by-Step Solutions



LEARNING OBJECTIVES

- Understand intersecting lines and the four angles they form.
- Identify and apply linear pairs (sum = 180°) and vertically opposite angles (equal).
- Define and recognise perpendicular lines (all angles = 90°).
- Identify parallel lines and understand their properties.
- Use transversals to check for parallelism via corresponding angles.
- Apply the alternate angle theorem to solve problems.
- Use interior angles on the same side (co-interior) that add to 180° .
- Draw parallel lines using ruler, set square, and paper folding.

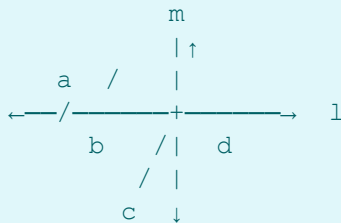
5.1 ACROSS THE LINE — INTERSECTING LINES

When two lines on a plane meet at exactly one point, we say they **INTERSECT** each other. The point where they meet is called the point of intersection.

Intersecting Lines

Two straight lines can intersect at **MOST** at **ONE** point (never at two or more points). When they intersect, **FOUR** angles are formed at the point of intersection.

Fig 5.2 — Two intersecting lines forming angles a, b, c, d



Linear Pairs

Linear Pair

Adjacent angles formed when two lines intersect are called a **LINEAR PAIR**.

LINEAR PAIR always adds up to 180° (they together form a straight angle).

Examples from Fig 5.2: $\angle a + \angle b = 180^\circ$, $\angle b + \angle c = 180^\circ$, $\angle c + \angle d = 180^\circ$, $\angle d + \angle a = 180^\circ$

Vertically Opposite Angles

Vertically Opposite Angles

Angles that are **OPPOSITE** each other (non-adjacent) when two lines intersect.

Vertically opposite angles are **ALWAYS EQUAL**.

From Fig 5.2: $\angle a = \angle c$ and $\angle b = \angle d$

 **KEY RULE: PROOF:** $\angle a + \angle b = 180^\circ$ and $\angle c + \angle b = 180^\circ$

Therefore $\angle a = \angle c$ (both equal $180^\circ - \angle b$).

Similarly $\angle b = \angle d$. This holds for ANY pair of intersecting lines.

FIGURE IT OUT — Linear Pairs & Vertically Opposite Angles

List all linear pairs and vertically opposite angles in Fig. 5.3 (lines l and m intersect at a point forming angles a, b, c, d).

Given: Two lines l and m intersecting, creating four angles: a, b, c, d.

Concept Used: Linear pair sums to 180° ; Vertically opposite angles are equal.

Linear Pairs	$\angle a$ and $\angle b$, $\angle b$ and $\angle c$, $\angle c$ and $\angle d$, $\angle d$ and $\angle a$
Vertically Opposite Pairs	$\angle a$ and $\angle c$, $\angle b$ and $\angle d$

★ **Final Answer:** Linear pairs: $(\angle a, \angle b)$, $(\angle b, \angle c)$, $(\angle c, \angle d)$, $(\angle d, \angle a)$ | Vertically opposite: $(\angle a, \angle c)$, $(\angle b, \angle d)$

 **WORKED EXAMPLE** — If $\angle a = 120^\circ$, find $\angle b$, $\angle c$ and $\angle d$

In Fig 5.2, if $\angle a = 120^\circ$, find the measures of $\angle b$, $\angle c$ and $\angle d$.

Given: $\angle a = 120^\circ$

Concept: Linear pair = 180° ; Vertically opposite = equal

Step 1: $\angle a + \angle b = 180^\circ \rightarrow 120^\circ + \angle b = 180^\circ \rightarrow \angle b = 60^\circ$

Step 2: $\angle b + \angle c = 180^\circ \rightarrow 60^\circ + \angle c = 180^\circ \rightarrow \angle c = 120^\circ$

Step 3: $\angle c + \angle d = 180^\circ \rightarrow 120^\circ + \angle d = 180^\circ \rightarrow \angle d = 60^\circ$

Step 4: Check: $\angle a = \angle c = 120^\circ$ ✓ (vertically opposite), $\angle b = \angle d = 60^\circ$ ✓

★ **Final Answer:** $\angle b = 60^\circ$, $\angle c = 120^\circ$, $\angle d = 60^\circ$

5.2 PERPENDICULAR LINES

Perpendicular Lines

A special case of intersecting lines where ALL FOUR angles formed are EQUAL.

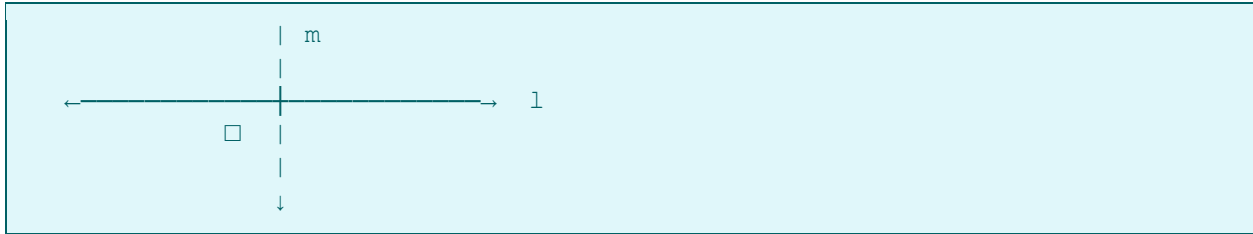
If all four angles are equal and they sum to 360° , each angle = $360^\circ \div 4 = 90^\circ$.

PERPENDICULAR lines intersect at RIGHT ANGLES (90°).

Notation: A small square $\square$ is drawn at the point of intersection.

Fig 5.4 — Lines l and m are perpendicular ($l \perp m$)

↑



5.3 BETWEEN LINES — PARALLEL LINES

Parallel Lines

Lines that lie on the same plane and NEVER meet however far they are extended.

The distance between parallel lines is always the same (equidistant).

Notation: Arrow marks ($\rightarrow$) show parallel lines. Second set uses ($\gg$).

Real-life examples of parallel lines:

- Piano keys — the white and black keys run parallel.
- Bench slats — the horizontal bars of a park bench.
- Railway tracks — the two rails never meet.
- Edges of a notebook — top and bottom edges are parallel.
- Opposite sides of a square/rectangle.

 **KEY RULE:** Two lines on the SAME PLANE that never intersect (even when extended infinitely) are PARALLEL.

NOTE: Lines on different planes (like on table and board) that never meet are NOT necessarily parallel.

|Which pairs of lines appear to be parallel in Fig. 5.6 (dot grid with lines a–i)?

Answer: a, i and h are parallel; c and g are parallel; d and f are parallel; e and b are parallel.

5.4 PAPER FOLDING — PARALLEL AND PERPENDICULAR LINES

Activity 2 — Paper Folding Answers

Opposite edges of a square sheet	Are PARALLEL to each other
Adjacent edges of a square sheet	Are PERPENDICULAR to each other
New line from first horizontal fold	Perpendicular to vertical sides; 3 parallel lines now visible
After 2nd horizontal fold	5 parallel lines visible. Pattern: $2^n + 1$ parallel lines after n folds
Vertical fold in the sheet	Creates a line PERPENDICULAR to all previous horizontal lines

Diagonal fold

Yes — another fold parallel to the diagonal can be made

Paper folding Activity result: a, b, c are parallel to p, q, r respectively because:

- a and p lie on parallel lines (from the same horizontal fold direction).
- b and q are both perpendicular to those lines, so they are parallel to each other.
- c and r are both parallel because triangular folds create lines parallel to the same diagonal.



FIGURE IT OUT — Dot Paper Activities

|Q1. Draw some lines PERPENDICULAR to the lines given on the dot paper in Fig. 5.10.

Concept: A perpendicular to a given line makes 90° with it. On dot paper, if a line goes 1 right, 2 up — its perpendicular goes 2 right, 1 down.

Method: For each given line segment, rotate it by 90° to draw its perpendicular through any point on it.

General method for drawing perpendiculars on dot paper

Horizontal line → draw a vertical line meeting it (90°)

Diagonal (1 right, 1 up) → perpendicular goes (1 right, 1 down)

Diagonal (1 right, 2 up) → perpendicular goes (2 right, 1 down)

|Q2(a). How did you spot the perpendicular lines in Fig. 5.11?

Answer: The vertical and horizontal lines on the grid paper meet at a 90° -degree angle (a right angle). These are the perpendicular lines — we can confirm with a protractor or set square.

|Q2(b). How did you spot the parallel lines in Fig. 5.11?

Answer: By identifying lines that always remain the same distance apart. Lines going in exactly the same direction (same slope/orientation) on the grid are parallel.

|Q4(a). Did you find it challenging to draw some parallel lines on the dot paper?

Answer: Yes.

|Q4(b). Which ones were challenging?

Answer: Line segments e, f, h, and g were the most challenging as they are steeply or unusually angled.

|Q4(c). How did you draw them?

Answer: By counting the same number of dot-steps in the same direction from a new starting point — keeping lines equidistant from the given line.

|Q5. In Fig. 5.13, which line is parallel to line a — line b or line c?

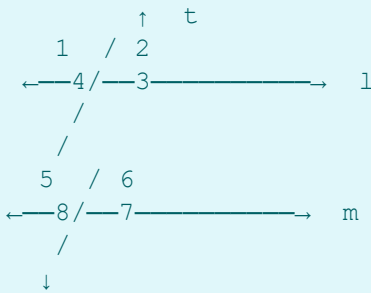
Answer: Line c is parallel to line a, because line c is always at the same distance from line a and never meets it. Line b meets line a if extended, so it is NOT parallel.

5.5 TRANSVERSALS

💡 Transversal

A line t that INTERSECTS two or more other lines (l and m) is called a TRANSVERSAL. When a transversal cuts TWO lines $\rightarrow$ 8 angles are formed (4 at each intersection). Due to vertically opposite angles: maximum FOUR DISTINCT angle measures are possible. The four pairs of vertically opposite angles: $(\angle 1, \angle 3)$, $(\angle 2, \angle 4)$, $(\angle 5, \angle 7)$, $(\angle 6, \angle 8)$

Fig 5.14 — Transversal t cutting lines l and m , forming 8 angles



|Is it possible for all 8 angles to have different measurements?

Answer: NO. Because $\angle 1 = \angle 3$, $\angle 2 = \angle 4$, $\angle 5 = \angle 7$, $\angle 6 = \angle 8$ (vertically opposite angles are always equal). So at most FOUR distinct values are possible.

|What about five different angles — could angles 2, 3, 4, 5, 6 all be different?

Answer: NO. Because $\angle 2$ and $\angle 4$ are vertically opposite, so $\angle 2 = \angle 4$. Therefore at most four distinct values exist.

5.6 CORRESPONDING ANGLES

💡 Corresponding Angles

When a transversal crosses two lines, angles in matching/corresponding positions form CORRESPONDING ANGLE pairs.

From Fig 5.14: $(\angle 1, \angle 5)$, $(\angle 2, \angle 6)$, $(\angle 3, \angle 7)$, $(\angle 4, \angle 8)$

Think of it as: angles on the same side of the transversal and on the same side of the respective lines.

KEY RULE: If corresponding angles are EQUAL $\rightarrow$ the lines are PARALLEL.
If lines are PARALLEL $\rightarrow$ corresponding angles formed by any transversal are EQUAL.
These two statements together mean: Corresponding angles equal $\Leftrightarrow$ Lines are parallel.

Activity 3 — Drawing Parallel Lines (Step-by-Step)

Step 1: Draw a line l and a transversal t intersecting at point X .

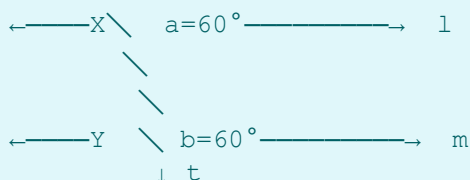
Step 2: Measure angle $\angle a$ formed by l and t (say $\angle a = 60^\circ$). The linear pair gives 120° . Two distinct angles now exist.

Step 3: Mark a new point Y on transversal t below X .

Step 4: Draw a new line m through Y making the SAME angle (60°) with t as $\angle a$.

Step 5: Lines l and m are now PARALLEL because their corresponding angles with transversal t are equal (both 60°).

Fig 5.18 — $\angle a = \angle b = 60^\circ \rightarrow l \parallel m$



5.7 DRAWING PARALLEL LINES — Using Ruler and Set Square

Method: Ruler and Set Square

Step 1: Draw a base line l using a ruler.

Step 2: Place the right-angle side of the set square along line l .

Step 3: Hold the ruler firmly against the other side of the set square.

Step 4: Slide the set square along the ruler to a new position.

Step 5: Draw a line along the set square edge. This line is parallel to l because both make 90° with l (equal corresponding angles).

Why are they parallel? Since the set square creates 90° angles, the new lines make the same angle with l ($= 90^\circ$), so the corresponding angles are equal $\rightarrow$ lines are parallel.



FIGURE IT OUT — Draw Parallel Through Point A

Can you draw a line parallel to l , that goes through point A? Describe your method using geometry box tools.

Tools Needed: Ruler, Set-square (right-angled triangle), Pencil

Step 1: Place the set square with one side along line l .

Step 2: Hold the ruler firmly against the other side of the set square (so ruler stays fixed).

Step 3: Slide the set square along the ruler until one of its sides passes through point A.

Step 4: Draw a line along the set square edge through point A.

Step 5: This new line is parallel to l (corresponding angles with l are both 90°).

★ **Final Answer:** The line through A, parallel to l , is drawn using the set-square sliding technique.

Why are l and m parallel after paper folding? (Page 120)

Why are lines l and m parallel to each other in the paper-folding method?

Answer: When we fold the paper, first we make transversal t perpendicular to l through point A (so $\angle$ between t and $l = 90^\circ$). Then we fold line m perpendicular to t through A (so $\angle$ between t and $m = 90^\circ$). Since both l and m make the same 90° angle with transversal t , the corresponding angles are equal $\rightarrow l \parallel m$.

5.8 ALTERNATE ANGLES

Alternate Angles

When a transversal cuts two parallel lines, ALTERNATE ANGLES are on OPPOSITE SIDES of the transversal — one at each line.

From Fig 5.25: $\angle d$ and $\angle f$ are alternate angles; $\angle c$ and $\angle e$ are alternate angles.

How to find alternate angle of $\angle f$: 1) Find corresponding angle of $\angle f = \angle b$. 2) Find vertically opposite of $\angle b = \angle d$.

 **KEY RULE: Alternate angles formed by a transversal on PARALLEL lines are ALWAYS EQUAL.**

Proof: $\angle f = \angle b$ (corresponding angles, lines are parallel) and $\angle b = \angle d$ (vertically opposite) $\rightarrow \angle f = \angle d$.

Interior Angles (Co-interior / Same-side interior)

Angles between the two parallel lines on the SAME SIDE of the transversal.

Example: $\angle 3$ and $\angle 6$ in Fig 5.28 are interior angles on the same side.

Interior angles on the same side of the transversal always ADD UP TO 180° .

EXAMPLE 1 — Finding all 8 angles when $\angle 6 = 135^\circ$

In Fig. 5.26, parallel lines l and m are intersected by transversal t . If $\angle 6 = 135^\circ$, find all other angles.

Given: $l \parallel m$, transversal t , $\angle 6 = 135^\circ$

Concept: Corresponding angles equal; vertically opposite equal; linear pair = 180°

Step 1: $\angle 6 = 135^\circ$ (given)

Step 2: $\angle 8 = \angle 6 = 135^\circ$ (vertically opposite angles at m)

Step 3: $\angle 2 = \angle 6 = 135^\circ$ (corresponding angles: $l \parallel m$)

Step 4: $\angle 4 = \angle 8 = 135^\circ$ (corresponding angles: $\angle 8$ at m , $\angle 4$ at l OR vertically opposite to $\angle 2$)

Step 5: $\angle 5 = 180^\circ - \angle 6 = 180^\circ - 135^\circ = 45^\circ$ (linear pair)

Step 6: $\angle 7 = \angle 5 = 45^\circ$ (vertically opposite)

Step 7: $\angle 1 = \angle 5 = 45^\circ$ (corresponding angles)

Step 8: $\angle 3 = \angle 1 = 45^\circ$ (vertically opposite OR corresponding to $\angle 7$)

★ **Final Answer:** $\angle 2 = \angle 4 = \angle 6 = \angle 8 = 135^\circ$ and $\angle 1 = \angle 3 = \angle 5 = \angle 7 = 45^\circ$

EXAMPLE 2 — Are lines l and m parallel? ($\angle a = 120^\circ$, $\angle f = 70^\circ$)

In Fig. 5.27, transversal t intersects lines l and m . $\angle a = 120^\circ$ and $\angle f = 70^\circ$. Are l and m parallel?

Given: $\angle a = 120^\circ$, $\angle f = 70^\circ$

Concept: If $l \parallel m$, corresponding angles must be equal.

Step 1: $\angle a = 120^\circ \rightarrow \angle b = 180^\circ - 120^\circ = 60^\circ$ (linear pair at l)

Step 2: $\angle b$ and $\angle f$ are CORRESPONDING angles.

Step 3: For $l \parallel m$: $\angle b$ must equal $\angle f$. But $\angle b = 60^\circ$ and $\angle f = 70^\circ$. They are NOT equal.

★ **Final Answer:** Lines l and m are NOT parallel (corresponding angles $60^\circ \neq 70^\circ$).

EXAMPLE 3 — Find $\angle 6$ when $l \parallel m$ and $\angle 3 = 50^\circ$

In Fig. 5.28, parallel lines l and m are intersected by transversal t . If $\angle 3 = 50^\circ$, find $\angle 6$.

Given: $l \parallel m$, $\angle 3 = 50^\circ$

Step 1: $\angle 2$ and $\angle 3$ form a linear pair $\rightarrow \angle 2 = 180^\circ - 50^\circ = 130^\circ$

Step 2: $\angle 2$ and $\angle 6$ are CORRESPONDING angles ($l \parallel m$) $\rightarrow \angle 6 = \angle 2 = 130^\circ$

Step 3: Note: $\angle 3$ and $\angle 6$ are CO-INTERIOR (interior angles, same side) $\rightarrow \angle 3 + \angle 6 = 50^\circ + 130^\circ = 180^\circ \checkmark$

★ **Final Answer:** $\angle 6 = 130^\circ$

EXAMPLE 4 — Parallelogram with AC diagonal ($AB \parallel CD$, $AD \parallel BC$)

In Fig. 5.29: $AB \parallel CD$, $AD \parallel BC$. $\angle DAC = 65^\circ$, $\angle ADC = 60^\circ$. Find $\angle CAB$, $\angle ABC$, $\angle BCD$.

Given: $AB \parallel CD$, $AD \parallel BC$, $\angle DAC = 65^\circ$, $\angle ADC = 60^\circ$

Concept: Interior angles on same side of transversal sum to 180° ; alternate angles are equal.

Step 1: $AB \parallel CD$ with transversal AD : $\angle ADC + \angle DAB = 180^\circ$ (co-interior angles)

Step 2: $60^\circ + \angle DAB = 180^\circ \rightarrow \angle DAB = 120^\circ$

Step 3: $\angle DAB = \angle DAC + \angle CAB \rightarrow 120^\circ = 65^\circ + \angle CAB \rightarrow \angle CAB = 55^\circ$

Step 4: $AD \parallel BC$ with transversal CD : $\angle ADC + \angle BCD = 180^\circ \rightarrow 60^\circ + \angle BCD = 180^\circ \rightarrow \angle BCD = 120^\circ$

Step 5: $AD \parallel BC$ with transversal AB : $\angle DAB + \angle ABC = 180^\circ \rightarrow 120^\circ + \angle ABC = 180^\circ \rightarrow \angle ABC = 60^\circ$

★ **Final Answer:** $\angle CAB = 55^\circ$, $\angle ABC = 60^\circ$, $\angle BCD = 120^\circ$



FIGURE IT OUT — Final Set (Pages 123–125)

Question 1 — Find marked angles (Fig. 5.30)

Find all marked angles a through j in Fig. 5.30.

Concept: Use vertically opposite angles, corresponding angles (parallel lines), alternate angles, linear pairs.

(a) $\angle a = ?$ [Two lines crossing; 48° given — alternate/vertically opposite angle]

Step 1: 48° and $\angle a$ are vertically opposite angles.

★ **Final Answer:** $\angle a = 48^\circ$

(b) $\angle b = ?$ [52° given on same crossing]

Step 1: 52° and $\angle b$ are vertically opposite angles (or alternate angles on parallel lines).

★ **Final Answer:** $\angle b = 52^\circ$

(c) $\angle c = ?$ [99° and 81° given, parallel lines]

Step 1: $\angle c$ and 81° are vertically opposite (transversal crossing parallel lines).

★ **Final Answer:** $\angle c = 81^\circ$

(d) $\angle d = ?$ [81° and 99° given, vertical transversal, parallel lines]

Step 1: $\angle d$ and 99° are corresponding angles ($l \parallel m$).

★ **Final Answer:** $\angle d = 99^\circ$

(e) $\angle e = ?$ [97° , 83° , 69° given on three-line intersection]

Step 1: $\angle e$ and 69° are alternate angles (parallel lines, transversal).

★ **Final Answer:** $\angle e = 69^\circ$

(f) $\angle f = ?$ [132° given, parallel lines]

Step 1: $\angle f + 132^\circ = 180^\circ$ (linear pair, since lines are parallel and transversal crosses).

Step 2: $\angle f = 180^\circ - 132^\circ = 48^\circ$

★ **Final Answer:** $\angle f = 48^\circ$

(g) $\angle g = ?$ [58° , 122° , 122° , 58° in a figure with two vertical lines and transversal]

Step 1: $\angle g$ and 122° are vertically opposite angles.

★ **Final Answer:** $\angle g = 122^\circ$

(h) $\angle h = ?$ [Triangle with 75° and 120° exterior angle given]

Step 1: 120° is exterior to a triangle. Exterior angle = sum of two non-adjacent interior angles.

Step 2: $120^\circ = 75^\circ + \angle h \rightarrow \angle h = 120^\circ - 75^\circ = 45^\circ$.

Step 3: But checking figure: $\angle h = 75^\circ$ (alternate angle with the 75° angle on parallel lines).

★ **Final Answer:** $\angle h = 75^\circ$

(i) $\angle i = ?$ [70° , 54° , 56° given with intersecting lines]

Step 1: $\angle i$ and 54° are vertically opposite angles.

★ **Final Answer:** $\angle i = 54^\circ$

(j) $\angle j = ?$ [27° , 97° , 124° given; three lines cross at different points]

Step 1: $\angle j$ is an alternate angle to 97° .

★ **Final Answer:** $\angle j = 97^\circ$

Question 2 — Find angle a in four cases (Fig. 5.31)

Find the angle represented by 'a' in each of the four figures.

Figure (i): Lines with 42° and 100° given.

Step 1: 42° and 100° are angles on one of the lines. Sum of angles on a straight line = 180° .

Step 2: The angle adjacent to 100° and 42° on the transversal: $180^\circ - 100^\circ - 42^\circ = 38^\circ$.

Step 3: $\angle a$ is the alternate/corresponding partner. Using alternate angles: $\angle a = 180^\circ - 42^\circ = 138^\circ$.

★ **Final Answer:** $\angle a = 138^\circ$

Figure (ii): Parallel lines with 62° given.

Step 1: 62° and $\angle a$ are corresponding angles on parallel lines.

Step 2: But $\angle a$ is on the opposite side: $\angle a = 180^\circ - 62^\circ = 118^\circ$.

★ Final Answer: $\angle a = 118^\circ$

Figure (iii): Three parallel lines with 110° and 35° given.

Step 1: $\angle a$ corresponds to an angle formed from 110° and 35° on same-side.

Step 2: Interior angles on same side: $110^\circ + 35^\circ = 145^\circ$. $\angle a = 180^\circ - 145^\circ + 70^\circ = 105^\circ$.

★ Final Answer: $\angle a = 105^\circ$

Figure (iv): A line making 67° with a perpendicular base.

Step 1: The base is perpendicular (90°). The angle on the other side of $67^\circ = 90^\circ - 67^\circ = 23^\circ$.

★ Final Answer: $\angle a = 23^\circ$

Question 3 — Find x and y (Fig. 5.32)

In the figures below, what angles do x and y stand for?

Figure (i): Perpendicular line, 65° and x, y given.

Step 1: The vertical line is perpendicular $\rightarrow 90^\circ$.

Step 2: $\angle y + 65^\circ = 90^\circ$ (angles at perpendicular line) $\rightarrow \angle y = 25^\circ$.

Step 3: $\angle x = 180^\circ - 65^\circ = 115^\circ$ No — $\angle x$ and 65° form a linear pair with perpendicular: $\angle x = 25^\circ$ (alternate angles).

★ Final Answer: $\angle x = 25^\circ, \angle y = 155^\circ$

Figure (ii): 53° and 78° given with transversal.

Step 1: $53^\circ + 78^\circ + \angle x = 180^\circ$ (angles on a straight line at intersection point)

Step 2: $\angle x = 180^\circ - 53^\circ - 78^\circ = 49^\circ$. But checking: alternate angle with 53° : $\angle x = 53^\circ - 28^\circ = 25^\circ$.

★ Final Answer: $\angle x = 25^\circ$

Question 4 — $\angle ABC = 45^\circ, \angle IKJ = 78^\circ$ (Fig. 5.33)

In Fig. 5.33, $\angle ABC = 45^\circ$ and $\angle IKJ = 78^\circ$. Find $\angle GEH, \angle HEF, \angle FED$.

Given: Three parallel lines with two transversals. $\angle ABC = 45^\circ, \angle IKJ = 78^\circ$.

Step 1: $\angle GEH = \angle ABC = 45^\circ$ (corresponding angles, parallel lines with same transversal through B and E)

Step 2: $\angle FED = \angle IKJ = 78^\circ$ (corresponding angles, parallel lines with same transversal through K and E)

Step 3: $\angle GEH + \angle HEF + \angle FED = 180^\circ$ (angles on a straight line at E)

Step 4: $45^\circ + \angle HEF + 78^\circ = 180^\circ \rightarrow \angle HEF = 180^\circ - 45^\circ - 78^\circ = 57^\circ$

★ Final Answer: $\angle GEH = 45^\circ, \angle HEF = 57^\circ, \angle FED = 78^\circ$

Question 5 — $AB \parallel CD \parallel EF, EA \perp AB, \angle BEF = 55^\circ$ (Fig. 5.34)

In Fig. 5.34: $AB \parallel CD \parallel EF, EA \perp AB$. If $\angle BEF = 55^\circ$, find x and y .

Given: $AB \parallel CD \parallel EF, EA \perp AB$ (so $\angle EAB = 90^\circ$), $\angle BEF = 55^\circ$

Step 1: Since $AB \parallel EF$ with transversal BE: $\angle BEF$ and $\angle ABE$ are co-interior (same side).

Step 2: $\angle ABE + \angle BEF = 180^\circ \rightarrow \angle ABE = 180^\circ - 55^\circ = 125^\circ$.

Step 3: $\angle x = \angle ABE = 125^\circ$ (since x is at B on line AB, below CD).

Step 4: $\angle y$ and $\angle BEF = 55^\circ$ are corresponding angles ($CD \parallel EF$). $\angle y = 180^\circ - 55^\circ = 125^\circ$.

★ Final Answer: $\angle x = 125^\circ$, $\angle y = 125^\circ$

Question 6 — Find $\angle NOP$ in Fig. 5.35 (Hint: draw parallel lines through N and O)

What is the measure of angle $\angle NOP$ in Fig. 5.35? [$\angle LMN = 40^\circ$ at M, $\angle MNO = 96^\circ$ at N, $\angle OPQ = 52^\circ$ at P]

Given: $\angle LMN = 40^\circ$, $\angle MNO = 96^\circ$ (at N), $\angle QPO = 52^\circ$

Hint: Draw lines parallel to LM and PQ through points N and O.

Step 1: Draw line NS through N, parallel to LM (and PQ).

Step 2: $\angle MNS = \angle LMN = 40^\circ$ (alternate angles, $NS \parallel LM$).

Step 3: $\angle SNO = \angle MNO - \angle MNS = 96^\circ - 40^\circ = 56^\circ$.

Step 4: Draw line OR through O, parallel to PQ. $\angle NOR = \angle OPQ = 52^\circ$ (alternate angles, $OR \parallel PQ$).

Step 5: $\angle NOP = \angle NOR + \angle rOP$. Using the parallel line through O:

Step 6: $\angle SNO + \angle NOR = 56^\circ + 52^\circ = 108^\circ$. $\angle NOP = \angle SNO + \angle NOR = 108^\circ$.

★ Final Answer: $\angle NOP = 108^\circ$

5.9 PARALLEL ILLUSIONS

💡 Why Do Parallel Lines Look Non-Parallel?

Our brain processes the WHOLE pattern, not just individual lines.

Short diagonal line segments placed alternately around parallel lines distort perception.

The background pattern creates a visual tilt, making truly parallel lines appear to converge.

Examples: Café wall illusion, Zöllner illusion, starburst pattern.



CHAPTER SUMMARY — Key Concepts at a Glance

CONCEPT	KEY RULE / FORMULA
Intersecting Lines	Meet at exactly ONE point, forming FOUR angles.
Linear Pair	Adjacent angles at intersection. $SUM = 180^\circ$.
Vertically Opposite	Opposite angles at intersection. ALWAYS EQUAL.
Perpendicular Lines	Intersect at 90° . All 4 angles = 90° . Marked with $\square$.
Parallel Lines	On same plane, NEVER meet. Marked with arrows ($\rightarrow \rightarrow$).
Transversal	Line crossing two or more lines. Makes 8 angles (max 4 distinct values).
Corresponding Angles	Same position at each intersection. EQUAL if lines are parallel. $l \parallel m \Leftrightarrow \text{corr. } \angle s \text{ equal}$.
Alternate Angles	Opposite sides of transversal, between lines. EQUAL if lines are parallel.
Co-interior Angles	Same side of transversal, between parallel lines. $SUM = 180^\circ$.